

# CSC 2232: Topics in Computer System Performance and Reliability

Bianca Schroeder

Department of Computer Science  
University of Toronto

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## SHORT ANNOUNCEMENT

- Lecture slides from last week are posted on course web page.
- First part of reading list is posted.
  - Volunteer now! :-)
- More project suggestions will be posted soon.

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## TODAY'S AGENDA

- Complete open versus closed systems
- Queueing Terminology
- First operational laws
- Little's law

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## PAPER PRESENTATIONS

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## PAPER PRESENTATIONS

- Each of you will present one paper in class
- Format of presentation:
  - 30 min presentation of paper contents
  - 5-15 min paper review
    - Good points
    - Bad points
  - 10 min class discussion

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## PURPOSE

- Wrong answers:
  - “To give a verbal version of the paper, cramming all its content into 30 min”
  - “To impress people with your technical depth and thoroughness”
- In fact, no one really cares about these things.
  - The goal is to filter out the main points of the paper and present them well.
  - By the end, everybody in the audience should remember 2-3 take-home messages

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## The Content

- Same basic topical structure as a paper:
  - Intro to the topic and problem
  - Brief preview of how the talk will progress
  - The solution
  - Evidence that the solution is good
  - Summary of the main points

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## Detail and time control

- Your main challenges:
  - Their limited time → You have exactly 30 min
  - Their limited attention → More than a little detail will tire and bore them
- These are related: The ways to limit detail also save time

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## 2 main principles

- K.I.S.S. (keep it simple stupid).
- Repeat key insights: tell them what you're going to tell them (Forecast), tell them, and tell them what you told them (Summary).

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## How many slides?

- At the absolute most, you could have 1 slide per minute; 1 slide per 1.5 minutes is often about right
- This means you have about 20-30 slides over which to get across your message(s)

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## What's on each slide?

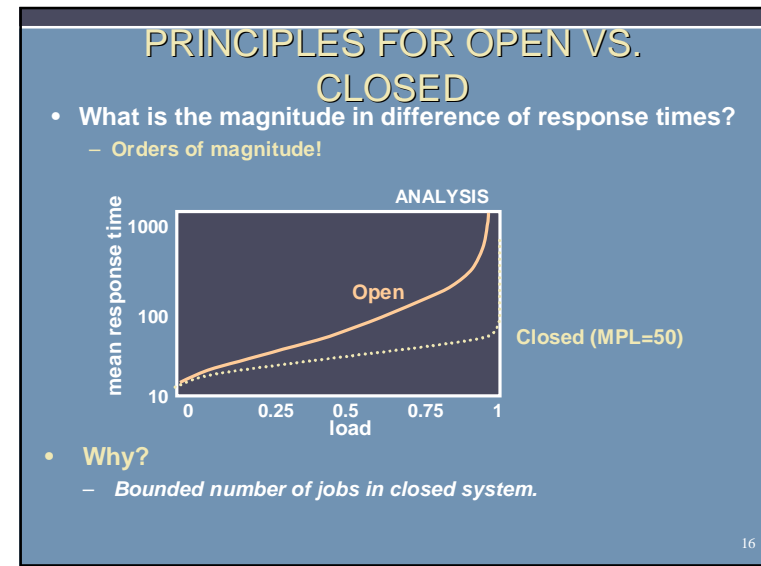
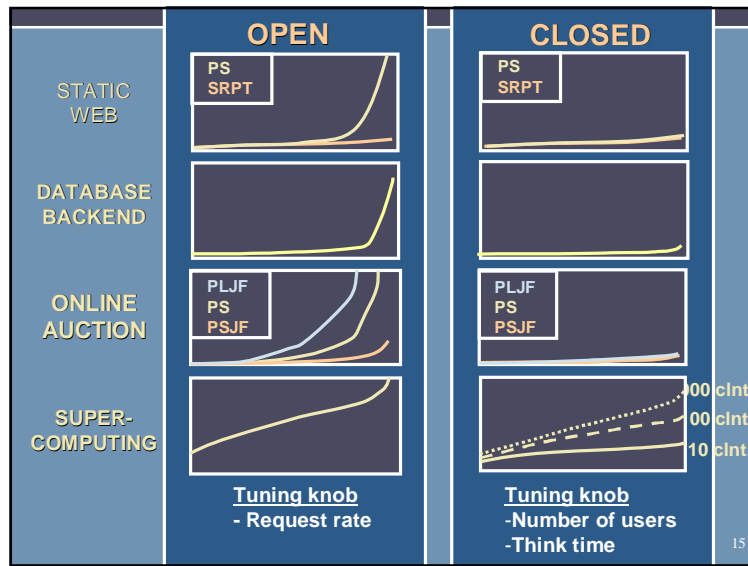
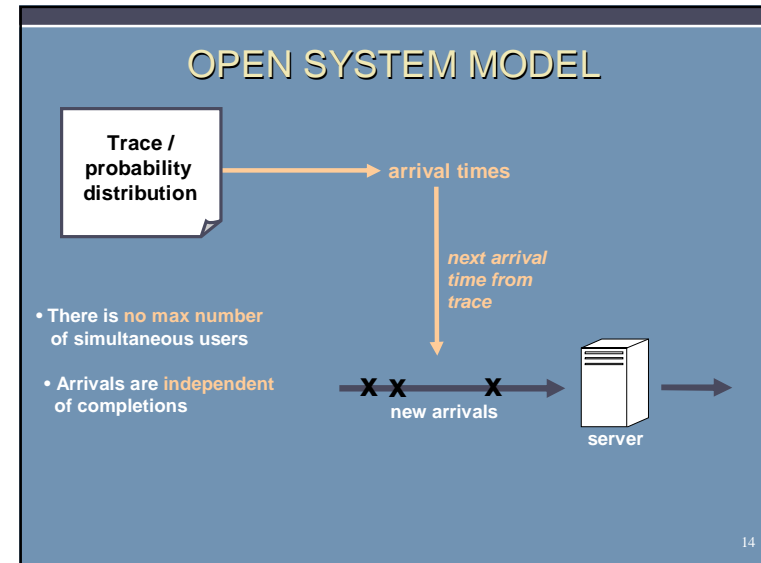
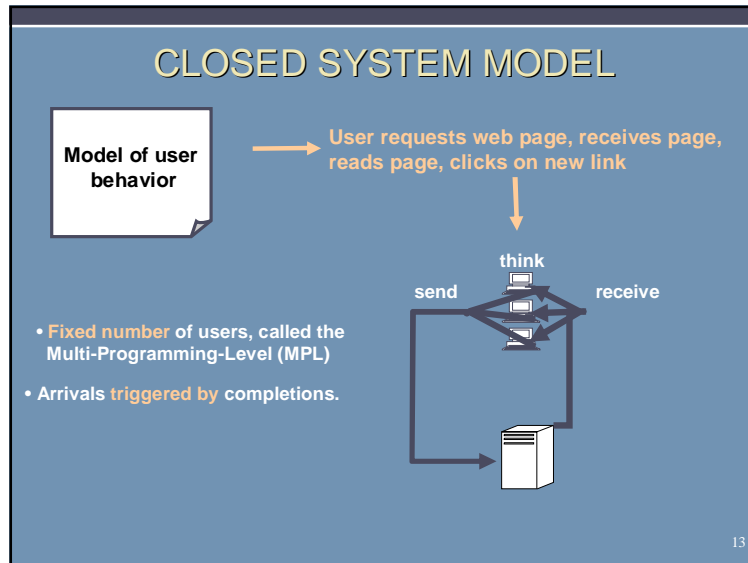
- Each slide should have one basic point
- There should NOT be tons of text
- Use sentence fragments
- Use big fonts
- Use a picture everywhere you possibly can!
  - Saves text and thus slides
  - Much more enjoyable to process

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## TODAY'S AGENDA

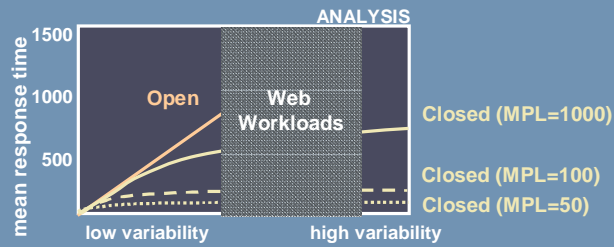
- ⇒ **Complete open versus closed systems**
  - **Queueing Terminology**
  - **First operational laws**
  - **Little's law**

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## PRINCIPLES FOR OPEN VS. CLOSED

- How does variability affect open/closed response times?
  - Huge effect on open, limited effect on closed system.

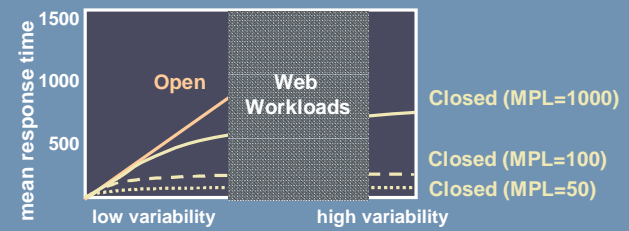


- Why?
  - Dependency between completions and arrivals in closed system reduces burstiness.

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## PRINCIPLES FOR OPEN VS. CLOSED

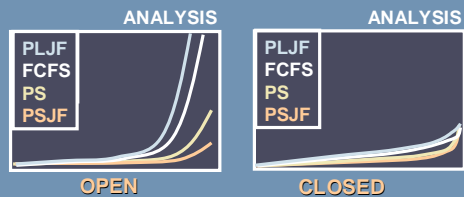
- Can we make closed look like open, by increasing MPL?



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## PRINCIPLES FOR OPEN VS. CLOSED

- What is the impact of scheduling?
  - Huge in open system, almost none in closed system.



- Why?
  - Scheduling takes advantage of variability in the system.
  - Closed systems reduce the effect of variability.

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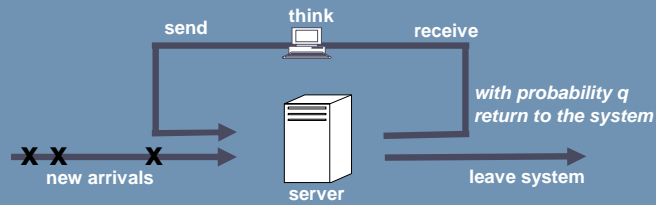
## HOW DO YOU CHOOSE THE RIGHT MODEL?

1. Is there a more realistic model?
1. What's most representative of real systems?



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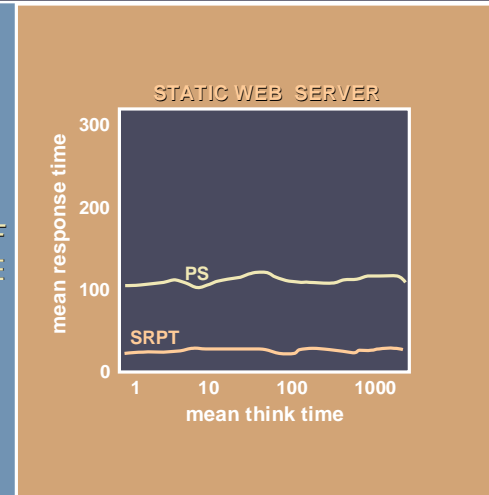
## THE PARTLY-OPEN MODEL



What parameters affect the load?  
 Does think time affect the load?  
 How do think times affect response times?

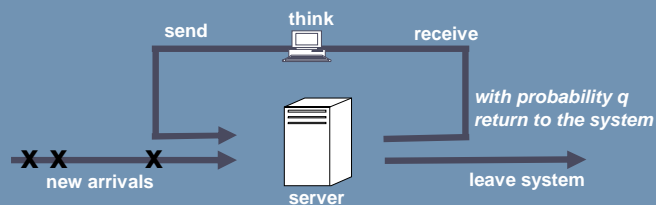
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## THE EFFECT OF THINK TIME



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## THE PARTLY-OPEN MODEL

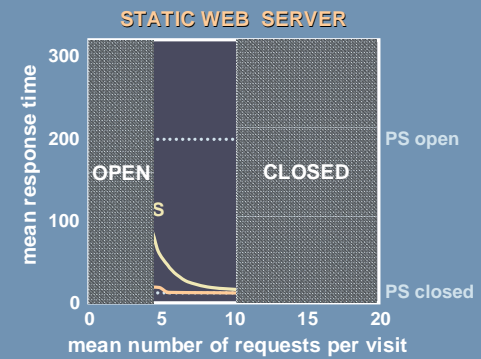


How does this model compare to Open/Closed?



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## THE TRANSITION FROM OPEN → CLOSED



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## CHOOSING A SYSTEM MODEL

Real web workloads #req. / visit

- A site being "Slashdotted" (1.2)
- Financial service provider (1.4)
- CMU web server (1.8)
- Kasparov vs Deep Blue (2.4)
- Large corporate web site (2.4)
- Science Institute USGS (3.6)
- Online dept. store (5.4)
- Supercomp. site (6.0)
- World cup site (11.6)
- Online gaming site (12.9)



Open or Closed?

Use partly-open system to decide

PARTLY-OPEN

CLOSED

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## Motivating examples: conclusion

- Intuition is not always good enough
  - Need back-of-the envelope calculations and analytical tools to answer questions.
- Workload / fault load matters hugely
  - Important to understand what the real world looks like!

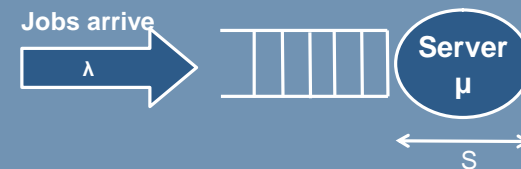
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## TODAY'S AGENDA

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## THE SINGLE SERVER NETWORK



- Service Order: FCFS (First-Come-First-Serve)
- Average arrival rate:  $\lambda = 1 \text{ job} / 6 \text{ sec}$
- Mean interarrival time:  $1/\lambda = 6 \text{ sec}$
- Service Requirement  $S = 5 \text{ sec}$
- Mean service time:  $E[S] = 3 \text{ sec}$
- Average service rate:  $\mu = 1/E[S] = 1 \text{ job} / 3 \text{ sec}$

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## HOW IS THIS DIFFERENT FROM NORMAL CONVERSATIONS?

- Normal conversation:
  - The average arrival rate is 3 jobs / second
  - The CPU can provide 20,000 cycles per second
  - Jobs need on average 5,000 cycles to complete
- Translation into queueing lingo :
  - $\lambda = 3$  jobs / second
  - $E[S] = 0.25$  seconds
  - $\mu = 4$  jobs / second ( $= 1/E[S]$ )

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## PERFORMANCE METRICS

- Response time:  $T_S$ 
  - Turnaround time, flow time, time in system
  - Main interest:  $E[T]$ , also  $\text{Var}[T]$
- Waiting time:  $T_Q$ 
  - Time in queue
- Number of jobs in system:  $N_S$
- Number of jobs in queue:  $N_Q$

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## SOME OBSERVATIONS

- As  $\lambda$  increases:
  - All metrics increase
- As  $\mu$  increases:
  - All metrics decrease
- Basic requirement:  $\lambda \leq \mu$ 
  - What happens if  $\lambda > \mu$ ? (Hint: what is  $E[N_s \text{ at time } T]$ )

Metrics:  
T\_S  
N\_S  
T\_Q  
N\_Q

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## MORE OBSERVATIONS

- Suppose  $\lambda \leq \mu$  and interarrival distribution and service time distribution are constant:
  - What is  $T_Q$  ?
  - What is  $T_S$  ?
- So queueing comes from variability
  - So how does variability lead to queues?
  - E.g. assume  $\lambda = 1$  job/sec and  $\mu = 2$  jobs /sec

Metrics:  
T\_S  
N\_S  
T\_Q  
N\_Q

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## CLASSIFICATION OF QUEUEING NETWORKS

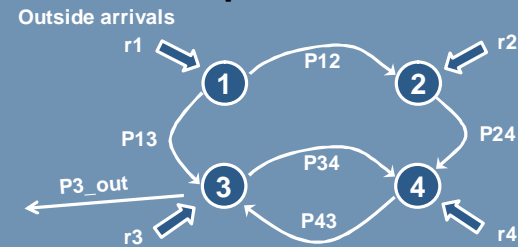
- OPEN versus CLOSED
- Let's start with OPEN:
  - Has external arrivals and departures

### EXAMPLE 1: The single server system



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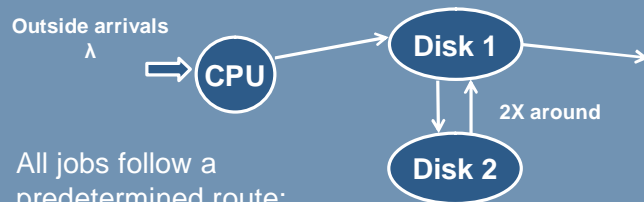
### EXAMPLE 2: Network-of-queues with probabilistic routing



- Server  $i$  receives
  - external arrivals at rate  $r_i$
  - and also internal arrivals from other servers
- Jobs finishing at server  $i$ , go to server  $j$  with prob.  $P_{ij}$

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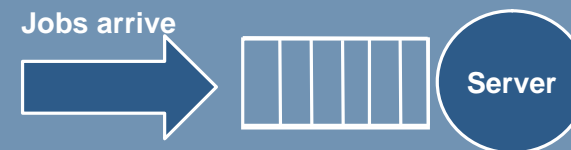
### EXAMPLE 3: Network-of-queues with non-probabilistic routing



- All jobs follow a predetermined route:
  - CPU
  - Disk 1
  - Disk 2
  - Disk 1
  - Disk 2
  - Disk 1

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### EXAMPLE 4: Finite buffer



- Space in queue is limited to  $n$  jobs
- Arrivals that find no room are dropped

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## TWO MORE PERFORMANCE METRICS

Metrics:  
T\_S  
N\_S  
T\_Q  
N\_Q

- Throughput X
- Utilization U



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## TWO MORE PERFORMANCE METRICS

Metrics:  
T\_S  
N\_S  
T\_Q  
N\_Q

- Definitions:
- $U_i$ : Fraction of time device i is busy
- $X_i$ : The rate of completions at device i (in jobs/ sec)
- How does  $X_i$  relate to  $U_i$ ?

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## HOW DOES $X_i$ RELATE TO $U_i$

- Suppose we observe the system for T time units and see that
  - Device i is busy for B time units
  - C jobs are completed
  - $U_i = B/T$       $X_i = C/T$
  - $\Rightarrow X_i = C/(B/U_i) = C/B * U_i$
  - What is C/B?
    - $B/C = E[S] \Rightarrow C/B = 1/E[S] = \mu$

$$X_i = \mu * U_i$$

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## HOW DOES $X_i$ RELATE TO $U_i$

- $X_i$  = Mean rate of completion
- = E{Rate of comp} + E{Rate of comp}
- $P\{\text{server busy}\}$
- +  $P\{\text{server is idle}\}$
- =  $\mu * U_i$

How does this change with changes in

- Job size distribution
- Interarrival time distribution
- Service order

$$X_i = \mu * U_i$$

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## THE UTILIZATION LAW

$$X_i = \mu * U_i$$

or equivalently

$$U_i = X_i * E[S]$$

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## WHAT IS THROUGHPUT?

$$X_i = \mu * U_i$$



- What is U?
  - Fraction of time server is busy
  - = mean service time / mean time betw. Arrivals
  - =  $(1/\mu)/(1/\lambda) = \lambda/\mu$

Throughput does not depend on service rate!

$$X_i = \lambda$$

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## BACK TO OUR OLD EXAMPLE

$$X_i = \mu * U_i = \lambda$$

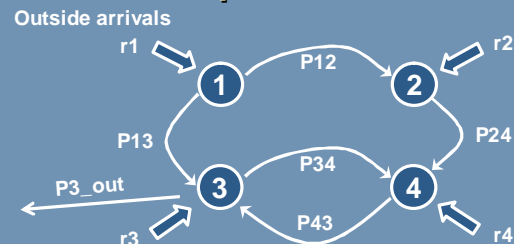
Metrics:

T  
S  
N  
S  
T  
Q  
N  
Q  
X  
U



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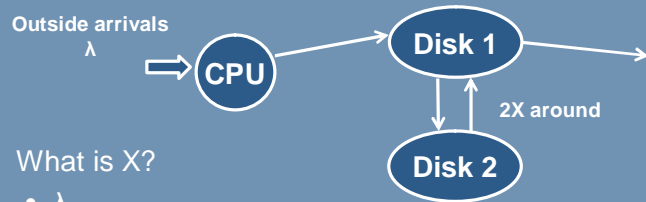
## EXAMPLE 2: Network-of-queues with probabilistic routing



- What is X?
  - $\sum r_i$
- What is  $X_i$ ?
  - $X_i = \lambda_i = r_i + \sum \lambda_j * P_{ji}$

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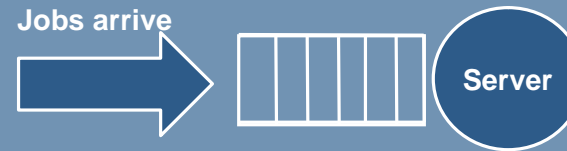
### EXAMPLE 3: Network-of-queues with non-probabilistic routing



- What is  $X$ ?
  - $\lambda$
- What is  $X_{\text{disk1}}$ 
  - $3\lambda$
- What is  $X_{\text{disk2}}$ 
  - $2\lambda$

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### EXAMPLE 4: Finite buffer

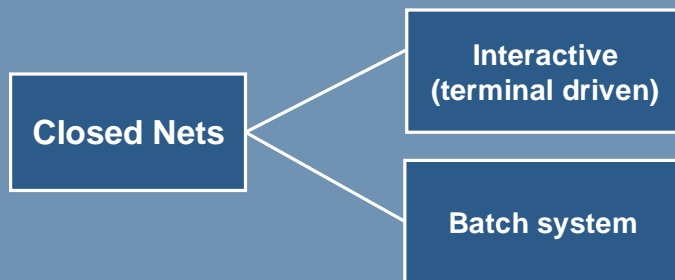


- Space in queue is limited to  $n$  jobs
- What is  $X$ ?
  - $X = U * \mu$
- But  $U$  is no longer  $\lambda/\mu$
- Need Markov chains ...

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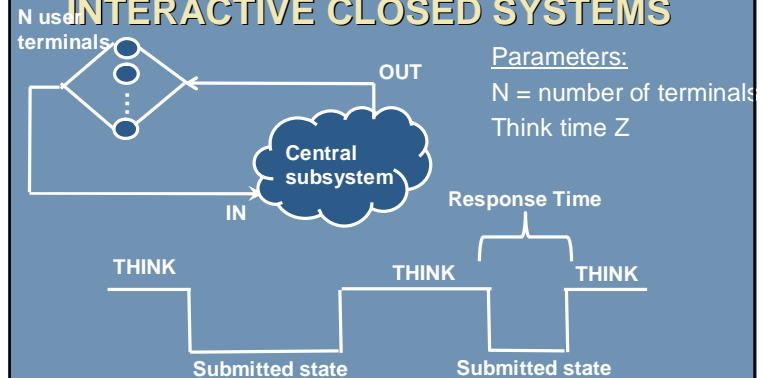
### CLOSED SYSTEMS

- Closed networks have no external arrivals or departures



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### INTERACTIVE CLOSED SYSTEMS



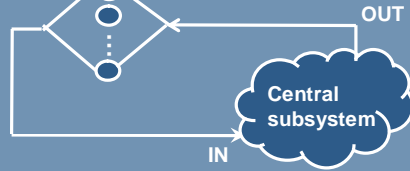
Parameters:  
 $N$  = number of terminals  
 Think time  $Z$

- How is response time defined?
  - Time it takes a job to go from IN to OUT

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## CLOSED INTERACTIVE SYSTEMS

N user terminals



Parameters:

N = number of terminals

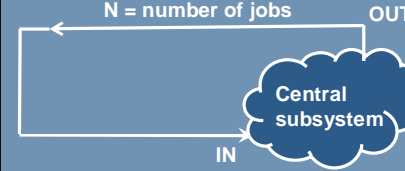
Think time Z

- Examples?
- Typical goals:
  - How high can we make N while keeping response times reasonably low?
  - Given a fixed N, what changes to central subsystem will improve response time the most?

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## CLOSED BATCH SYSTEMS

N = number of jobs



Parameters:

N = number of jobs

- As soon as one job completes, another one is started
- So there's always exactly N jobs in central subsystem
- Typical Goal?
  - Throughput!
- How is throughput defined?

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