

Sample Terminal Sessions

```
?| - makeEmpty(Q1).
```

```
Q1 = q(X1,X1)
```

```
?| - makeEmpty(Q1),
```

```
enqueue(a,Q1,Q2).
```

```
Q2 = q([a|X2], X2)
```

```
?| - makeEmpty(Q1),
```

```
enqueue(a,Q1,Q2),
```

```
enqueue(b,Q2,Q3).
```

```
Q3 = q([a,b|X3], X3)
```

```
?| - makeEmpty(Q1),
```

```
enqueue(a,Q1,Q2),
```

```
enqueue(b,Q2,Q3),
```

```
enqueue(c,Q3,Q4),
```

```
enqueue(d,Q4,Q5).
```

```
Q5 = q([a,b,c,d|X5], X5)
```

```
?| - makeEmpty(Q1),  
    enqueue(a,Q1,Q2),  
    enqueue(b,Q2,Q3),  
    enqueue(c,Q3,Q4),  
    enqueue(d,Q4,Q5),  
    dequeue(A,Q5,Q6).  
  
A = a  
Q6 = q([b,c,d|X6], X6)
```

```
?| - makeEmpty(Q1),  
    enqueue(a,Q1,Q2),  
    enqueue(b,Q2,Q3),  
    enqueue(c,Q3,Q4),  
    enqueue(d,Q4,Q5),  
    dequeue(_,Q5,Q6),  
    dequeue(A,Q6,Q7).  
  
A = b  
Q7 = q([c,d|X7], X7)
```

```
?| - makeEmpty(Q1),  
    enqueue(a,Q1,Q2),  
    enqueue(b,Q2,Q3),  
    enqueue(c,Q3,Q4),  
    enqueue(d,Q4,Q5),  
    dequeue(_,Q5,Q6),  
    dequeue(_,Q6,Q7),  
    enqueue(e,Q7,Q8).  
  
Q8 = q([c,d,e|X8], X8)
```

Efficient Queues

Make-Queue Program and Query:

```
makeEmpty(q(X,X)).
```

```
? | - makeEmpty(Q).
```

```
Q = q(X,X)
```

Enqueue Program and Query:

```
enqueue(A, q(L,X), q(L,Y)) :- X = [A|Y].
```

i.e., replace X by [A|Y] in L.

```
? | - enqueue(d, q([a,b,c|X],X), Q).
```

```
Q = q([a,b,c,d|Y], Y)
```

Efficient Queues (Cont'd)

Dequeue Program and Query:

```
dequeue(A, q(L1,Y), q(L2,Y)) :- L1 = [A|L2].  
i.e., extract A and L2 from L1.
```

```
?|- dequeue(A, q([a,b,c,d|Y],Y), Q).  
A = a  
Q = q([b,c,d|Y],Y).
```