

**The “obvious greedy algorithm” for the unweighted interval covering problem.**

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Input:  $\{I_1, \dots, I_n\}$  with  $I_j = [s_j, f_j)$ 
 $C := \emptyset$ ;  %  $C$  will be the indices of the cover
 $U := \{1, \dots, n\}$   %  $U$  is the set of indices of so far uncovered intervals
While  $U \neq \emptyset$ 
     $k := \operatorname{argmax}_{\ell: 1 \leq \ell \leq n} [|\{i \in U : I_i \cap I_\ell \neq \emptyset\}|]$ 
    %  $I_k$  will be the interval that intersects the most currently uncovered intervals.
    % To make this algorithm unambiguous we need to state a tie-breaking rule so
    % let  $k$  be the smallest index achieving maximum overlap with uncovered intervals.
    % Note that a covered interval can later be used in the cover  $C$ .
     $C := C \cup \{k\}$ 
     $U := U - \{i \in U : I_i \cap I_k \neq \emptyset\}$ 
EndWhile
```

The homework problem asks you to show that this algorithm does not always produce an optimal size cover.