

Assessing Human Error Against a Benchmark of Perfection

Ashton Anderson
University of Toronto

Joint work with Jon Kleinberg and Sendhil Mullainathan

Humans and Machines



One leading narrative for AI: **humans versus machines**

For any given domain, when will algorithms exceed expert-level human performance?

Humans and Machines

A set of questions around human/AI interaction:

- Relative performance of humans and algorithms
- Algorithms as lenses on human decision-making
- Humans and algorithms working together: pathways for introducing algorithms into complex human systems

Can we use algorithms to characterise and predict human error?

Chess for Decision-Making

Long-standing **model system** for decision-making

- “The drosophila of artificial intelligence.”
—John McCarthy, 1960
- “The drosophila of psychology.”
—Herb Simon and William Chase, 1973



Chess provides data on a sequence of cognitively difficult tasks.
When a human player chooses a move, we have data on:

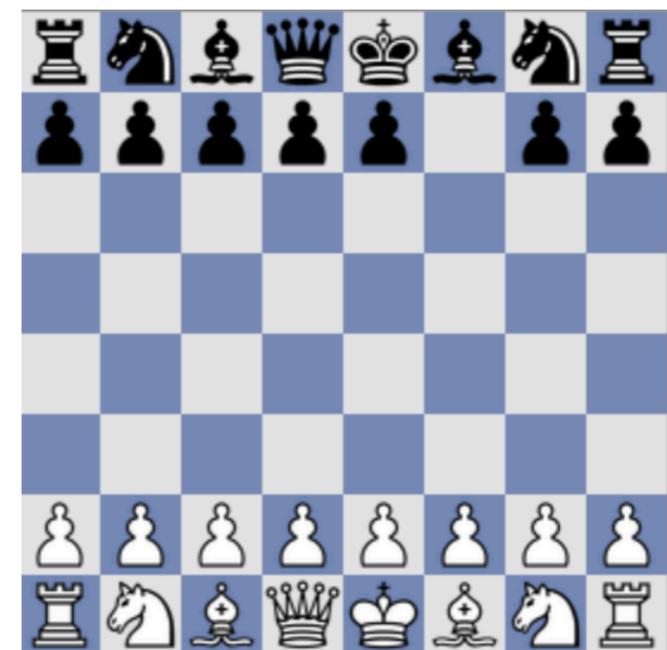
- The task instance: the chess position itself.
- The skill of the decision-maker: a chess player’s Elo rating.
- The time available to make the decision.

Can we use computation to analyze human performance?

- Characterize human “blunders” (mistakes in choice of move)
- Chess as the drosophila of machine superintelligence?

A History of Chess Engines

- 1988: First recorded win by computer against human grandmaster under standard tournament conditions.
- 1997: Deep Blue defeats world champion Kasparov in 6-game match.
- 2002–2003: Draws against world champions using desktop computers.
- 2005: Last recorded win by a human player against a full-strength desktop computer engine under standard tournament conditions.
- 2007: Computers defeat several top players with “pawn odds.”



Chess for Decision-Making

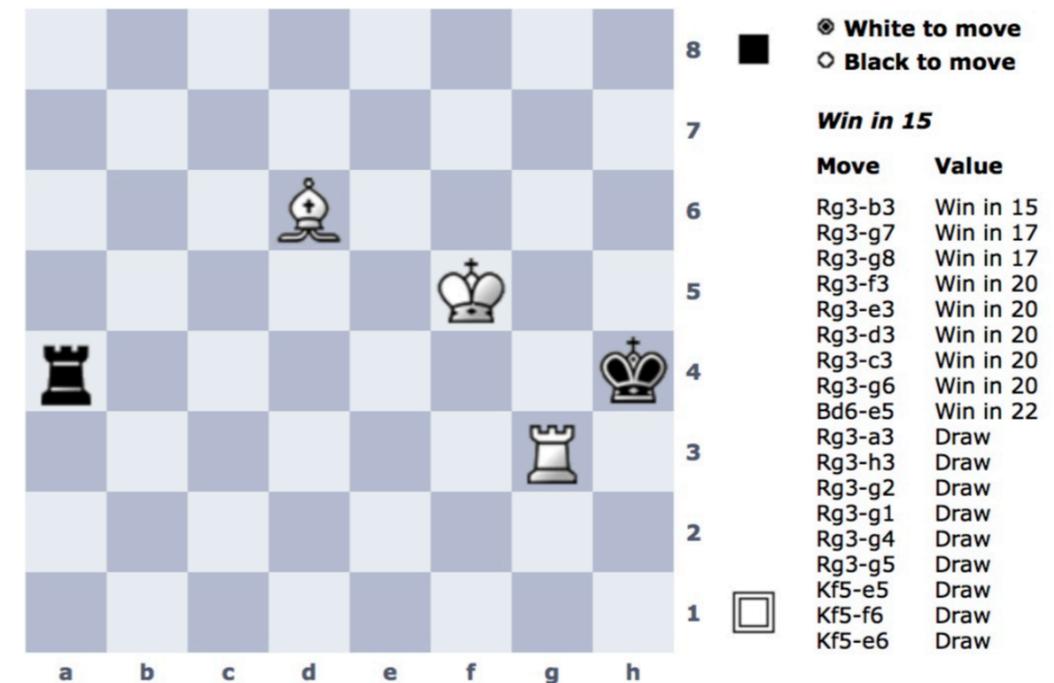


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Analysis 1
Lines: 3 [up] [down] [star] Stock [up] [down] Stop
-1.41 [+] [*] 2... Rc4 3. Rb6+ Kf5 4. Rxa6 d4 5. Ra5+
Kf6 6. Bf2 Rc1+ 7. Ke2 d3+ 8. Kxd3 Nxf2+ 9. Ke3 Nh1
10. h4 gxh4 11. Rxh5 Rc4 12. a5 Ng3 13. Rh8 Nf5+
14. Kf3 Ra4 15. Ra8 Nd4+ 16. Kg4 Nc6+ 17. Kh3
Nxa5 (depth 20, 0:00:09)
-1.07 [+] [*] 2... Rc2 3. g4 hxg4 4. hxg4 Rc4 5. Rb6+
Kf7 6. Rb7+ Ke6 7. Rb6+ Ke5 8. Rxa6 d4 9. Ra5+ Kf6
10. Bg1 Rc1+ 11. Kg2 d3 12. Bd4+ Kg6 13. Be3 d2 14.
Ra6+ Kf7 15. Ra7+ Ke6 16. Ra6+ Ke5 17. Ra5+ Kf6
18. Ra6+ Ke7 19. Ra7+ Kd6 20. Bxd2 Nxd2 21. Rg7
(depth 19, 0:00:09)
-0.94 [+] [*] 2... g4 3. hxg4 hxg4 4. Rd7 Nf6 5. Re7
Rc4 6. a5 Kf5 7. Rf7 d4 8. Bd2 Ke6 9. Ra7 Ne4 10.
Rxa6+ Kf5 11. Be1 Rc1 12. Ra8 d3 13. Rf8+ Kg5 14.
Rg8+ Kf4 15. a6 (depth 19, 0:00:09)
[+] 2... Rc4 (suggested move)
```

Could use chess engines to evaluate moves [Biswas-Regan 2015]

- Promising, since engines are vastly superior to the world's best players
- Engines sometimes detect clear-cut errors, but very often a “grey area”: engines and humans disagree, but doesn't necessarily change the outcome of the game

Chess for Decision-Making



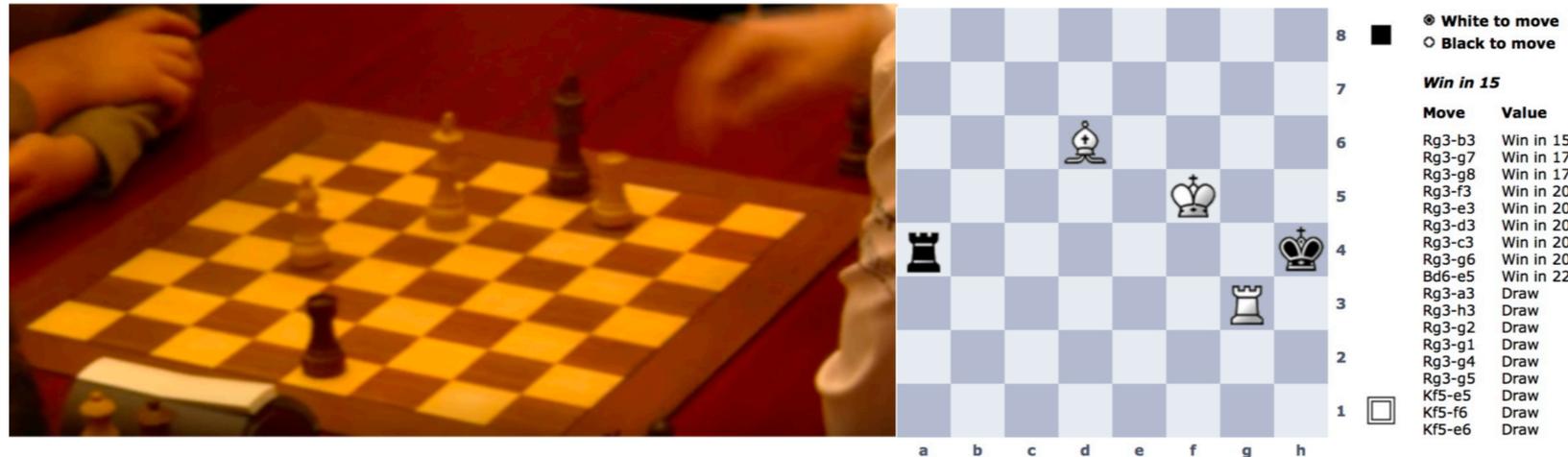
We use the fact that chess has been **solved** for positions with at most 7 pieces on the board.

- “Tablebases” record all possible positions with ≤ 7 pieces
- Can determine (game-theoretic) blunders by table look-up
- These positions are still difficult for even the world’s best players

The Stiller moves are awesome, almost scary, because you know they are the truth, God’s Algorithm; it’s like being revealed the Meaning of Life, but you don’t understand one word.

— Tim Krabbé, commenting on an early tablebase by Lewis Stiller

Chess for Decision-Making



Data from two sources:

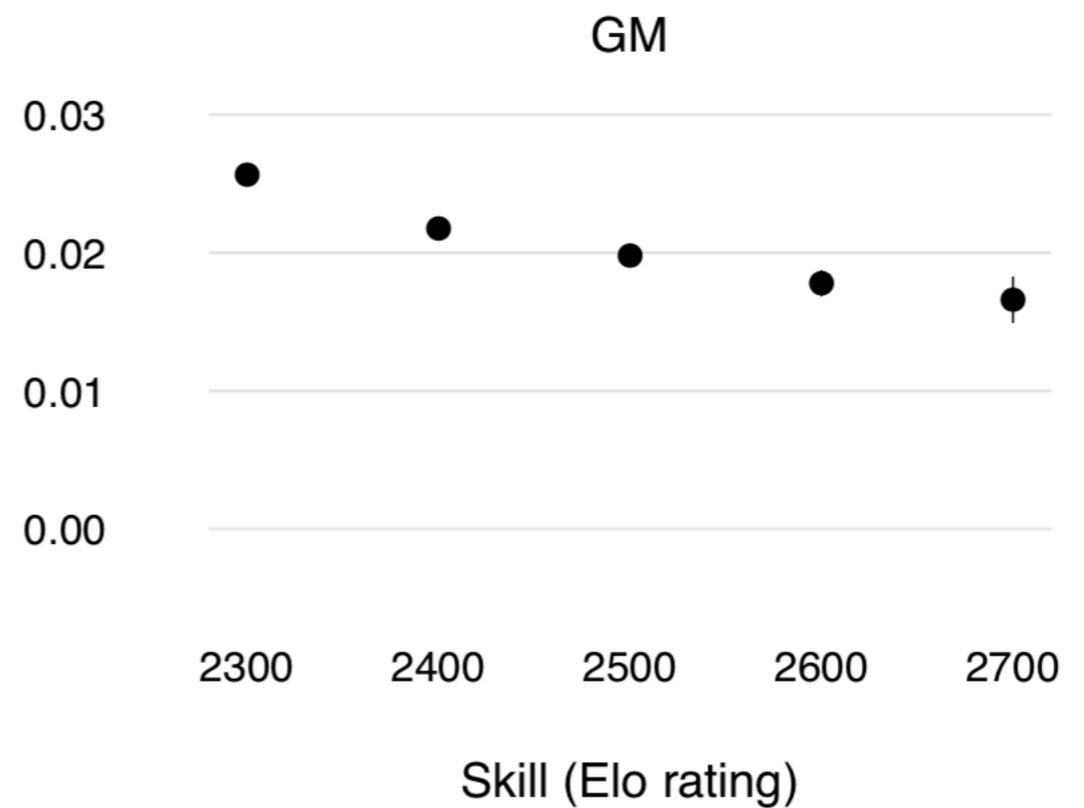
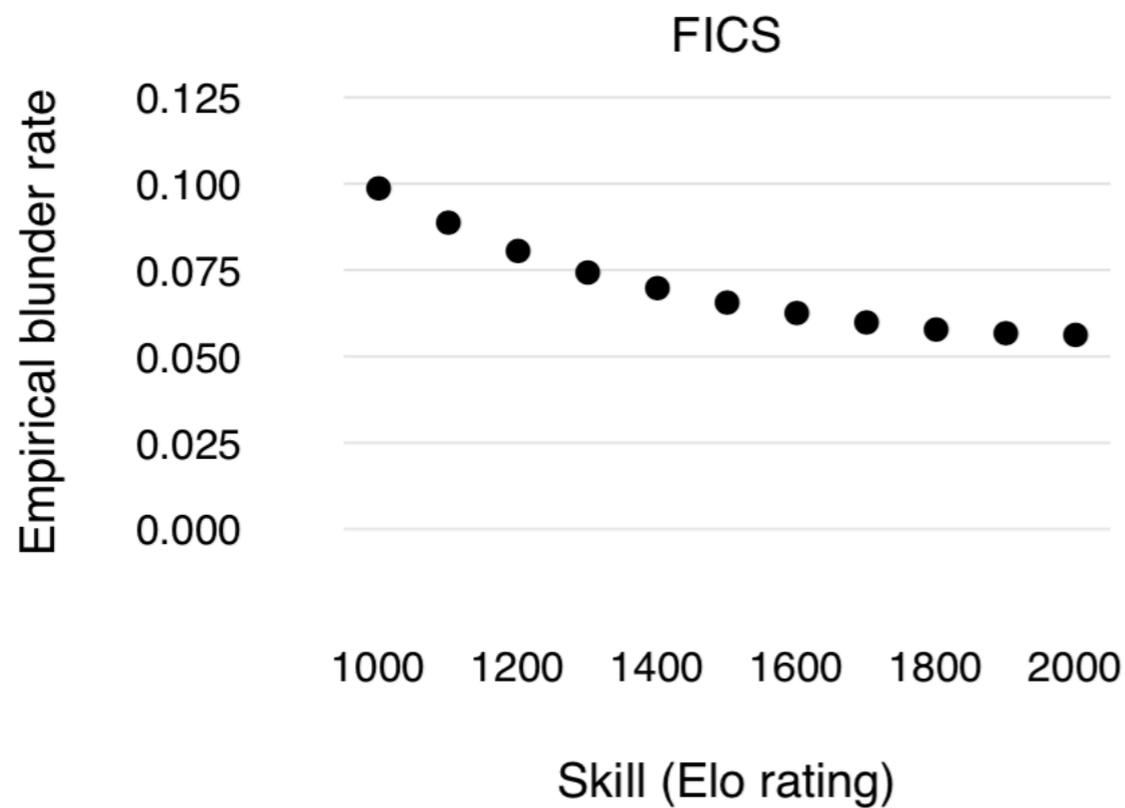
	# Games	Rating	Duration	Setting
FICS	200M	1200–1800	Minutes	Casual enthusiasts playing online
GM	1M	2400–2800	Hours	Professional tournaments

Take all <7-piece positions, classify a move as a blunder if and only if it changes the win/loss/draw outcome

Basic Dependence on Fundamental Dimensions

How does decision quality vary with  skill
time ?
difficulty

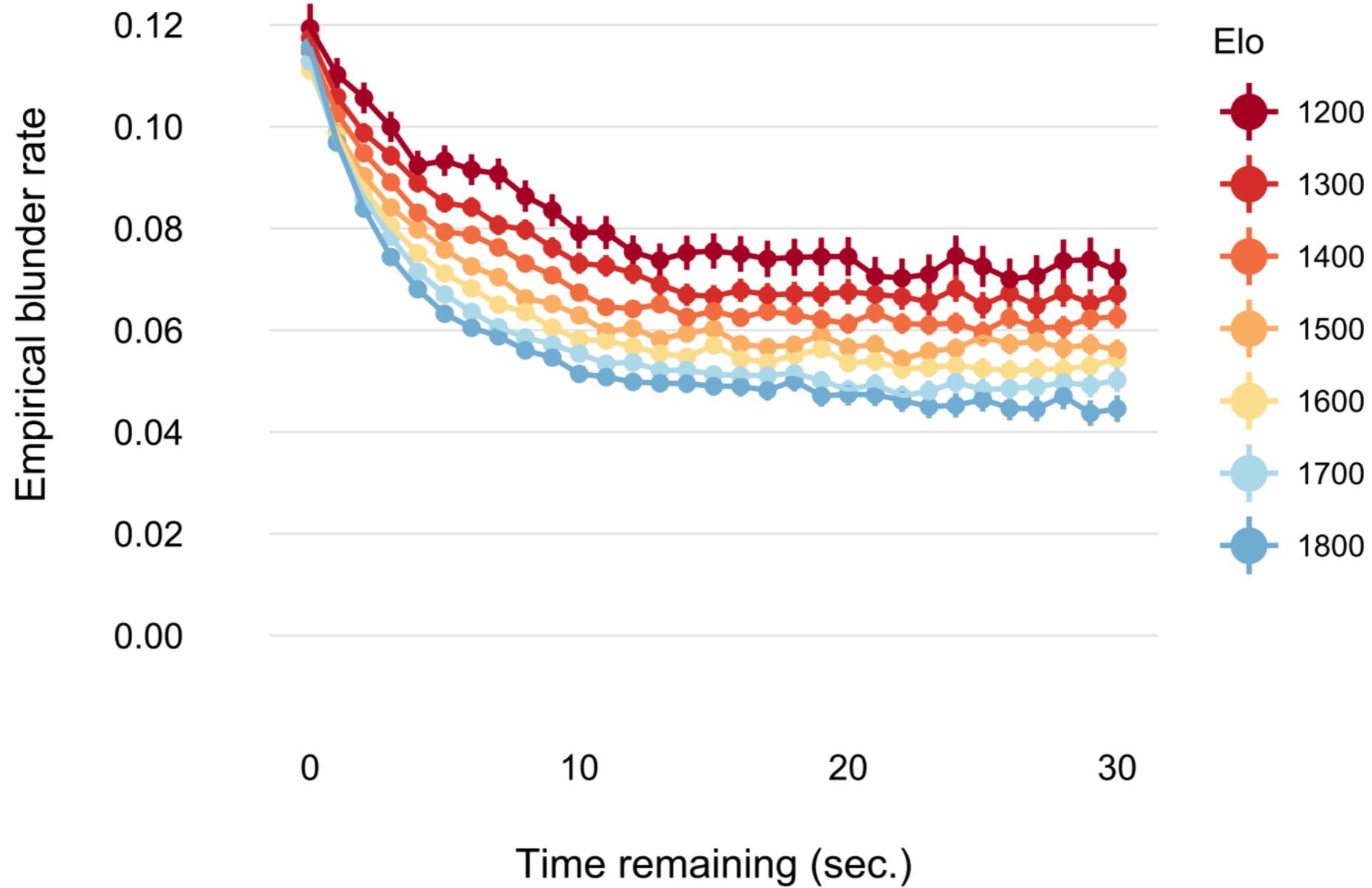
Human Error as a Function of Skill



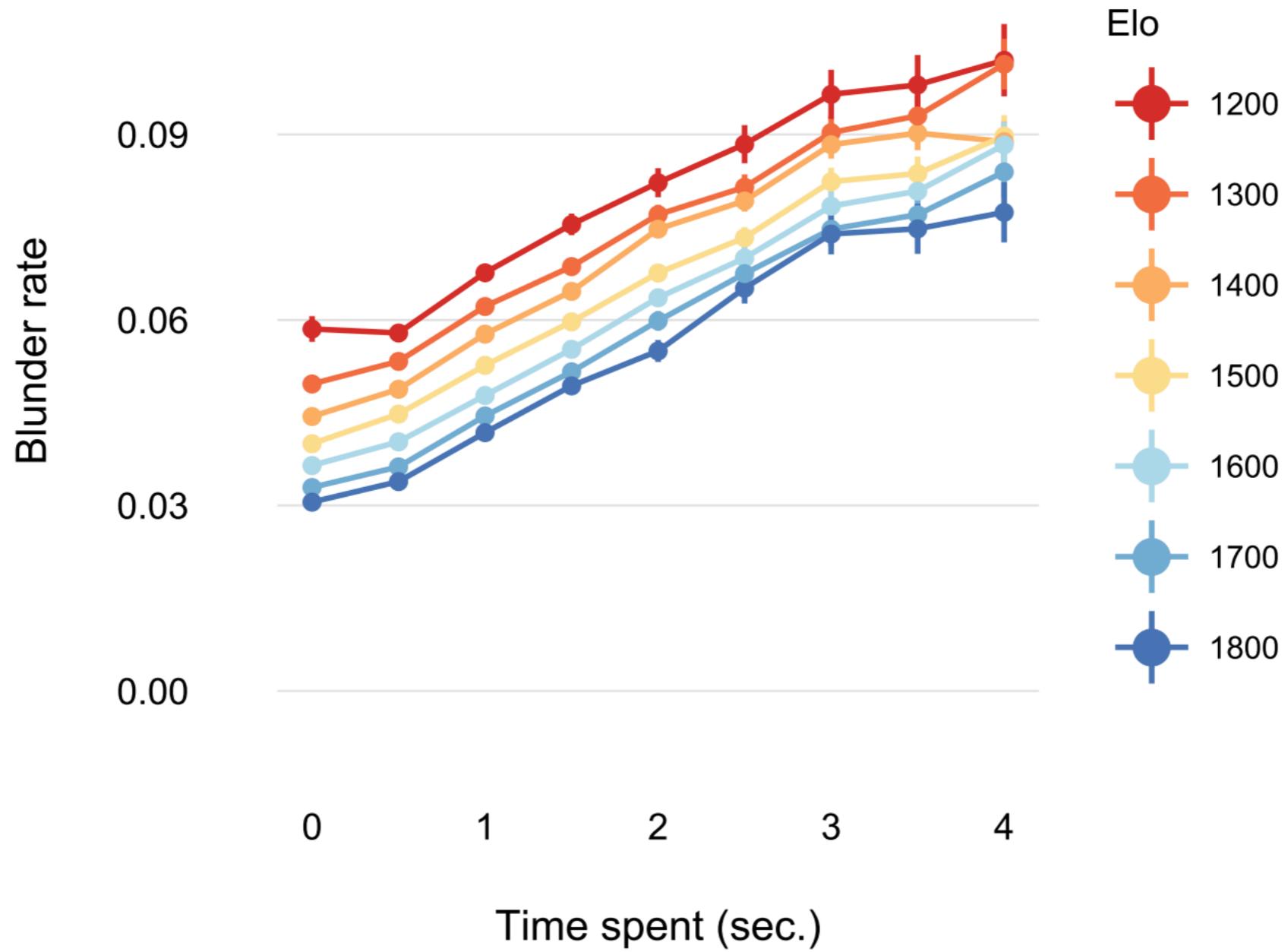
- 1000: Winner of a local scholastic contest
- 1600: Competent amateur
- 2000: Top 1% of players

- 2300: Lowest international title
- 2500: Grandmaster
- 2850: Current world champion

Human Error as a Function of Time



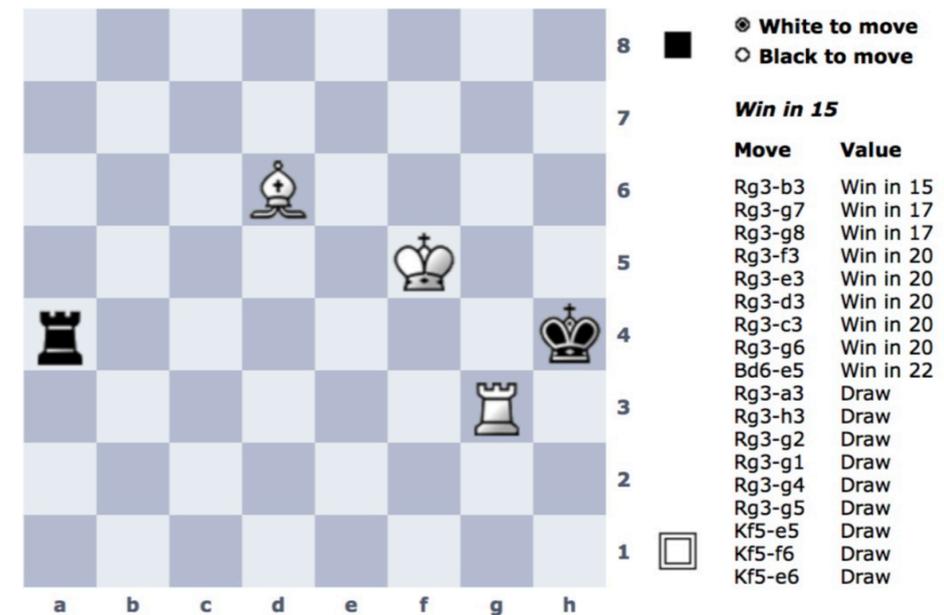
Human Error as a Function of Time



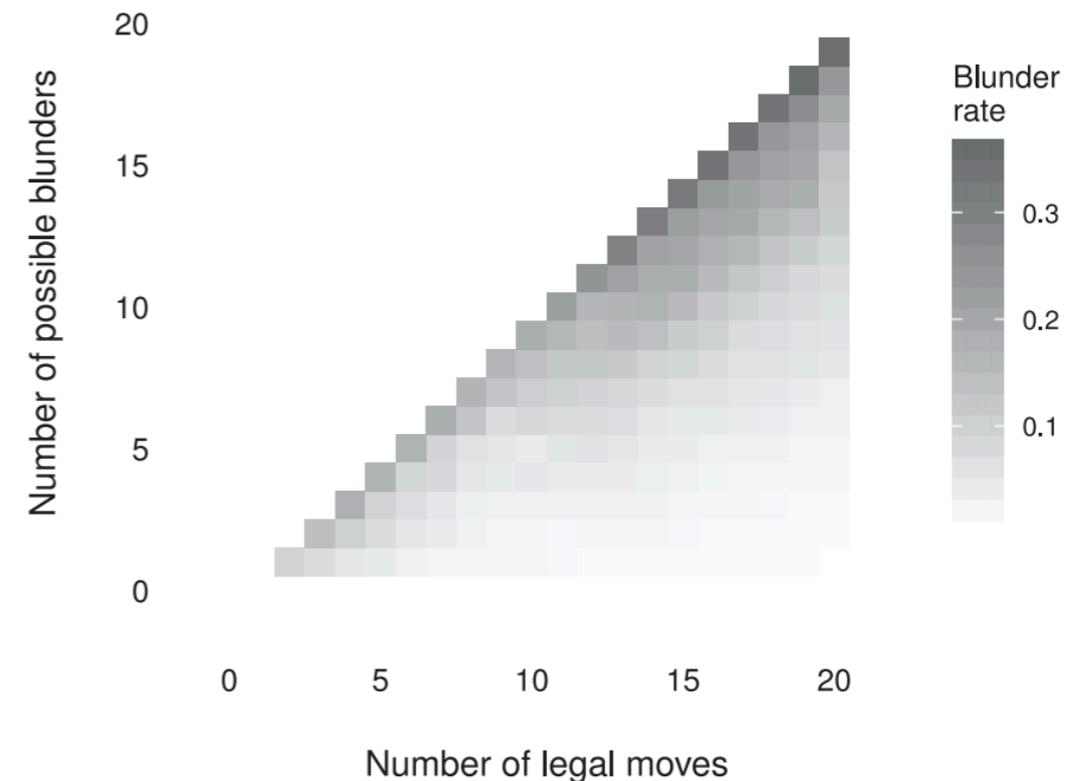
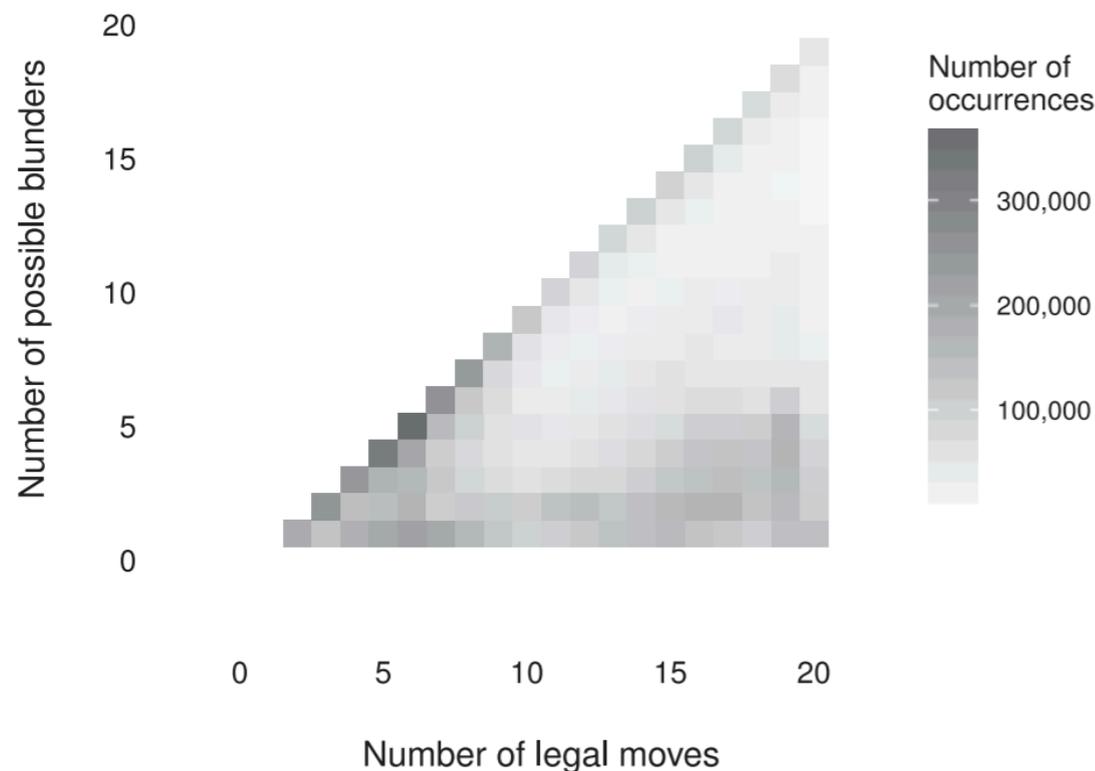
Human Error as a Function of Difficulty

A simple measure for the difficulty of a position: the “blunder potential” is the probability of blundering if you choose a move at random

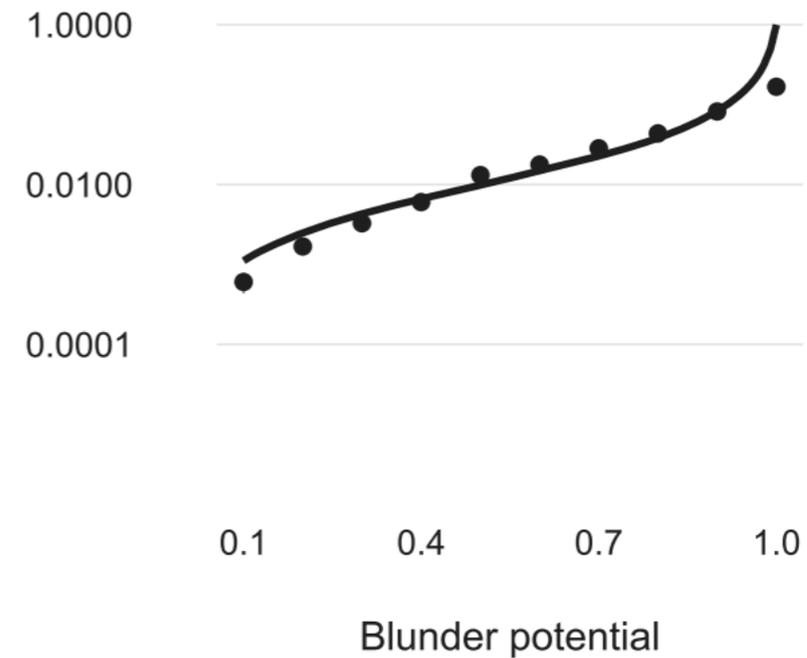
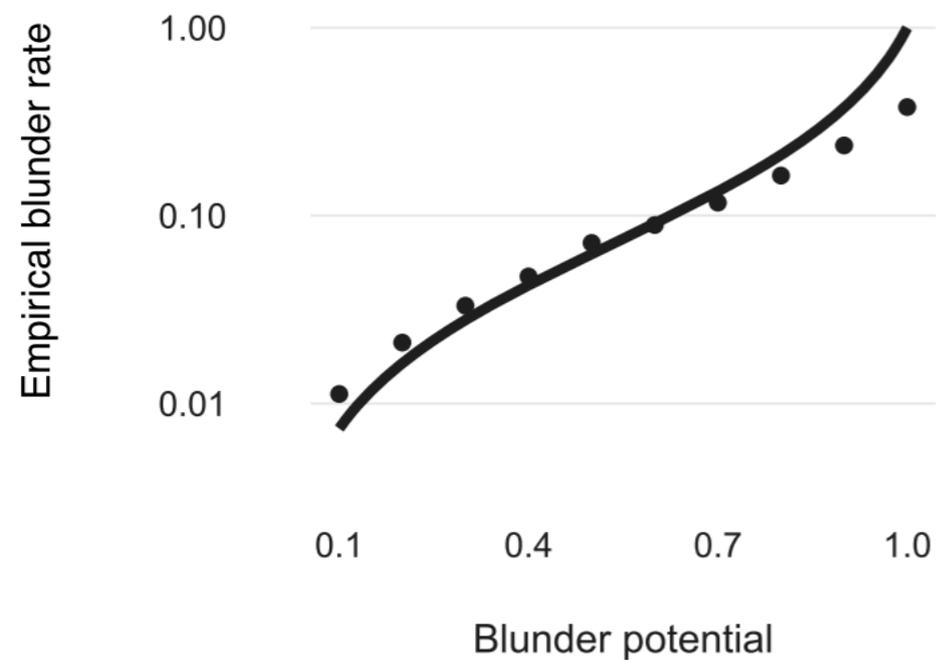
$$\text{Blunder potential} = \frac{\# \text{ possible blunders}}{\# \text{ legal moves}}$$



$$\text{Blunder potential} = 9 / 18 = 0.5$$



Human Error as a Function of Difficulty



Simple, quantal-response model captures how error varies with difficulty:
a particular non-blunder is c times more likely than a particular blunder

Blunder Prediction

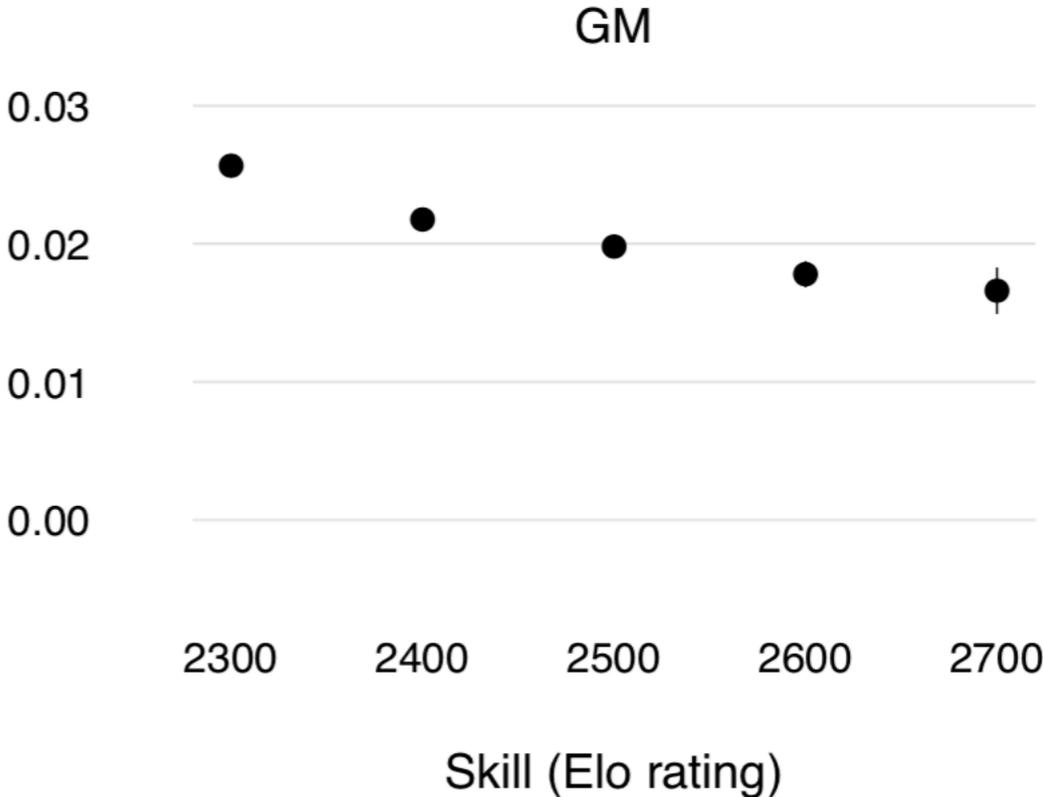
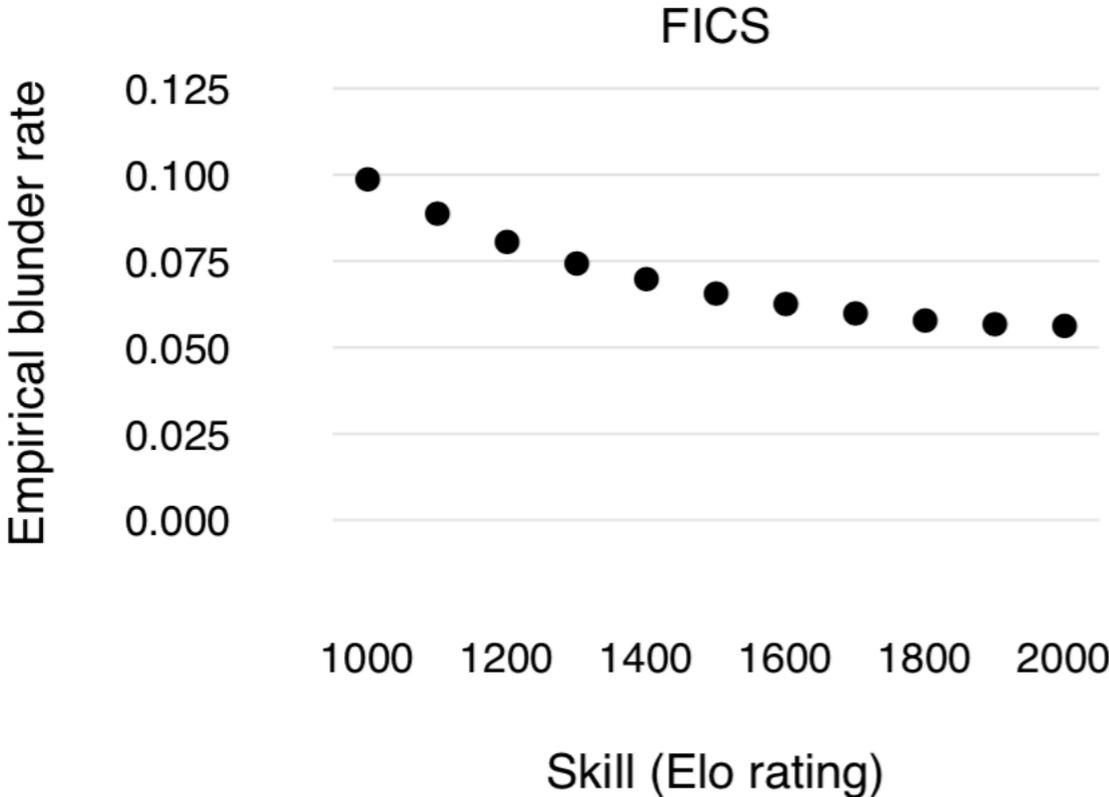
Use fundamental dimensions to predict: will the player blunder in a given instance?

- The difficulty of the position
- The skill of the decision-maker (Elo rating)
- The time remaining
- A set of features encoding difficulty deeper in the game tree

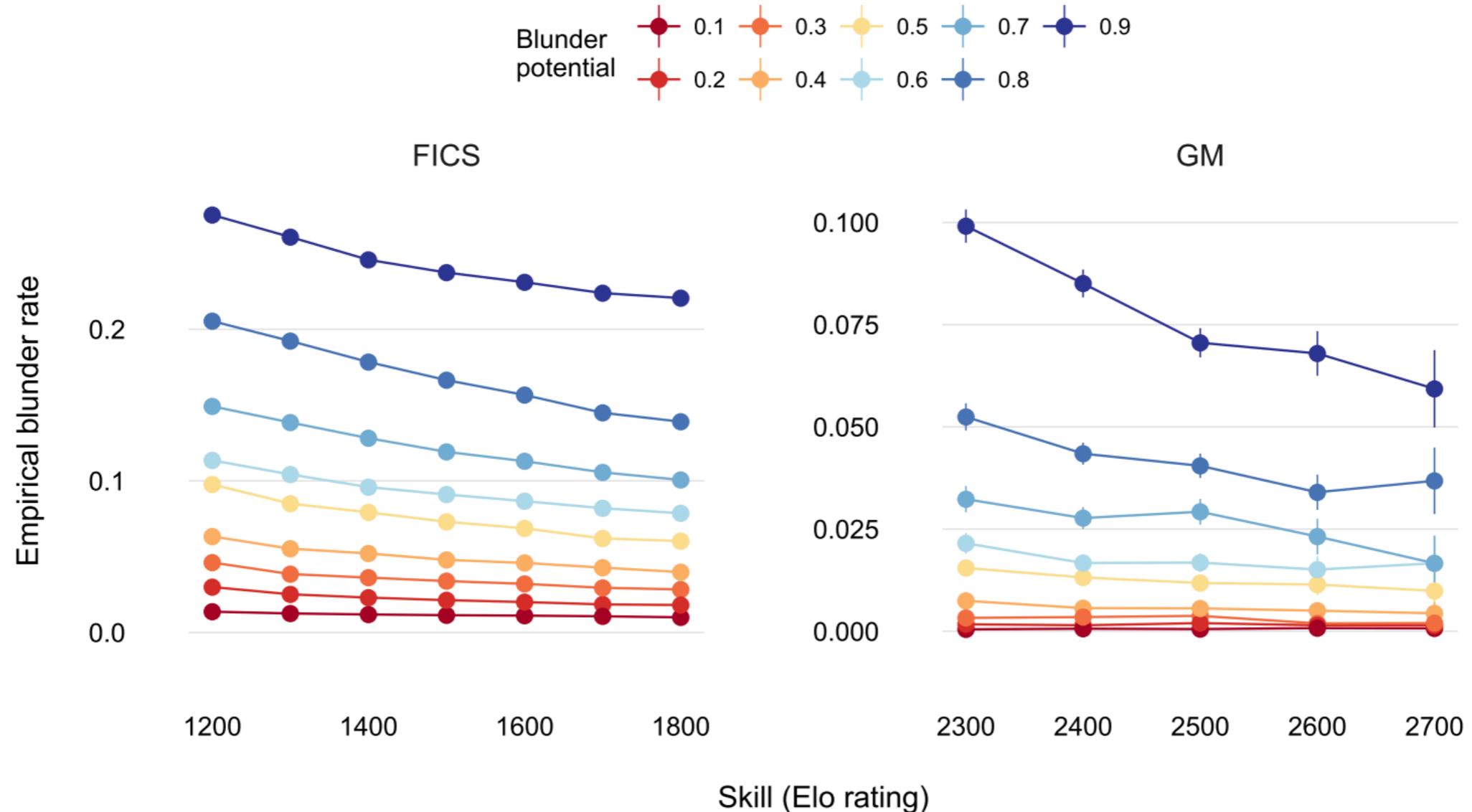
Performance using decision-tree algorithms:

- All features: 75%
- Blunder potential alone: 73%
- Elo of player and opponent: 54%
- Time remaining: 52%

Human Error as a Function of Skill



Human Error as a Function of Skill



Difficulty is the dominant feature

To the extent this is surprising, connections with fundamental attribution error, and Abelson's Paradox [Abelson 1985]

Human Error as a Function of Skill

Fix blunder potential: higher-depth blunder potential is the dominant feature.

Fix the **exact position**: skill and time become predictive.

Difficulty is dominant on average. Is this true point-wise?

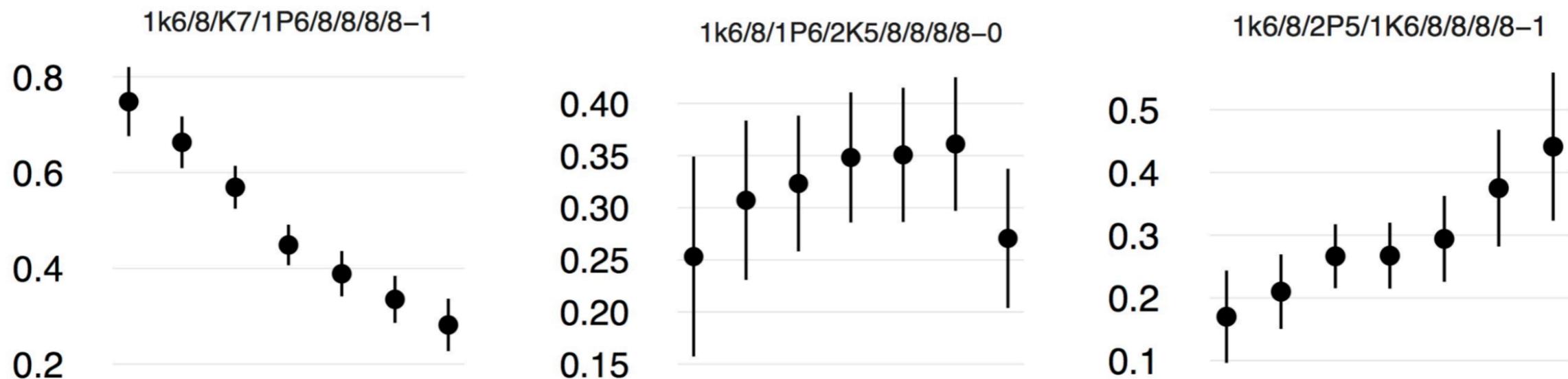
- For position p , examine blunder rate as a function of skill in p
- Call a position **skill-monotone** if blunder rate is decreasing in r
- **Natural conjecture**: all positions are skill-monotone

Fixing the position

Difficulty is dominant on average. Is this true point-wise?

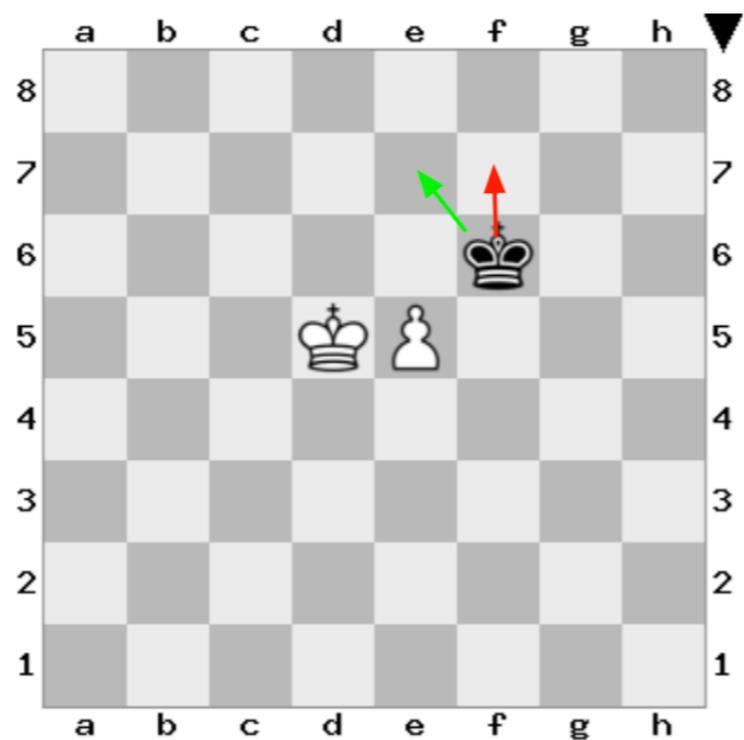
- For position p , examine blunder rate as a function of skill in p
- Call a position skill-monotone if blunder rate is decreasing in r
- Natural conjecture: all positions are skill-monotone

In fact, we observe a **wide variation**, including *skill-anomalous* positions

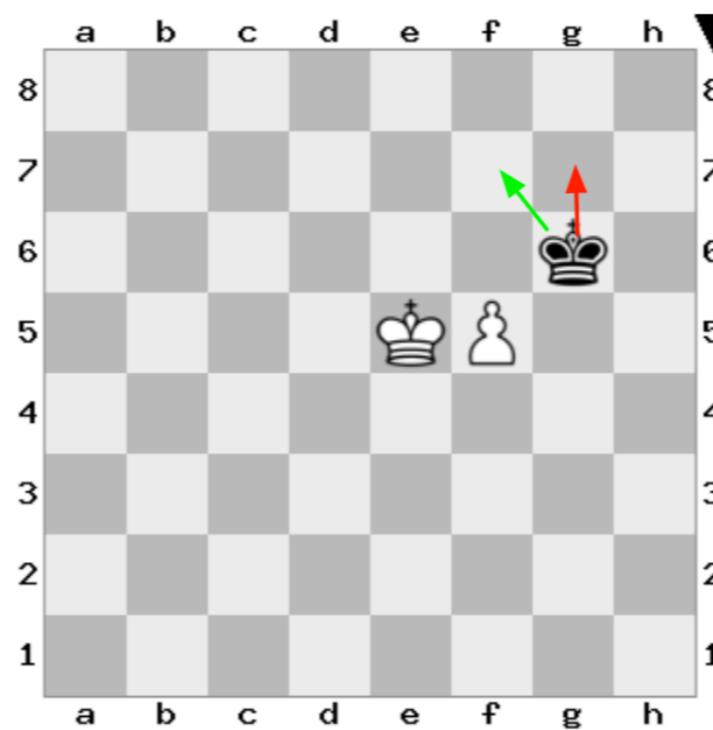


Connections with U-shaped development

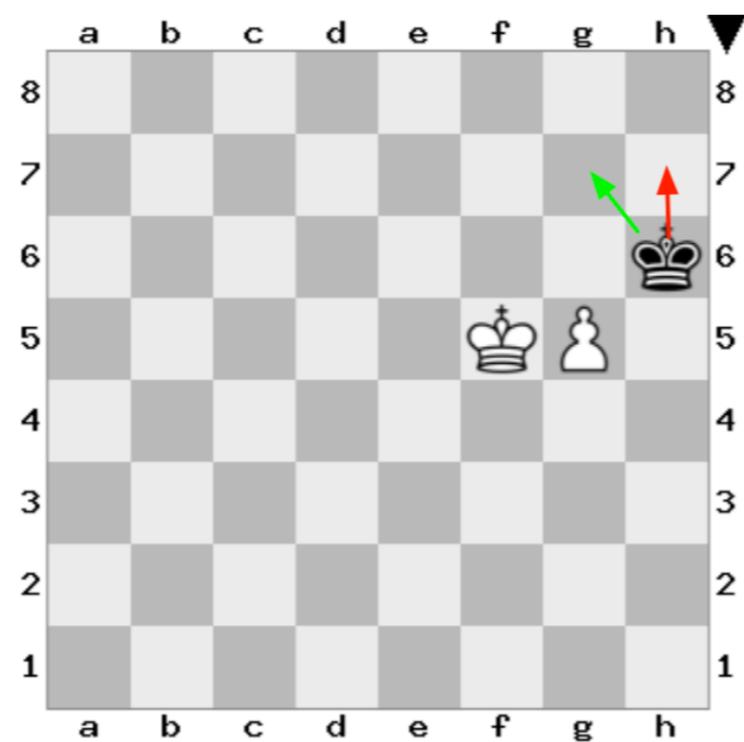
Challenges arising from misleading analogies?



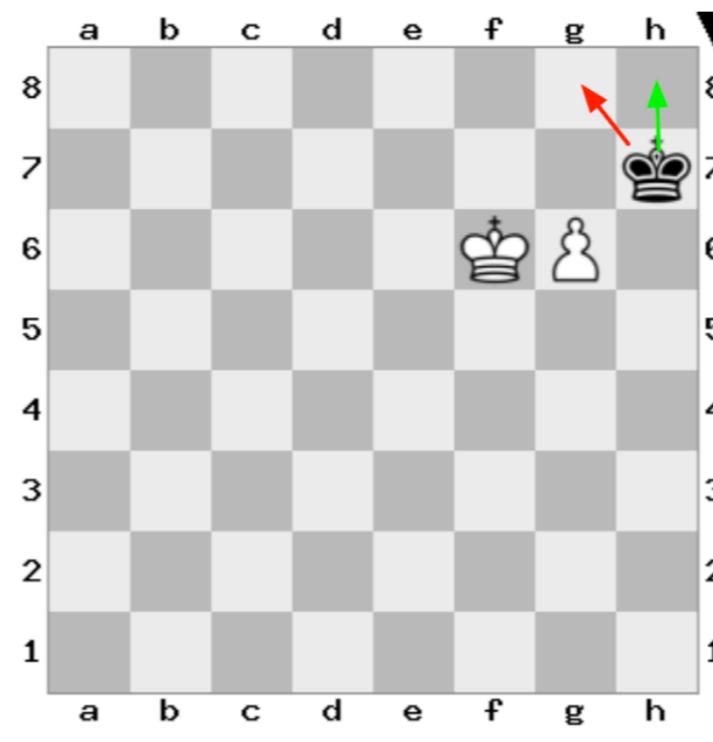
Blunder rate .046



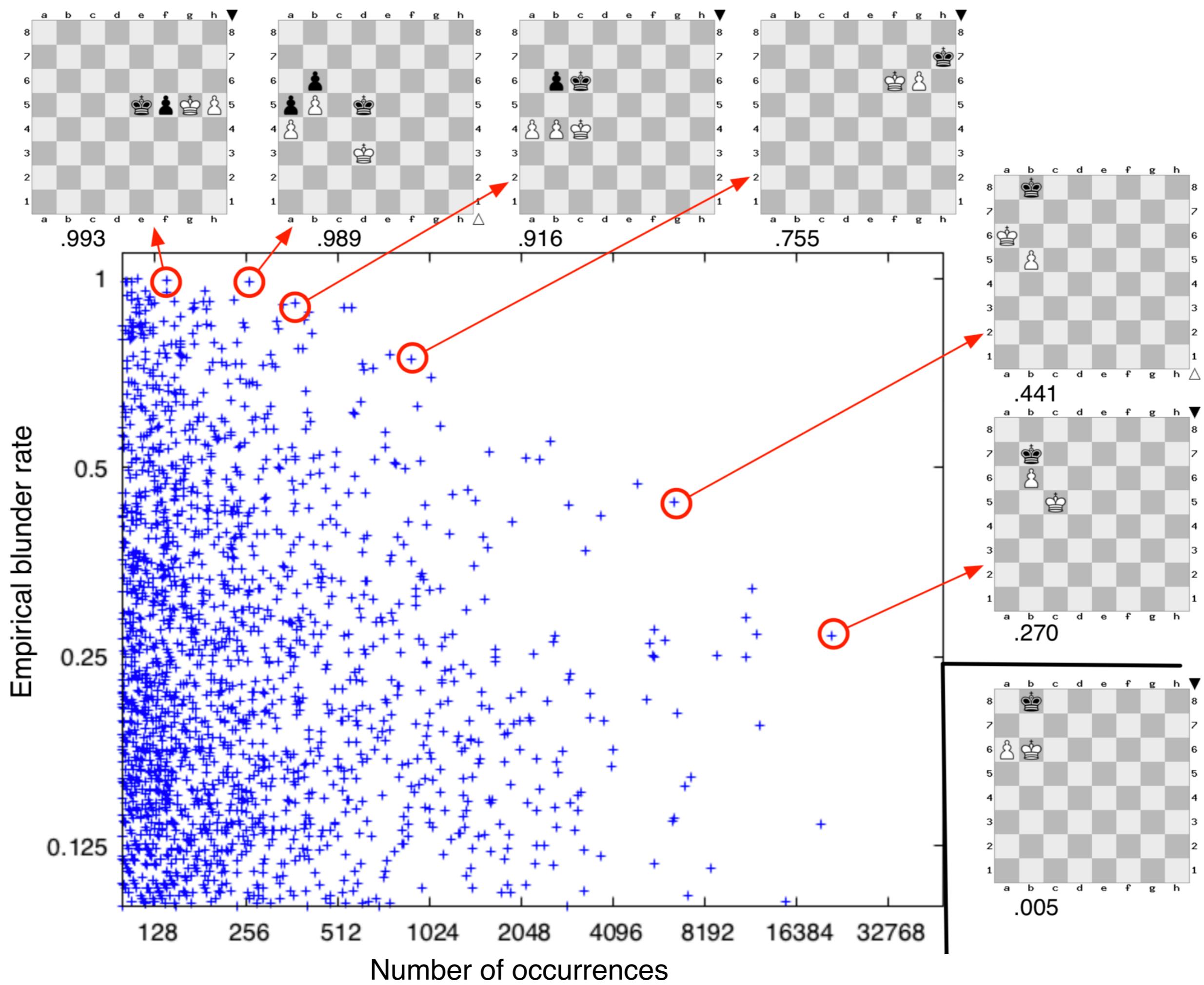
Blunder rate .079



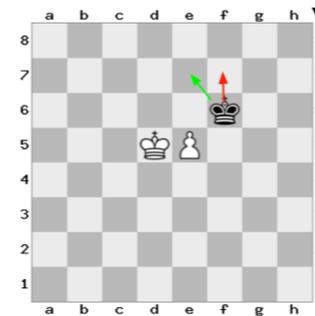
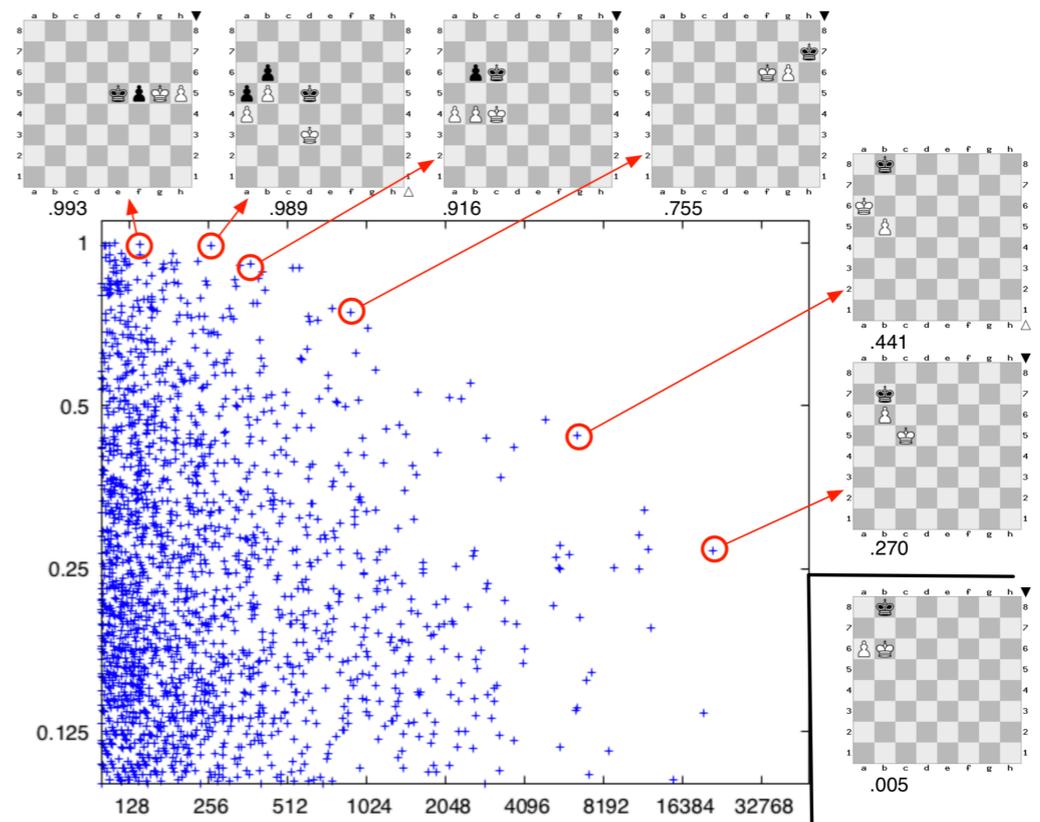
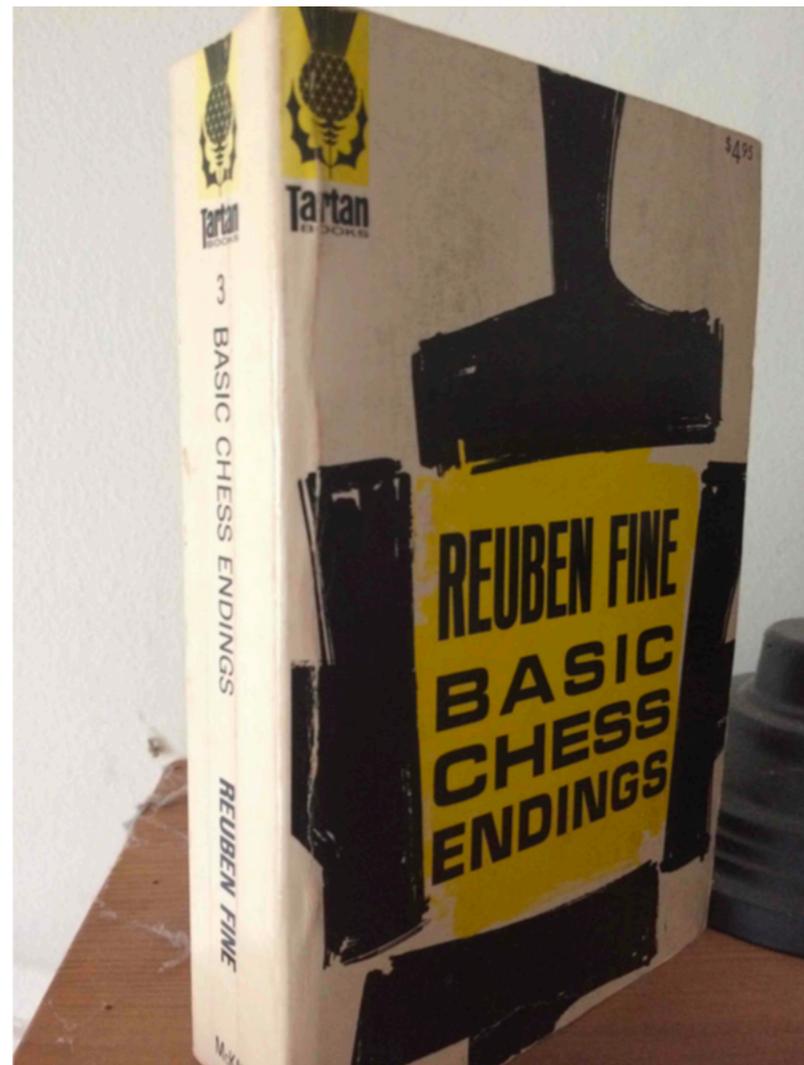
Blunder rate .165



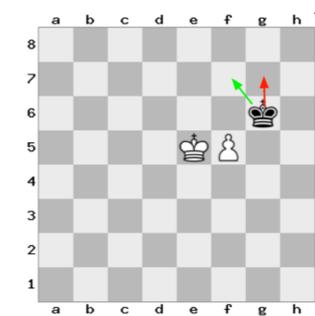
Blunder rate .755



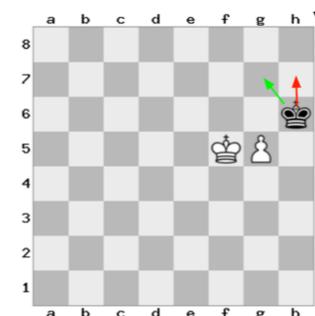
Reflections on Teaching



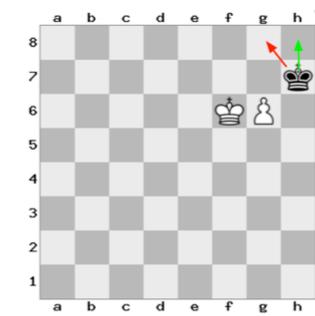
Blunder rate .046



Blunder rate .079



Blunder rate .165



Blunder rate .755

Contrast:

Traditional organization in textbooks

Adding information about frequency and rate

Reflections on Teaching

High-level goal: create a human-like AI

Understand and model human decision-making qualities at various levels

Can we build an algorithmic teacher from large-scale data on human decisions?

Reflections

Framework for analyzing human error given large numbers of similarly structured instances.

Compare human performance to computational benchmark (in this case a perfect one)

In chess, difficulty is the dominant predictor of human error

Similar for other domains?

Opportunities for rich understanding of human decision-making using algorithms