

# ON THE ADVERSARIAL ROBUSTNESS OF UNCERTAINTY AWARE DEEP NEURAL NETWORKS

APRIL 29<sup>TH</sup>, 2019

PREPARED BY: ALI HARAKEH



UNIVERSITY OF TORONTO  
FACULTY OF APPLIED SCIENCE & ENGINEERING

# QUESTION

Can a neural network mitigate the effects of adversarial attacks by estimating the uncertainty in its predictions ?

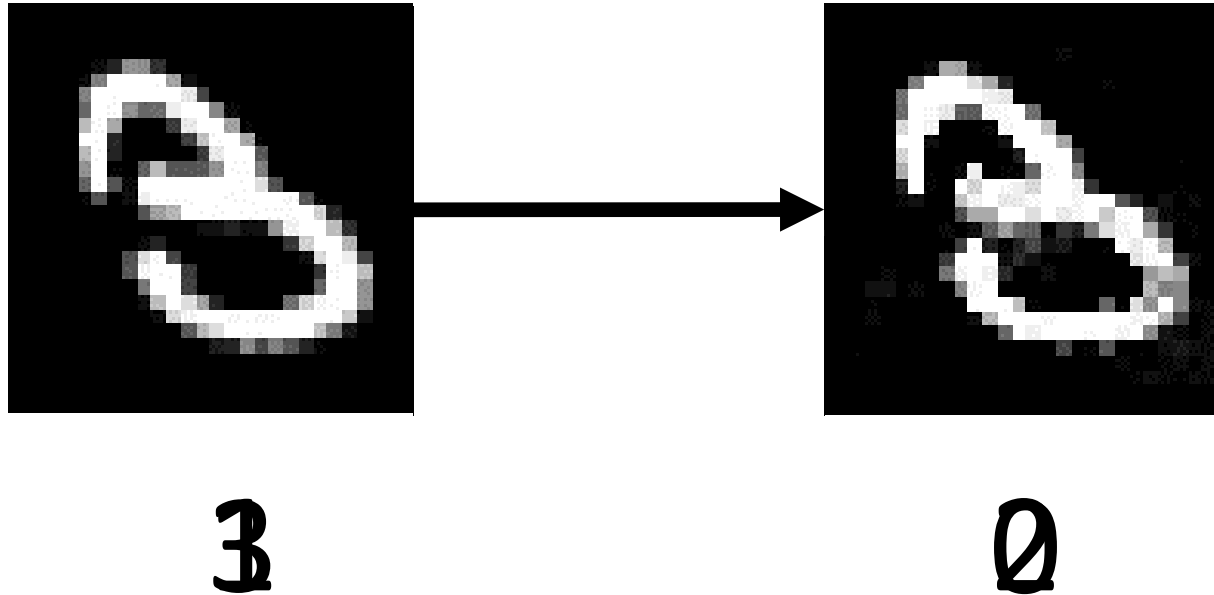
# ADVERSARIAL ROBUSTNESS



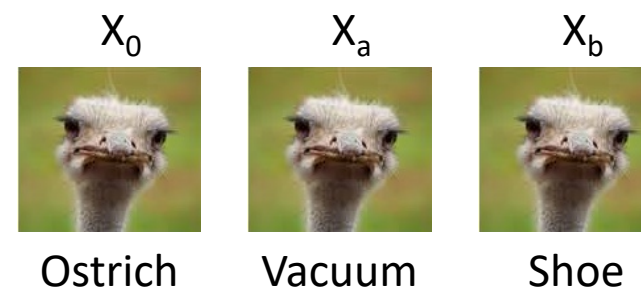
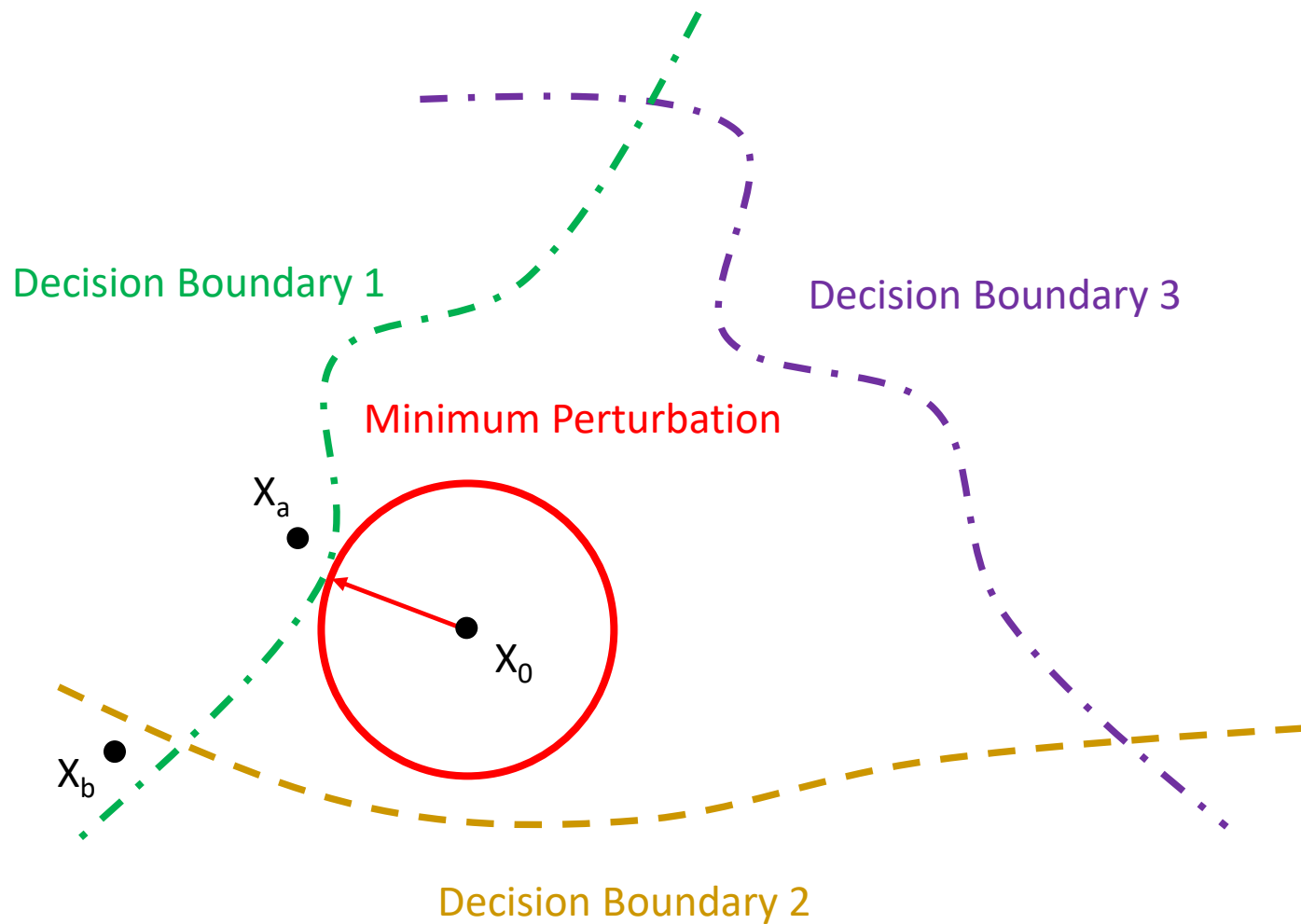
UNIVERSITY OF TORONTO  
FACULTY OF APPLIED SCIENCE & ENGINEERING

# HOW GOOD IS YOUR NEURAL NETWORK ?

- Neural networks **are not** robust to input perturbations.
- **Example:** Carlini and Wagner Attack on MNIST



# ADVERSARIAL PERTURBATIONS



# UNCERTAINTY IN DNNS



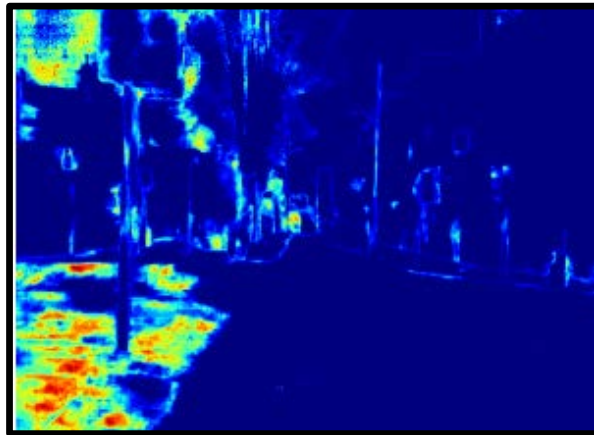
UNIVERSITY OF TORONTO  
FACULTY OF APPLIED SCIENCE & ENGINEERING

# SOURCES OF UNCERTAINTY IN DNNs

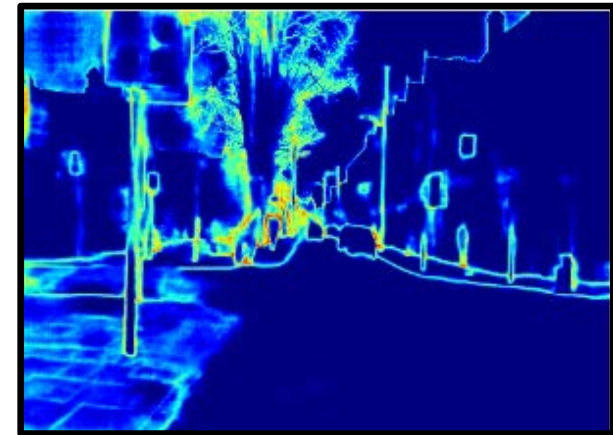
- Two sources of uncertainty exist in DNNs.
- **Epistemic (Model) Uncertainty:** Captures the ignorance about which model generated our data.
- **Aleatoric (Observation) Uncertainty:** Captures the inherent noise in the observations.



Original Image



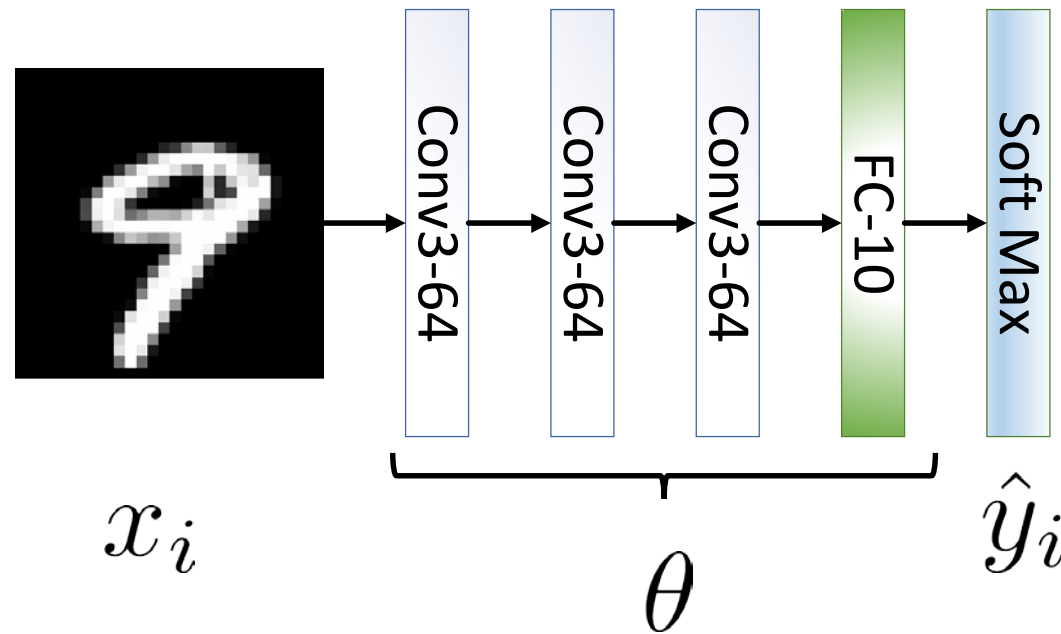
Epistemic Uncertainty



Aleatoric Uncertainty

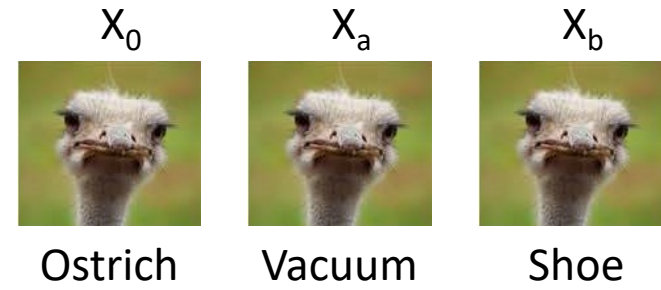
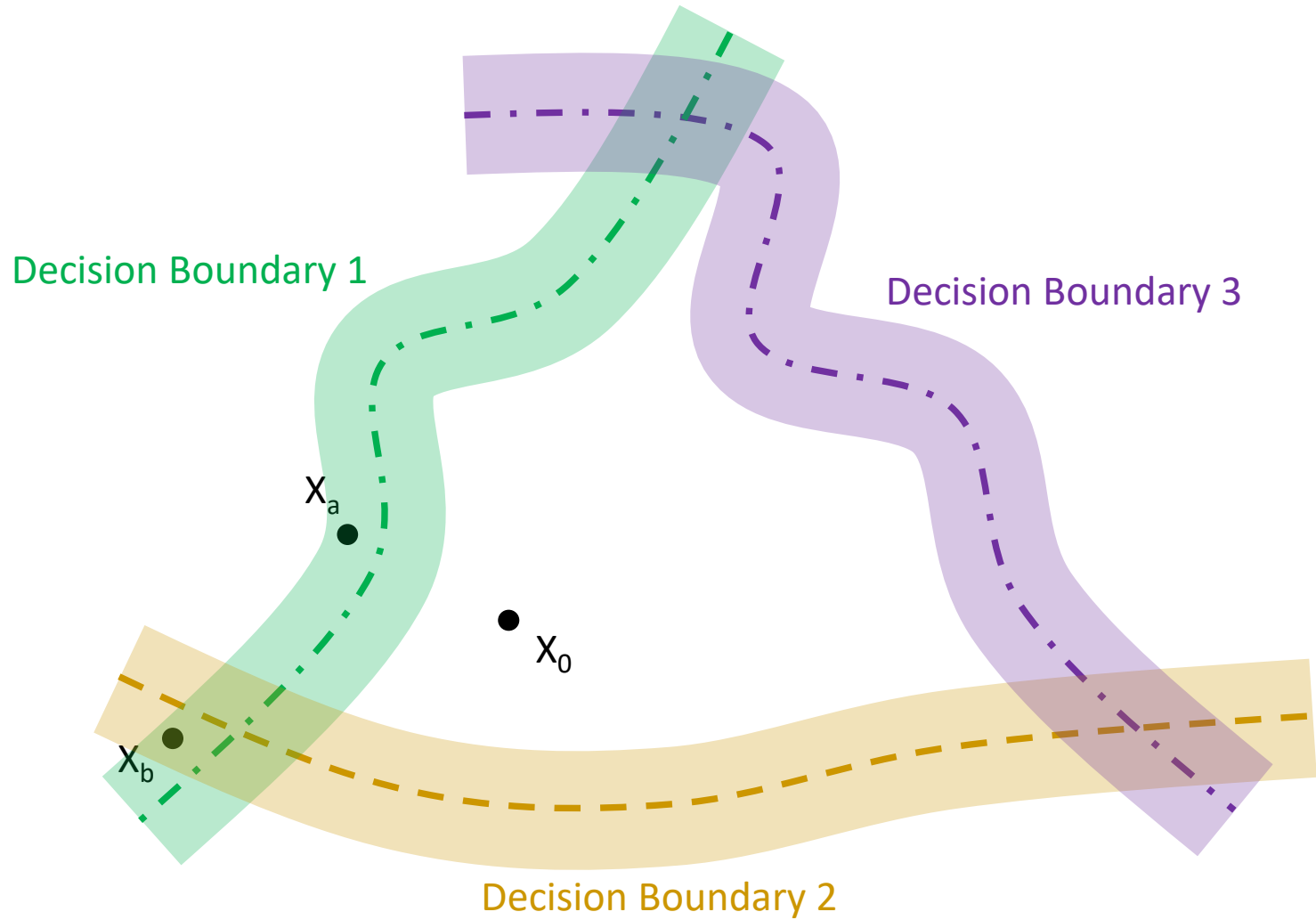
# CAPTURING EPISTEMIC UNCERTAINTY

- Marginalizing over neural network parameters:  $p(\hat{y}_i|x_i, \mathcal{D}) = \int_{\theta} p(\hat{y}_i|x_i, \mathcal{D}, \theta)p(\theta|\mathcal{D})d\theta$



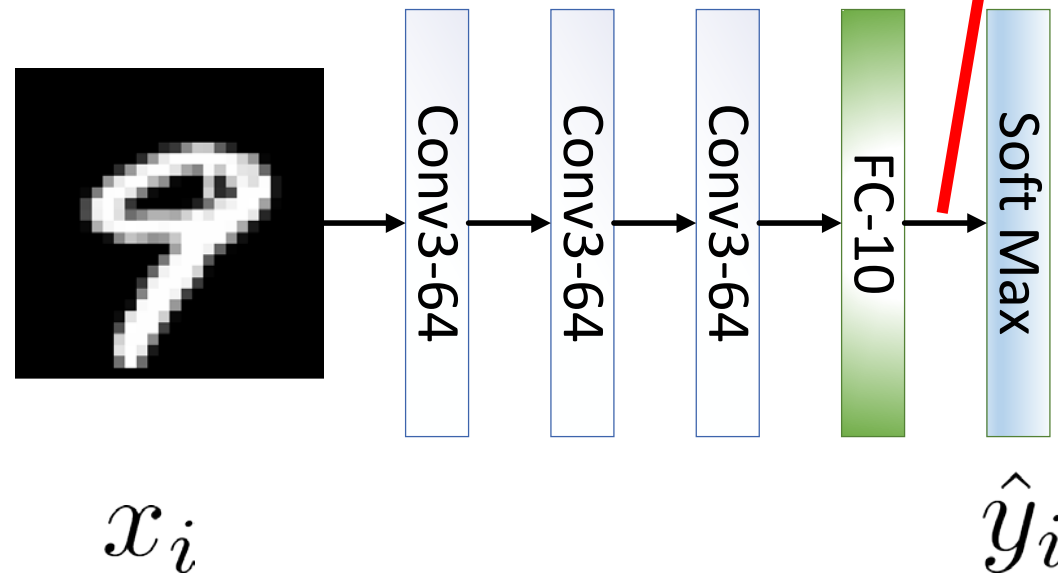


# CHANGE IN DECISION BOUNDARIES

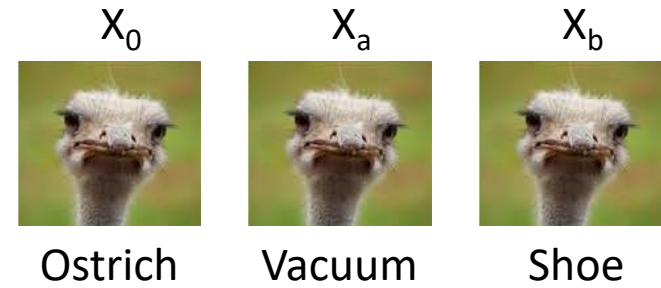
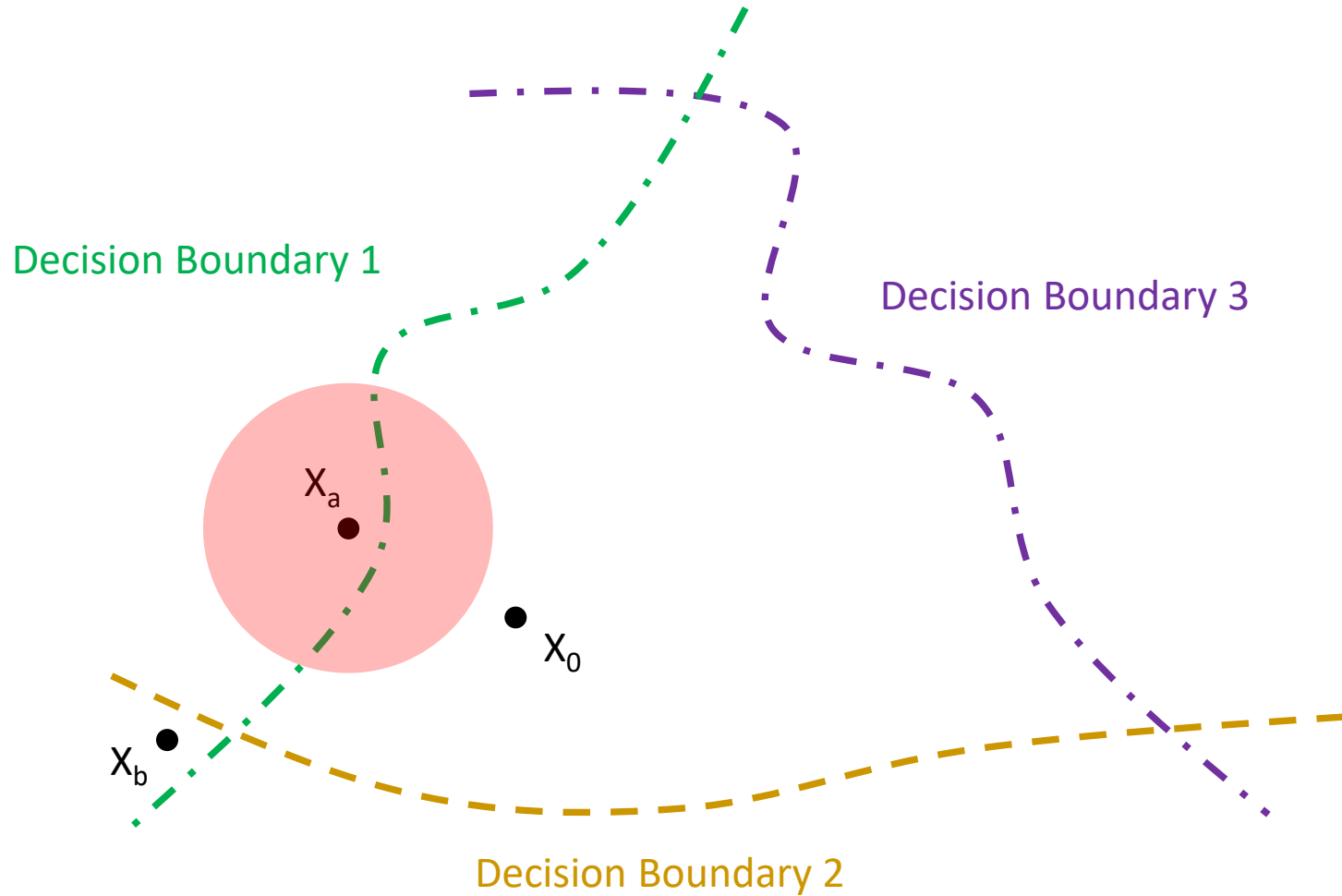


# CAPTURING ALEATORIC UNCERTAINTY

- Heteroscedastic variance estimation:  $p(\hat{y}_i | x_i, \mathcal{D}, \theta) = \mathcal{N}(\mu(x_i, \theta), \sigma(x_i, \theta))$



# CHANGE IN DATA POINT

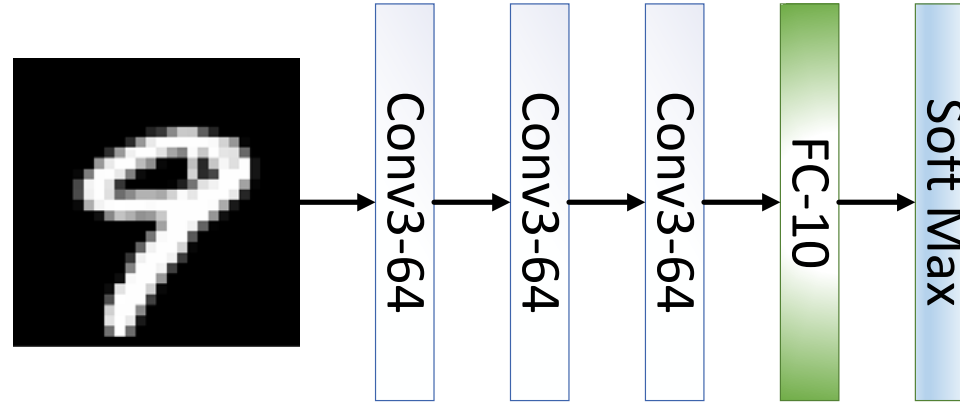


# METHODOLOGY

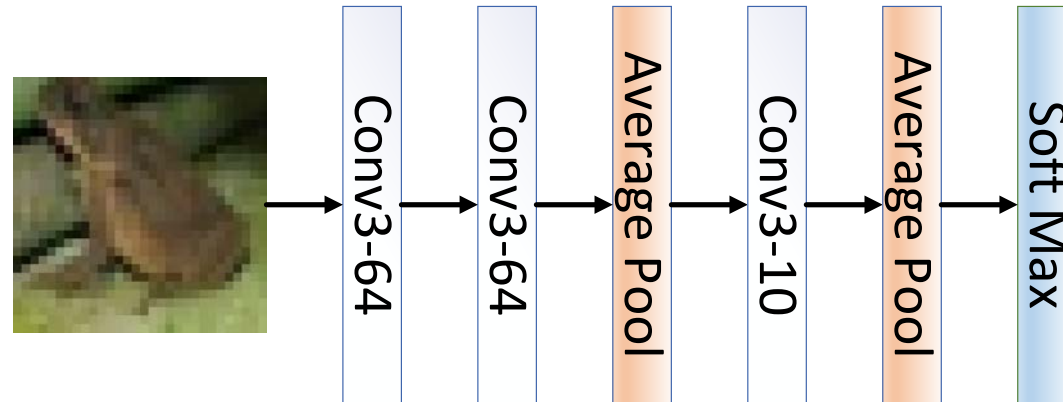


# NEURAL NETWORKS AND DATASETS

ConvNet On MNIST

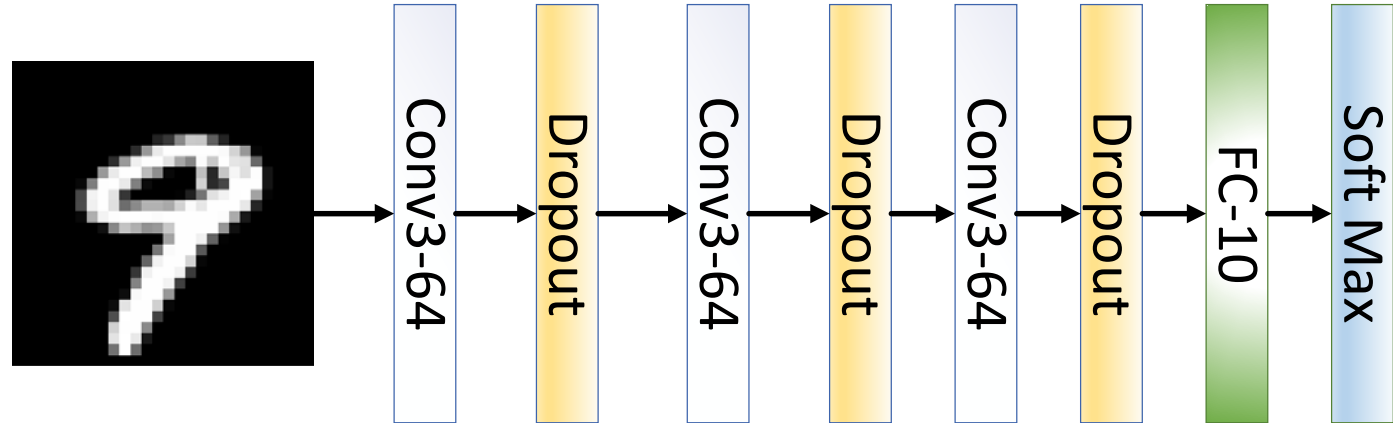


ConvNet On CIFAR10

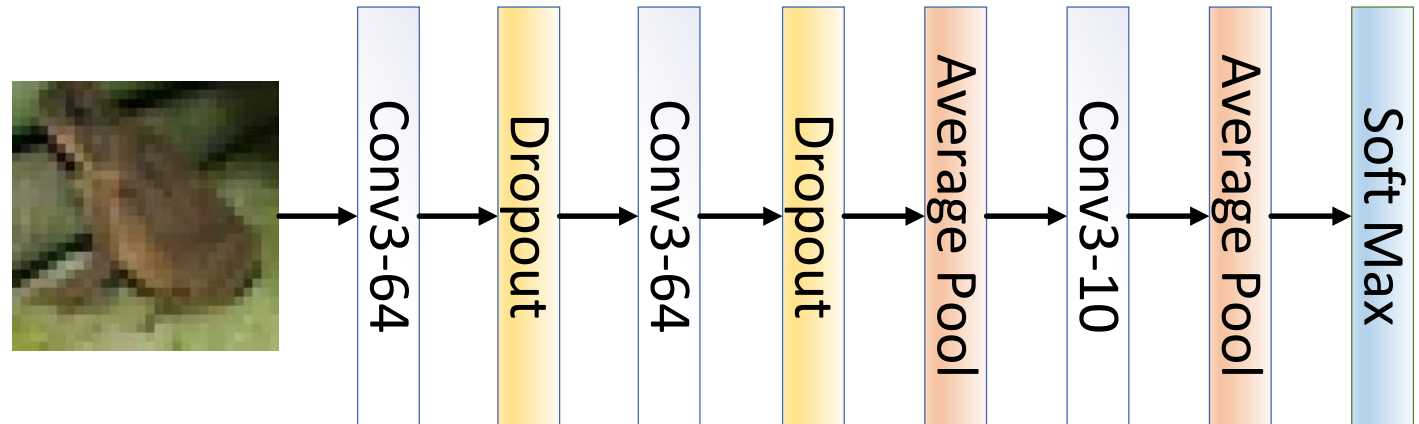


# EPISTEMIC UNCERTAINTY: AN APPROXIMATION

ConvNet On MNIST

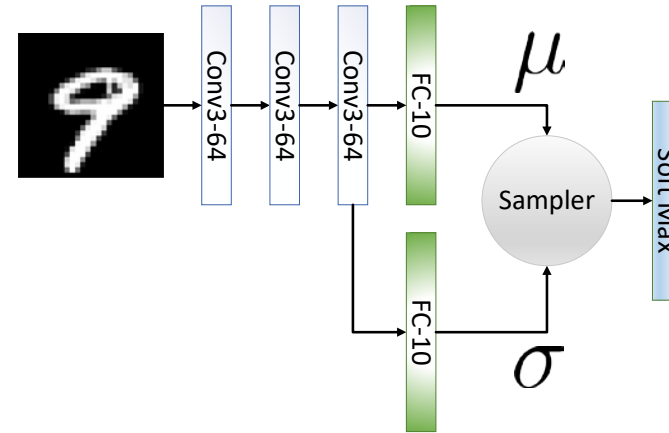


ConvNet On CIFAR10

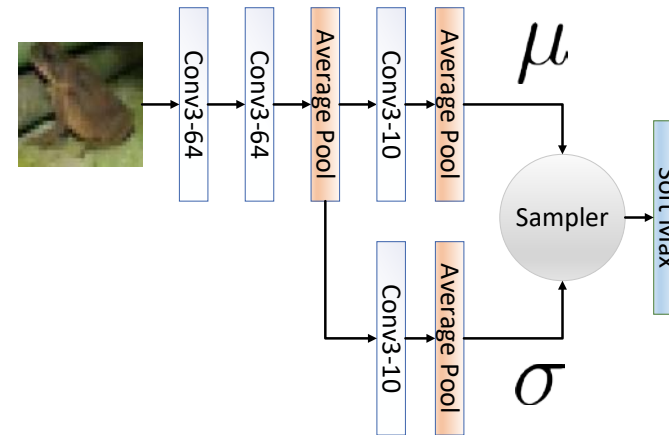


# ALEATORIC UNCERTAINTY ESTIMATION

ConvNet On MNIST



ConvNet On CIFAR10



# GENERATING ADVERSARIAL PERTURBATIONS

- Use Cleverhans: <https://github.com/tensorflow/cleverhans>
  
- Adversarial Attacks:
  1. **Fast Gradient Sign Method (FGSM)**: Goodfellow et. Al.
  2. **Jacobian- Based Saliency Map Attacks (JSMA)**: Paparnot et. Al.
  3. **Carlini and Wagner Attacks**: Carlini et. Al.
  4. **Black Box Attack**: Paparnot et. Al.



# RESULTS



# RESULTS

Dataset	Network	Attack Type	Defense Type	Accuracy (%)	Adversarial Accuracy (%)	Fooling Rate (%)
MNIST	Basic CNN	FGSM[6]	None	99.37	9.96	-
			Epistemic	98.50	22.92	-
			Aleatoric	99.35	8.75	-
		CW[1]	None	99.30	-	99-100
			Epistemic	98.37	-	30-37
			Aleatoric	99.32	-	67-80
		JSMA[12]	None	99.35	-	89-92
			Epistemic	98.62	-	22-27
			Aleatoric	99.34	-	73-81
		BB[11]	None	99.32	67.78	-
			Epistemic	98.51	63.29	-
			Aleatoric	99.20	62.08	-
CIFAR10	Fully Convolutional Network	FGSM[6]	None	77.84	9.98	-
			Epistemic	76.28	12.44	-
			Aleatoric	78.00	10.38	-

# EPISTEMIC UNCERTAINTY ESTIMATION

Dataset	Network	Attack Type	Defense Type	Accuracy (%)	Adversarial Accuracy (%)	Fooling Rate (%)
MNIST	Basic CNN	FGSM[6]	None	99.37	9.96	-
			Epistemic	98.50	22.92	-
			Aleatoric	99.35	8.75	-
		CW[1]	None	99.30	-	99-100
			Epistemic	98.37	-	30-37
			Aleatoric	99.32	-	67-80
		JSMA[12]	None	99.35	-	89-92
			Epistemic	98.62	-	22-27
			Aleatoric	99.34	-	73-81
		BB[11]	None	99.32	67.78	-
			Epistemic	98.51	63.29	-
			Aleatoric	99.20	62.08	-
CIFAR10	Fully Convolutional Network	FGSM[6]	None	77.84	9.98	-
			Epistemic	76.28	12.44	-
			Aleatoric	78.00	10.38	-

# ALEATORIC UNCERTAINTY ESTIMATION

Dataset	Network	Attack Type	Defense Type	Accuracy (%)	Adversarial Accuracy (%)	Fooling Rate (%)
MNIST	Basic CNN	FGSM[6]	None	99.37	9.96	-
			Epistemic	98.50	22.92	-
			Aleatoric	99.35	8.75	-
		CW[1]	None	99.30	-	99-100
			Epistemic	98.37	-	30-37
			Aleatoric	99.32	-	67-80
		JSMA[12]	None	99.35	-	89-92
			Epistemic	98.62	-	22-27
			Aleatoric	99.34	-	73-81
		BB[11]	None	99.32	67.78	-
			Epistemic	98.51	63.29	-
			Aleatoric	99.20	62.08	-
CIFAR10	Fully Convolutional Network	FGSM[6]	None	77.84	9.98	-
			Epistemic	76.28	12.44	-
			Aleatoric	78.00	10.38	-

# BLACK BOX ATTACK

Dataset	Network	Attack Type	Defense Type	Accuracy (%)	Adversarial Accuracy (%)	Fooling Rate (%)
MNIST	Basic CNN	FGSM[6]	None	99.37	9.96	-
			Epistemic	98.50	22.92	-
			Aleatoric	99.35	8.75	-
		CW[1]	None	99.30	-	99-100
			Epistemic	98.37	-	30-37
			Aleatoric	99.32	-	67-80
		JSMA[12]	None	99.35	-	89-92
			Epistemic	98.62	-	22-27
			Aleatoric	99.34	-	73-81
		BB[11]	None	99.32	67.78	-
			Epistemic	98.51	63.29	-
			Aleatoric	99.20	62.08	-
CIFAR10	Fully Convolutional Network	FGSM[6]	None	77.84	9.98	-
			Epistemic	76.28	12.44	-
			Aleatoric	78.00	10.38	-

# MC-DROPOUT APPROXIMATION

Dataset	Network	Attack Type	Defense Type	Accuracy (%)	Adversarial Accuracy (%)	Fooling Rate (%)
MNIST	Basic CNN	FGSM[6]	None	99.37	9.96	-
			Epistemic	98.50	22.92	-
			Aleatoric	99.35	8.75	-
		CW[1]	None	99.30	-	99-100
			Epistemic	98.37	-	30-37
			Aleatoric	99.32	-	67-80
		JSMA[12]	None	99.35	-	89-92
			Epistemic	98.62	-	22-27
			Aleatoric	99.34	-	73-81
		BB[11]	None	99.32	67.78	-
			Epistemic	98.51	63.29	-
			Aleatoric	99.20	62.08	-
CIFAR10	Fully Convolutional Network	FGSM[6]	None	77.84	9.98	-
			Epistemic	76.28	12.44	-
			Aleatoric	78.00	10.38	-

# CONCLUSION



# QUESTION

Can a neural network mitigate the effects of adversarial attacks by estimating the uncertainty in its predictions ?



# ANSWER(S)

- Adversarial perturbations cannot be distinguished as input noise through aleatoric uncertainty estimation.
- Epistemic uncertainty estimation, manifested as Bayesian Neural Networks might be robust to adversarial attacks.
- Results inconclusive, due to the lack of mathematical bounds on the approximation through ensembles and MC-Dropout.
- **Sufficient Conditions for Robustness to Adversarial Examples: a Theoretical and Empirical Study with Bayesian Neural Network.**
- <https://openreview.net/forum?id=B1eZRIC9YX>

# CONCLUSION

- There is no easy way out of using robustness certification to guarantee safety of deep neural networks.
- Even then, the mode of action of a specific type of adversarial attack needs to be taken into consideration.
- **Research Question:** How to certify against black box attacks?