

# Assessing Human Error Against a Benchmark of Perfection

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# Humans and Machines



One leading narrative for AI: **humans versus machines**

For any given domain, when will algorithms exceed expert-level human performance?

# Humans and Machines

A set of questions around human/AI interaction:

- Relative performance of humans and algorithms
- Algorithms as lenses on human decision-making
- Humans and algorithms working together: pathways for introducing algorithms into complex human systems

Can we use algorithms to characterise and predict human error?

# Chess for Decision-Making

Long-standing **model system** for decision-making

- “The drosophila of artificial intelligence.”  
—John McCarthy, 1960
- “The drosophila of psychology.”  
—Herb Simon and William Chase, 1973



Chess provides data on a sequence of cognitively difficult tasks.  
When a human player chooses a move, we have data on:

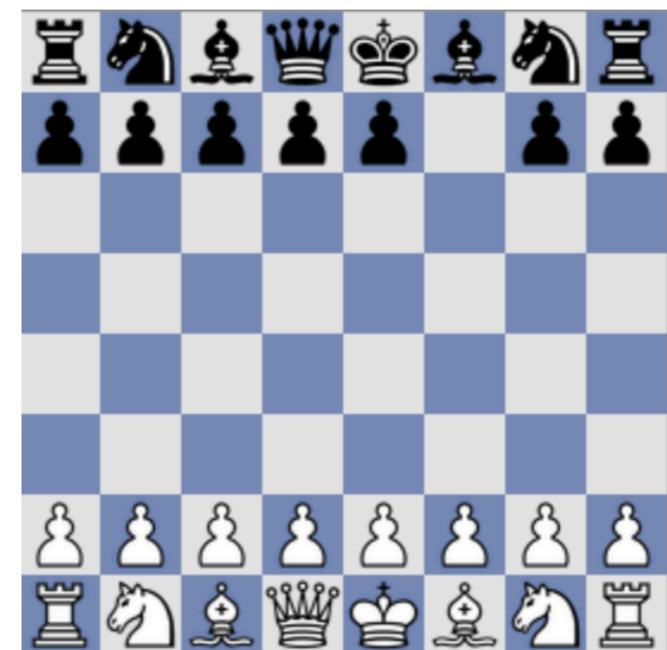
- The task instance: the chess position itself.
- The skill of the decision-maker: a chess player’s Elo rating.
- The time available to make the decision.

Can we use computation to analyze human performance?

- Characterize human “blunders” (mistakes in choice of move)
- Chess as the drosophila of machine superintelligence?

# A History of Chess Engines

- 1988: First recorded win by computer against human grandmaster under standard tournament conditions.
- 1997: Deep Blue defeats world champion Kasparov in 6-game match.
- 2002–2003: Draws against world champions using desktop computers.
- 2005: Last recorded win by a human player against a full-strength desktop computer engine under standard tournament conditions.
- 2007: Computers defeat several top players with “pawn odds.”



# Chess for Decision-Making

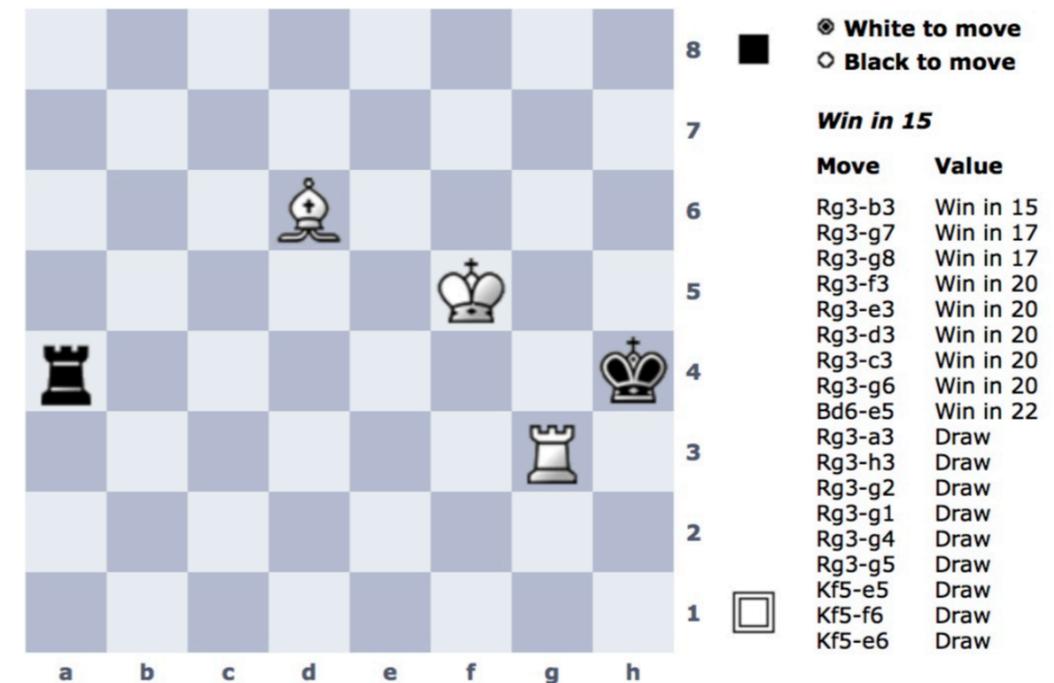


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Analysis 1
Lines: 3 [v] [u] Stock [v] [v] Stop
-1.41 [u] [*] 2... Rc4 3. Rb6+ Kf5 4. Rxa6 d4 5. Ra5+
Kf6 6. Bf2 Rc1+ 7. Ke2 d3+ 8. Kxd3 Nxf2+ 9. Ke3 Nh1
10. h4 gxh4 11. Rxh5 Rc4 12. a5 Ng3 13. Rh8 Nf5+
14. Kf3 Ra4 15. Ra8 Nd4+ 16. Kg4 Nc6+ 17. Kh3
Nxa5 (depth 20, 0:00:09)
-1.07 [u] [*] 2... Rc2 3. g4 hxg4 4. hxg4 Rc4 5. Rb6+
Kf7 6. Rb7+ Ke6 7. Rb6+ Ke5 8. Rxa6 d4 9. Ra5+ Kf6
10. Bg1 Rc1+ 11. Kg2 d3 12. Bd4+ Kg6 13. Be3 d2 14.
Ra6+ Kf7 15. Ra7+ Ke6 16. Ra6+ Ke5 17. Ra5+ Kf6
18. Ra6+ Ke7 19. Ra7+ Kd6 20. Bxd2 Nxd2 21. Rg7
(depth 19, 0:00:09)
-0.94 [u] [*] 2... g4 3. hxg4 hxg4 4. Rd7 Nf6 5. Re7
Rc4 6. a5 Kf5 7. Rf7 d4 8. Bd2 Ke6 9. Ra7 Ne4 10.
Rxa6+ Kf5 11. Be1 Rc1 12. Ra8 d3 13. Rf8+ Kg5 14.
Rg8+ Kf4 15. a6 (depth 19, 0:00:09)
[u] 2... Rc4 (suggested move)
```

Could use chess engines to evaluate moves [Biswas-Regan 2015]

- Promising, since engines are vastly superior to the world's best players
- Engines sometimes detect clear-cut errors, but very often a “grey area”: engines and humans disagree, but doesn't necessarily change the outcome of the game

# Chess for Decision-Making



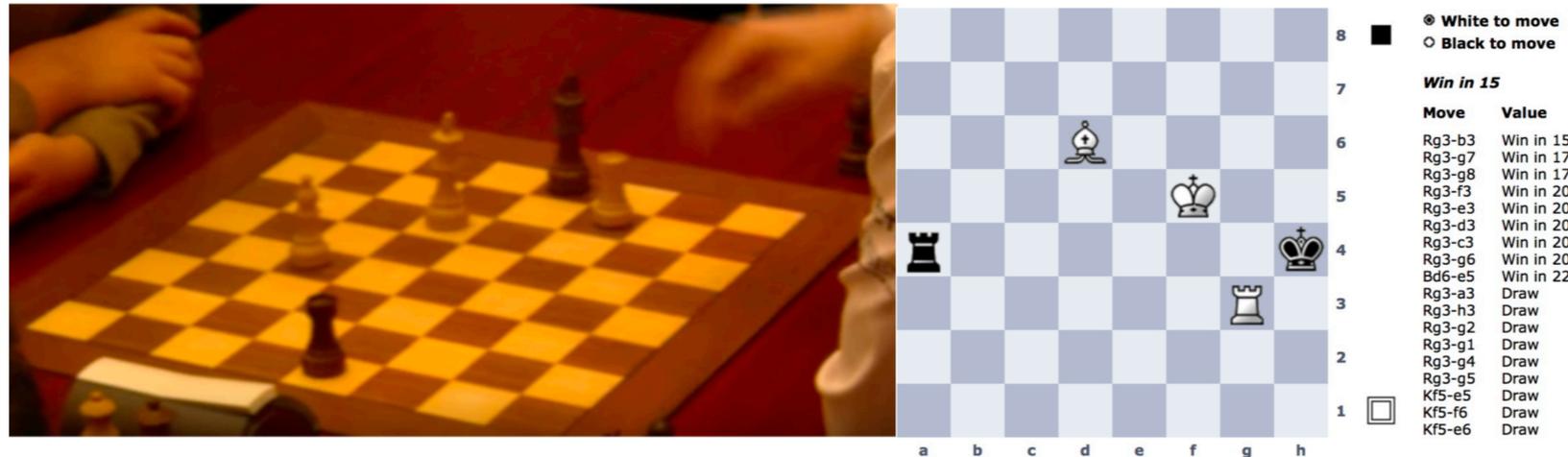
We use the fact that chess has been **solved** for positions with at most 7 pieces on the board.

- “Tablebases” record all possible positions with  $\leq 7$  pieces
- Can determine (game-theoretic) blunders by table look-up
- These positions are still difficult for even the world’s best players

*The Stiller moves are awesome, almost scary, because you know they are the truth, God’s Algorithm; it’s like being revealed the Meaning of Life, but you don’t understand one word.*

— Tim Krabbé, commenting on an early tablebase by Lewis Stiller

# Chess for Decision-Making



Data from two sources:

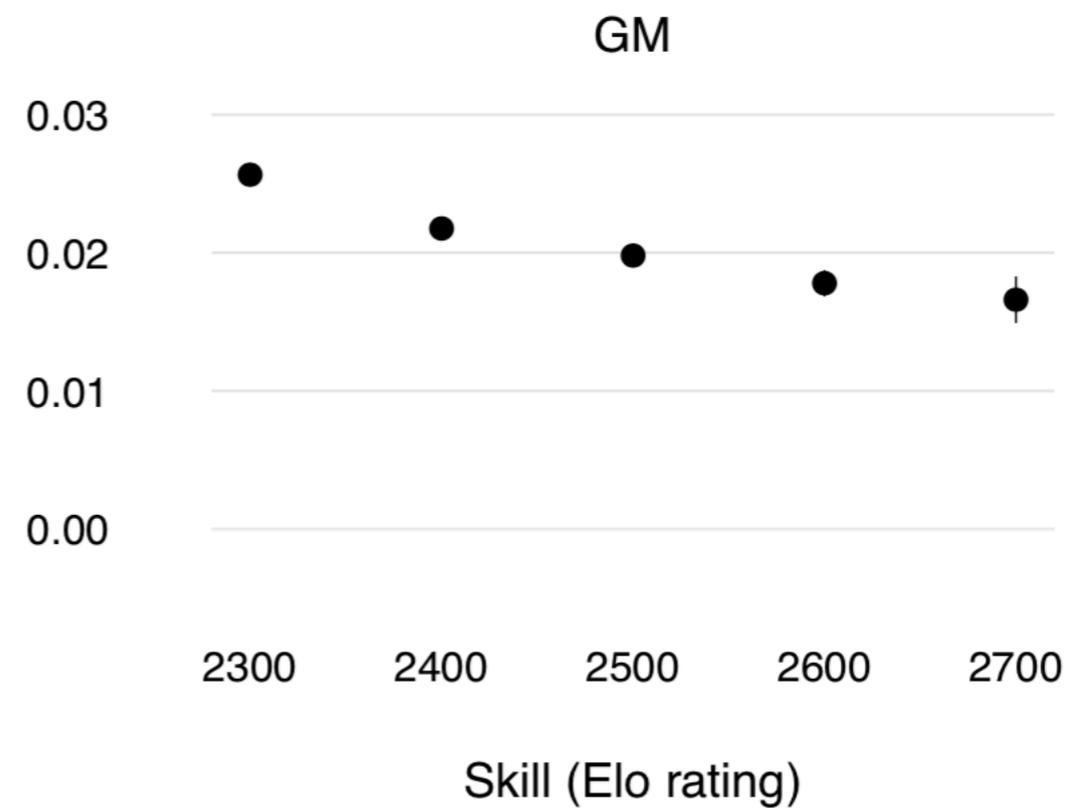
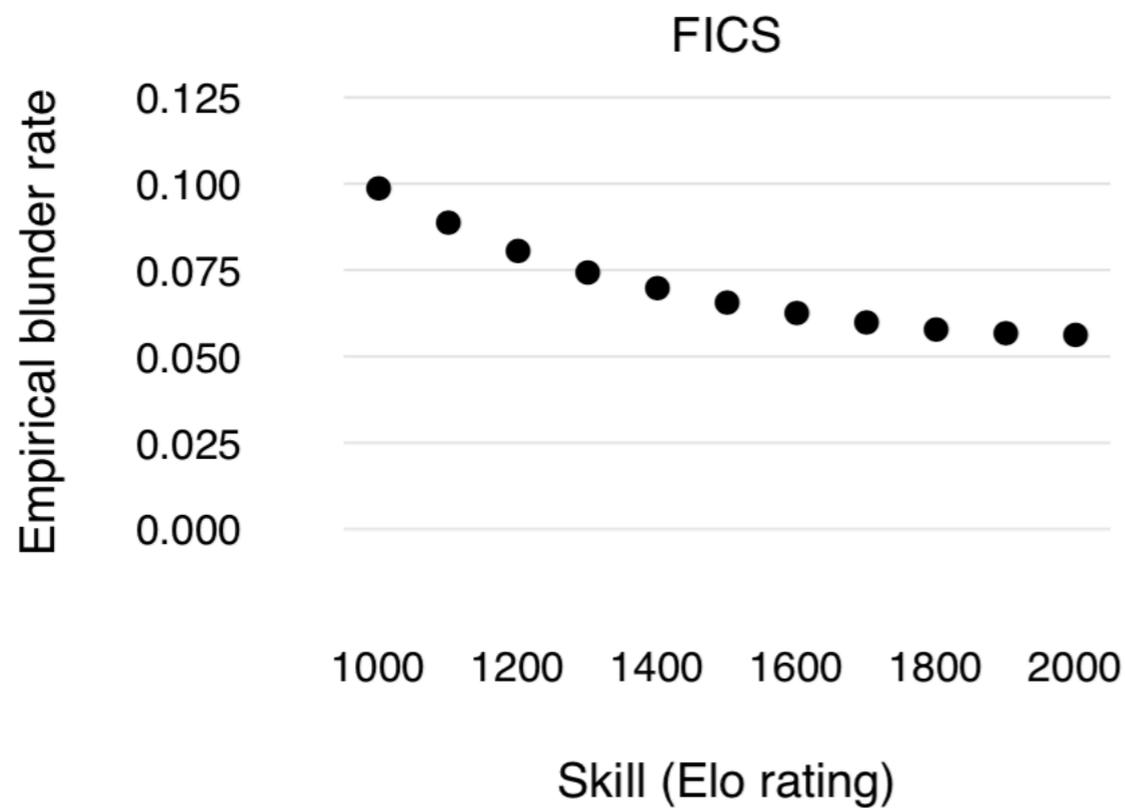
	# Games	Rating	Duration	Setting
<b>FICS</b>	200M	1200–1800	Minutes	Casual enthusiasts playing online
<b>GM</b>	1M	2400–2800	Hours	Professional tournaments

Take all <7-piece positions, classify a move as a blunder if and only if it changes the win/loss/draw outcome

# Basic Dependence on Fundamental Dimensions

How does decision quality vary with  skill  
time ?  
difficulty

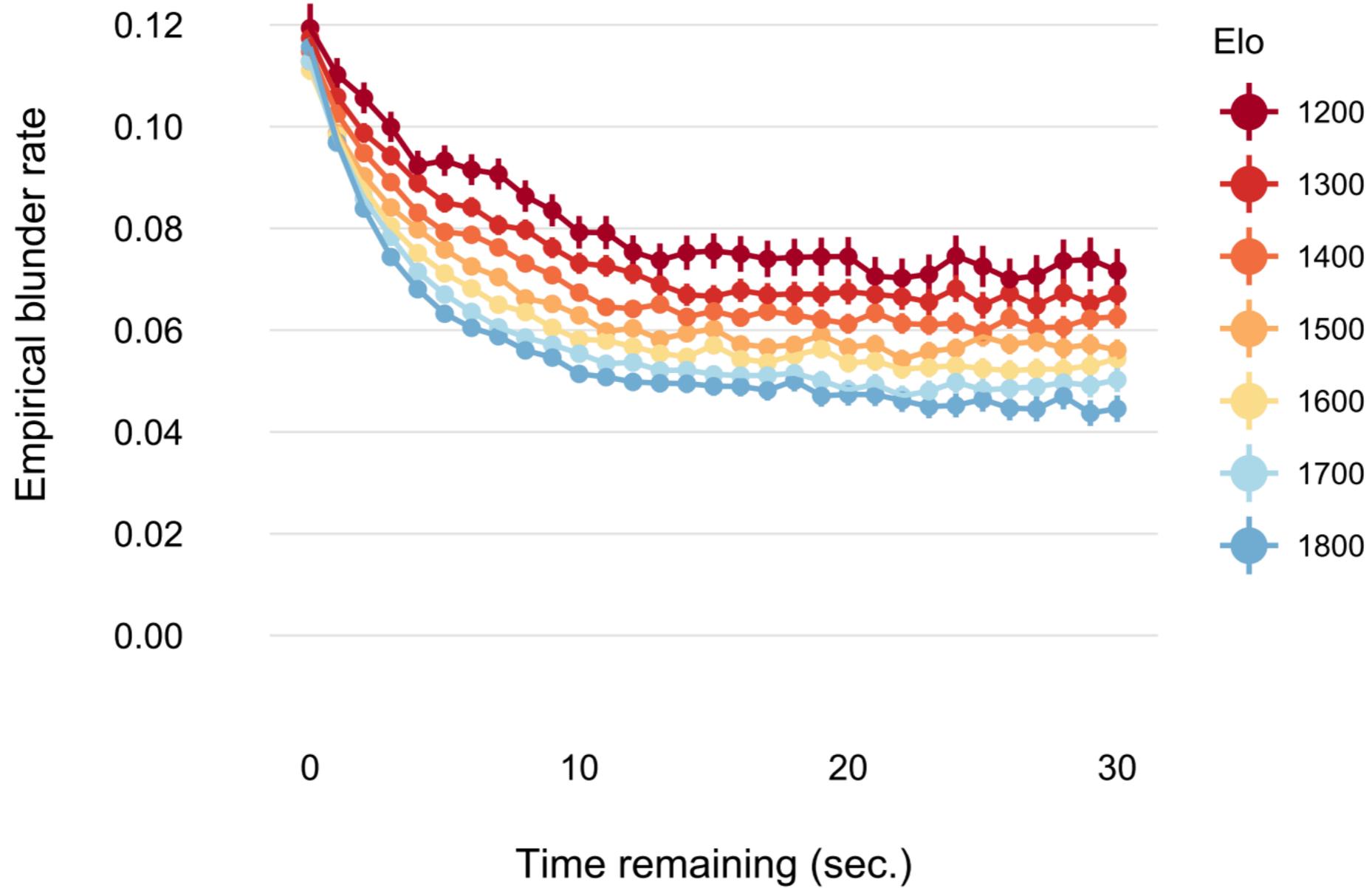
# Human Error as a Function of Skill



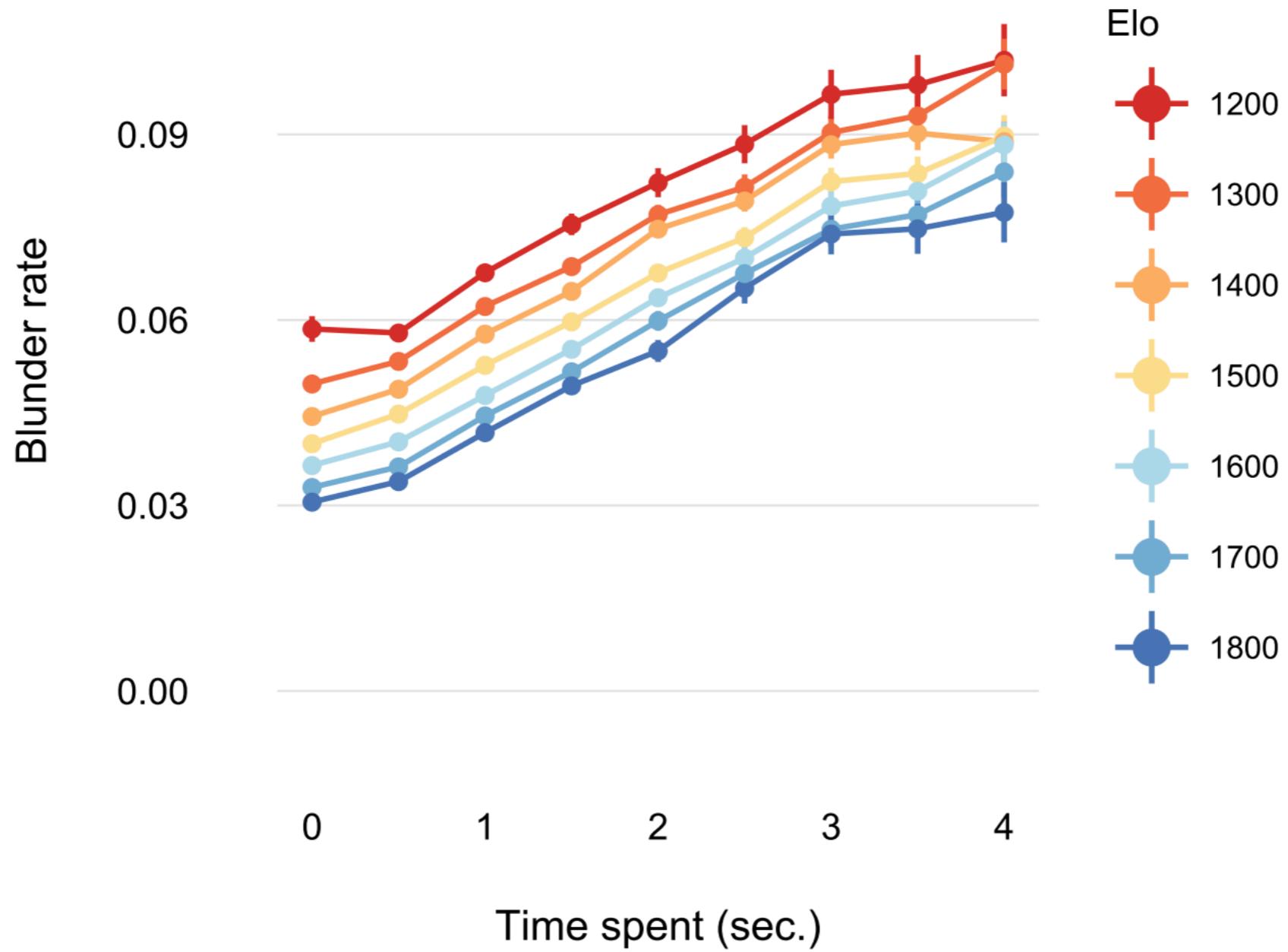
- 1000: Winner of a local scholastic contest
- 1600: Competent amateur
- 2000: Top 1% of players

- 2300: Lowest international title
- 2500: Grandmaster
- 2850: Current world champion

# Human Error as a Function of Time



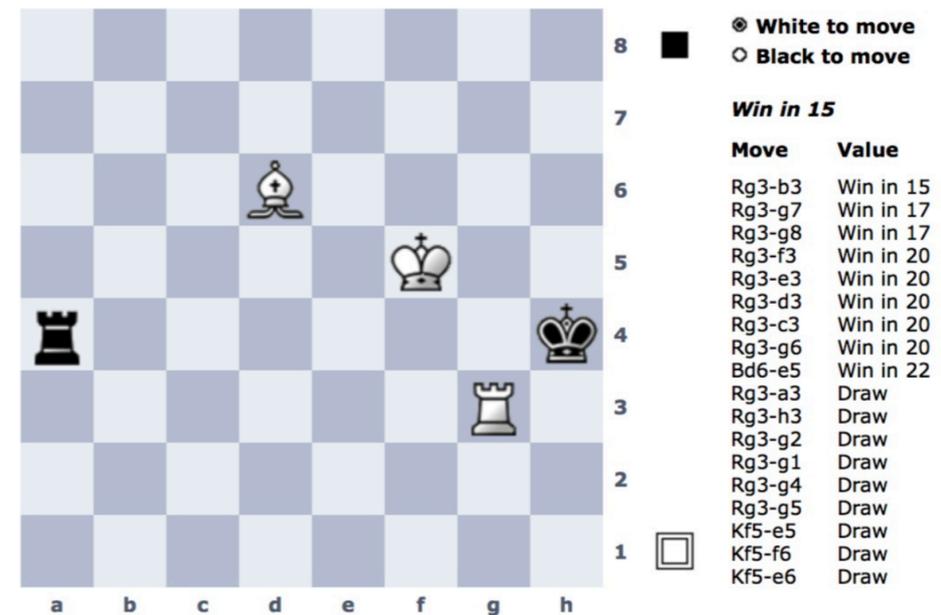
# Human Error as a Function of Time



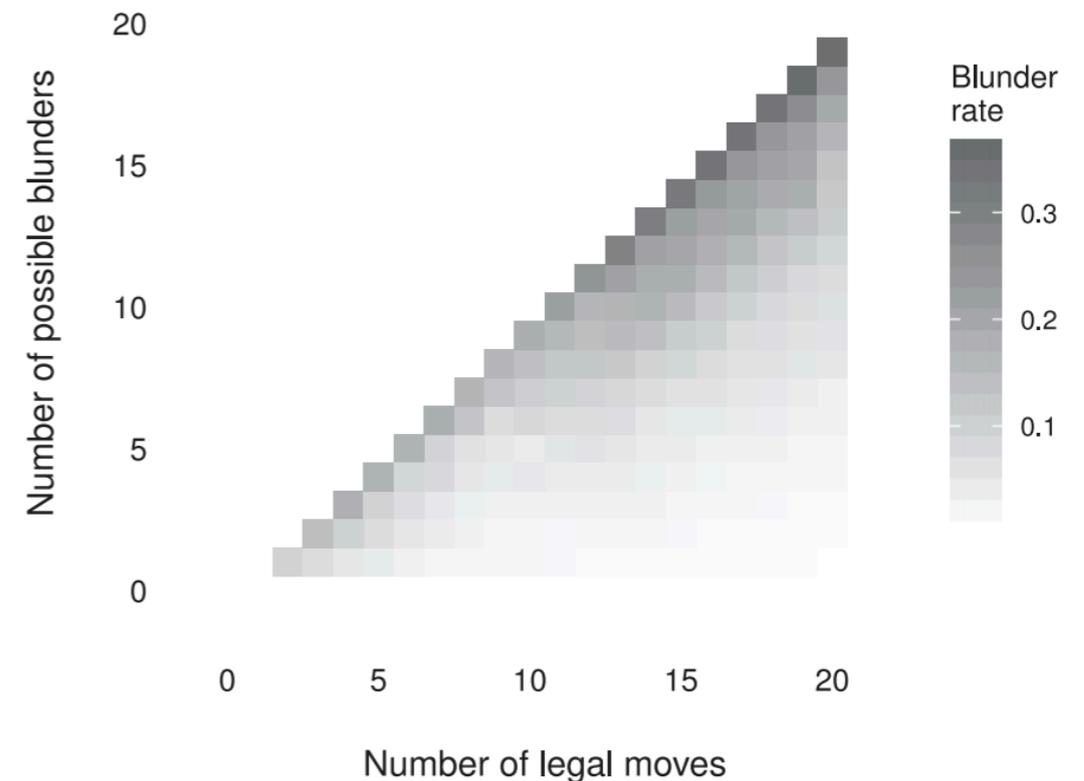
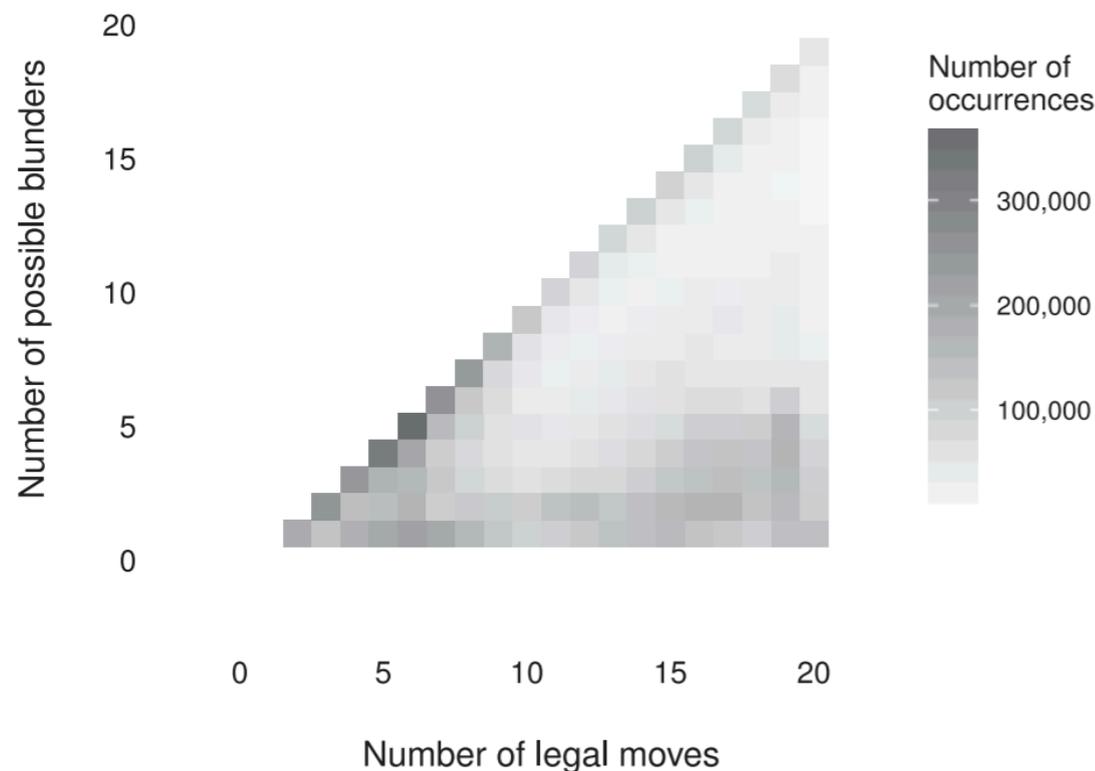
# Human Error as a Function of Difficulty

A simple measure for the difficulty of a position: the “blunder potential” is the probability of blundering if you choose a move at random

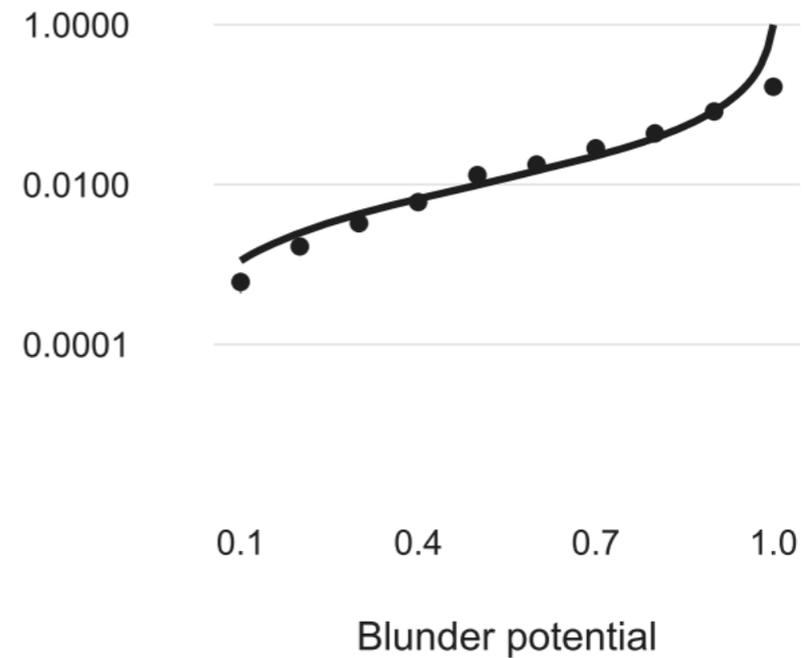
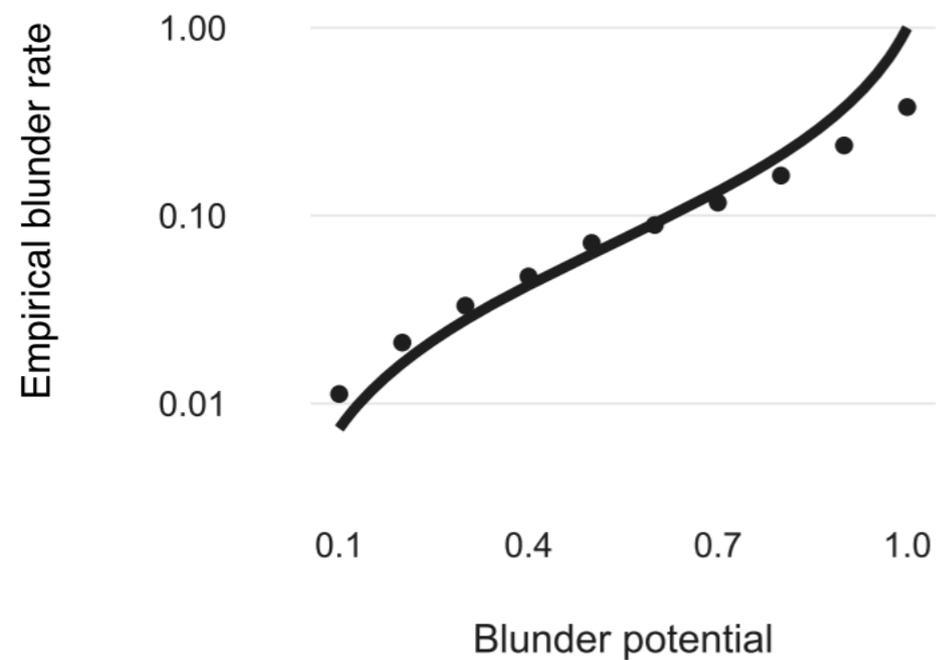
$$\text{Blunder potential} = \frac{\# \text{ possible blunders}}{\# \text{ legal moves}}$$



$$\text{Blunder potential} = 9 / 18 = 0.5$$



# Human Error as a Function of Difficulty



Simple, quantal-response model captures how error varies with difficulty:  
a particular non-blunder is  $c$  times more likely than a particular blunder

# Blunder Prediction

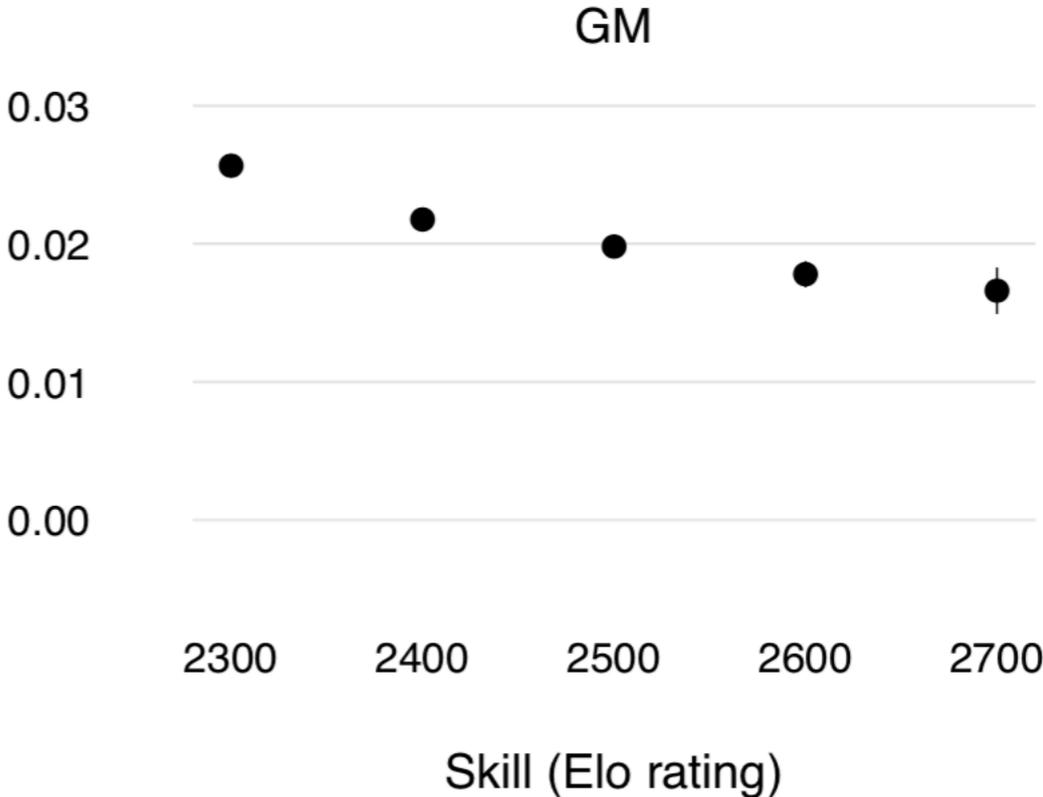
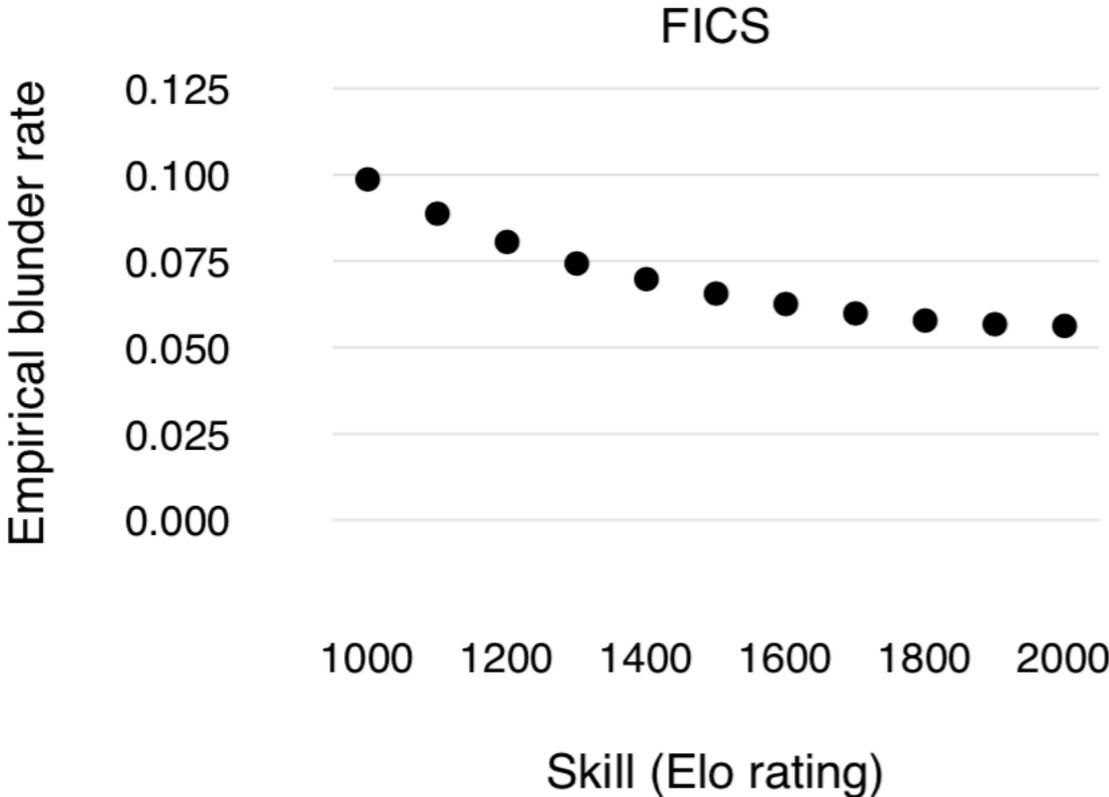
Use fundamental dimensions to predict: will the player blunder in a given instance?

- The difficulty of the position
- The skill of the decision-maker (Elo rating)
- The time remaining
- A set of features encoding difficulty deeper in the game tree

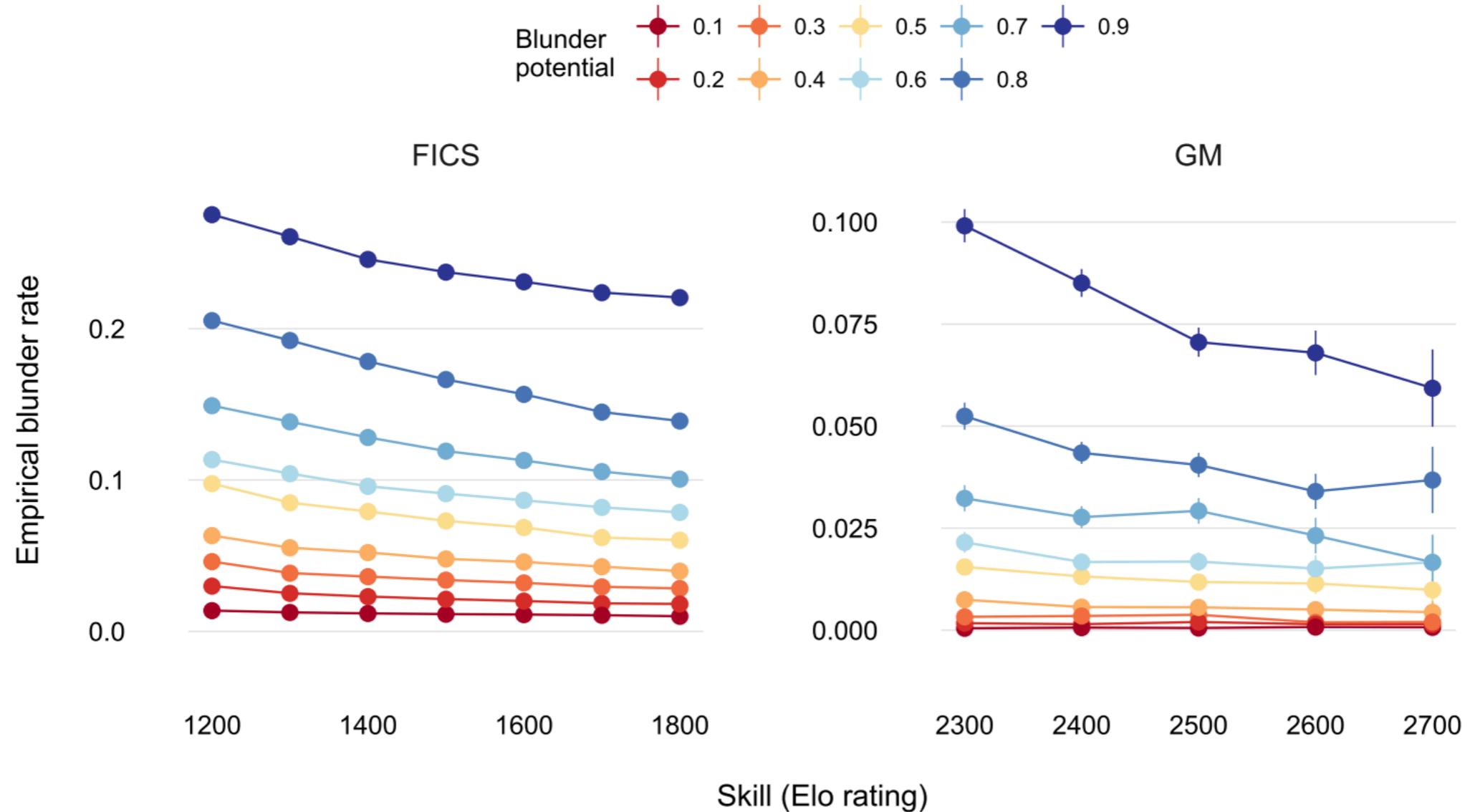
Performance using decision-tree algorithms:

- All features: 75%
- Blunder potential alone: 73%
- Elo of player and opponent: 54%
- Time remaining: 52%

# Human Error as a Function of Skill



# Human Error as a Function of Skill



Difficulty is the dominant feature

To the extent this is surprising, connections with fundamental attribution error, and Abelson's Paradox [Abelson 1985]

# Human Error as a Function of Skill

Fix blunder potential: higher-depth blunder potential is the dominant feature.

Fix the **exact position**: skill and time become predictive.

Difficulty is dominant on average. Is this true point-wise?

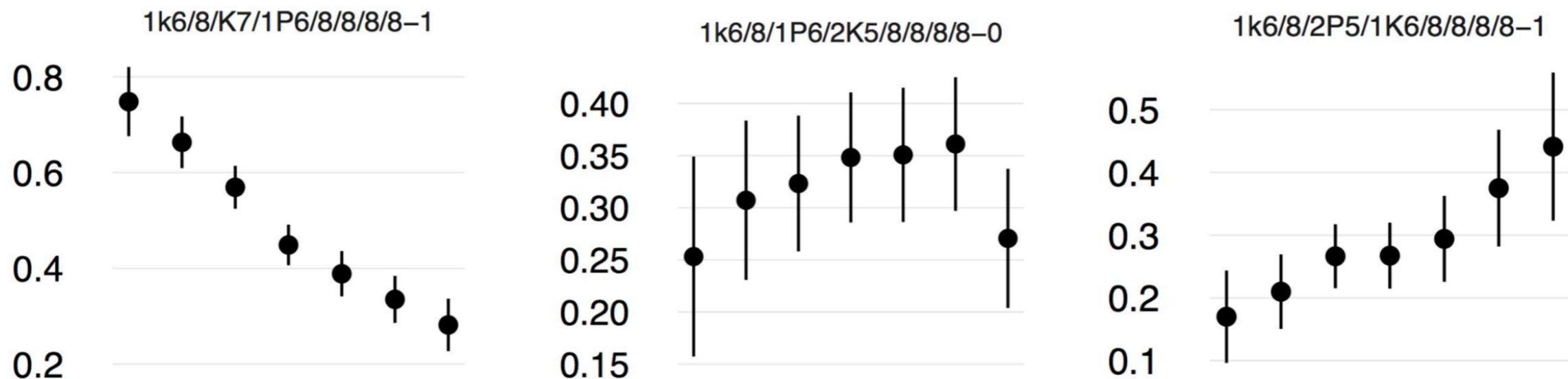
- For position  $p$ , examine blunder rate as a function of skill in  $p$
- Call a position **skill-monotone** if blunder rate is decreasing in  $r$
- **Natural conjecture**: all positions are skill-monotone

# Fixing the position

Difficulty is dominant on average. Is this true point-wise?

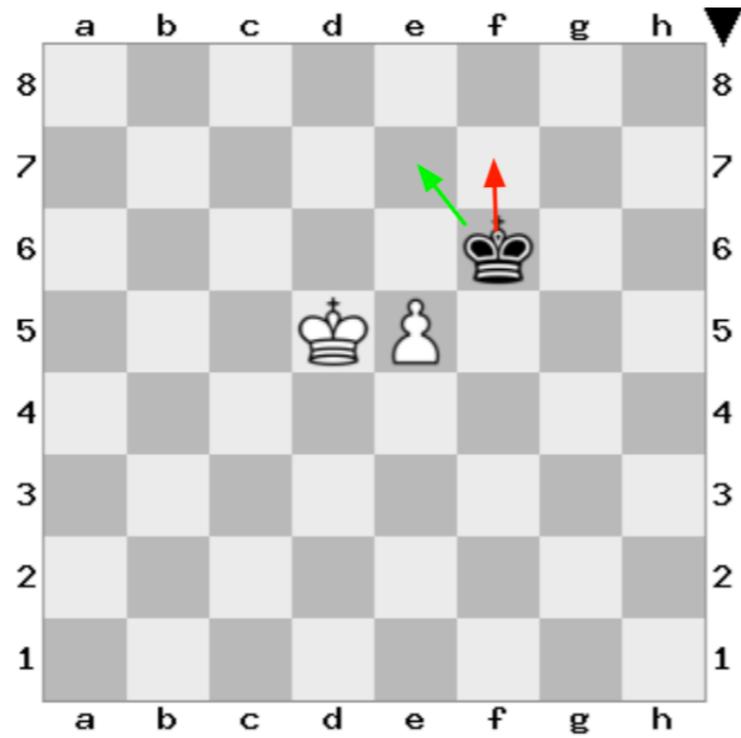
- For position  $p$ , examine blunder rate as a function of skill in  $p$
- Call a position skill-monotone if blunder rate is decreasing in  $r$
- Natural conjecture: all positions are skill-monotone

In fact, we observe a **wide variation**, including *skill-anomalous* positions

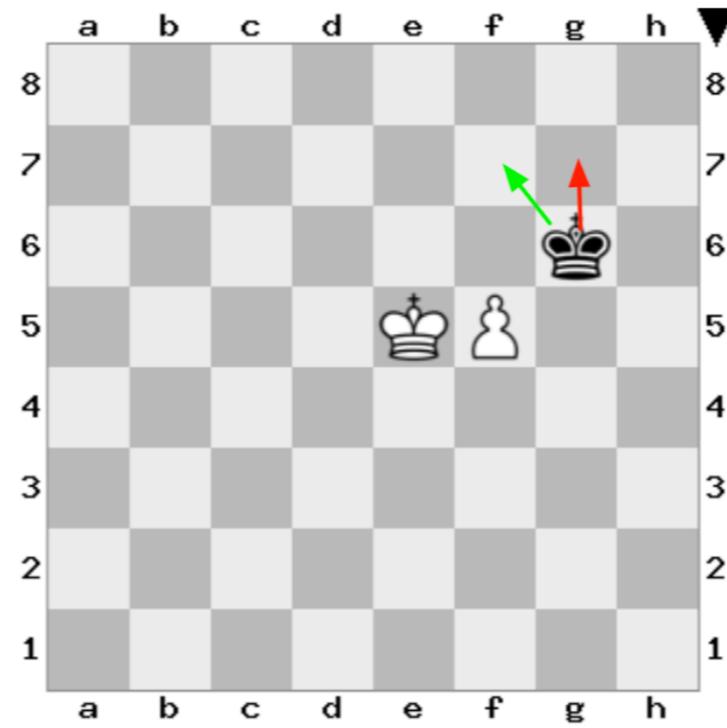


Connections with U-shaped development

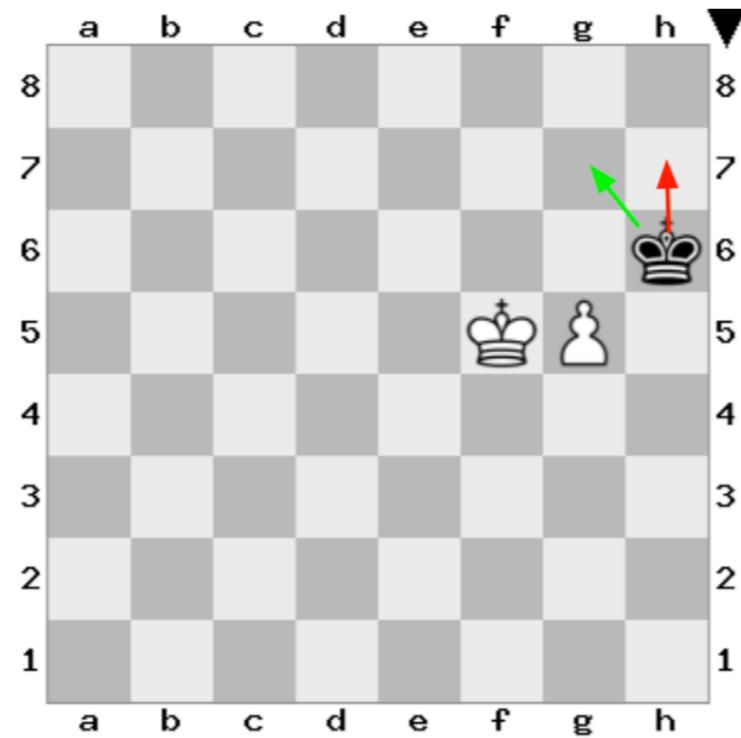
# Challenges arising from misleading analogies?



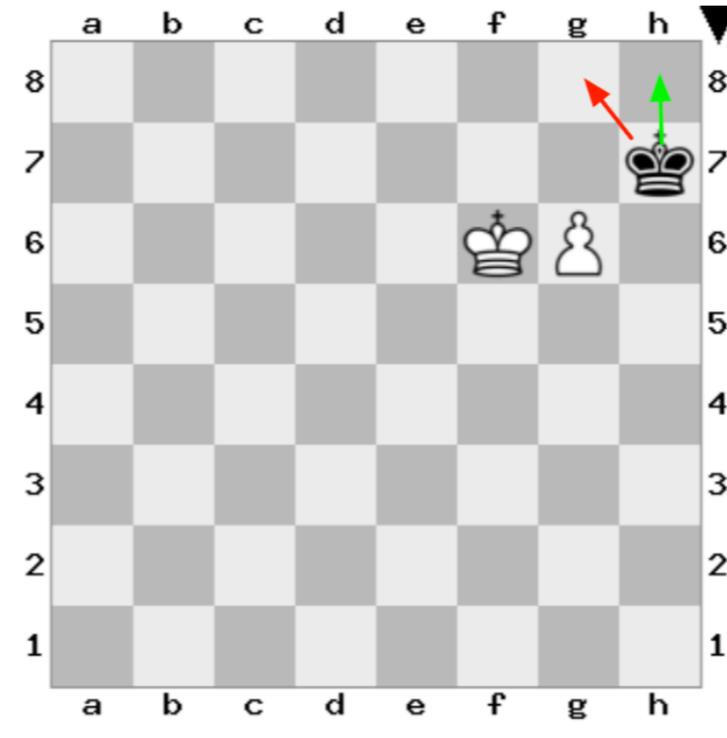
Blunder rate .046



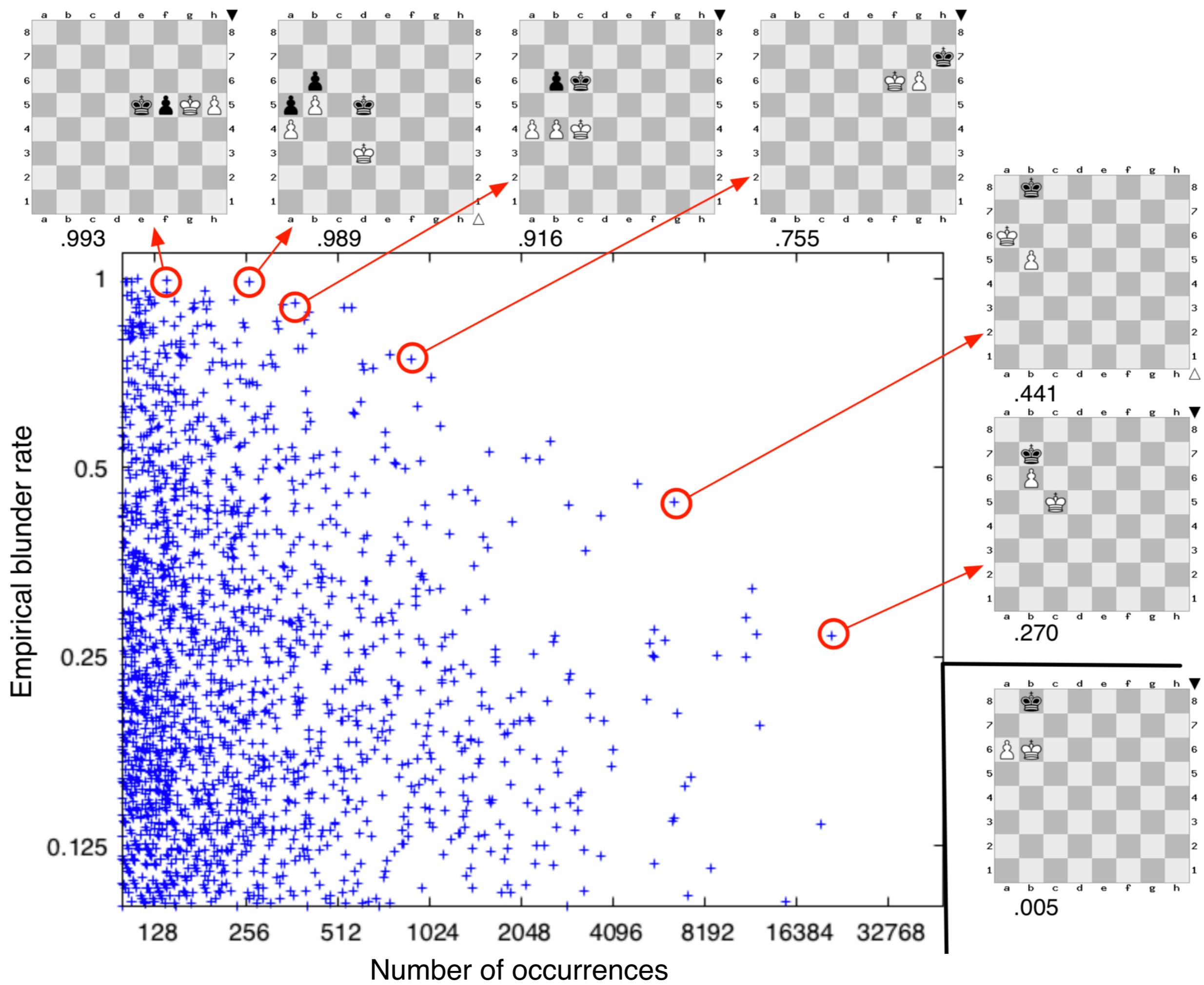
Blunder rate .079



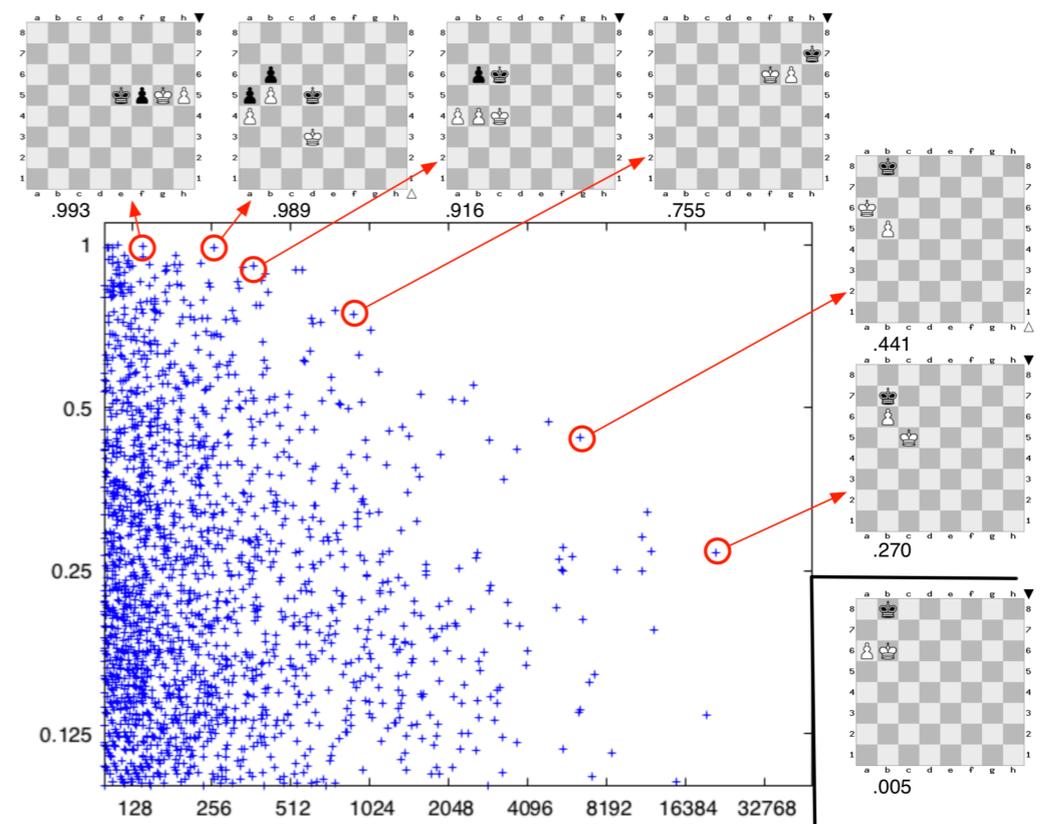
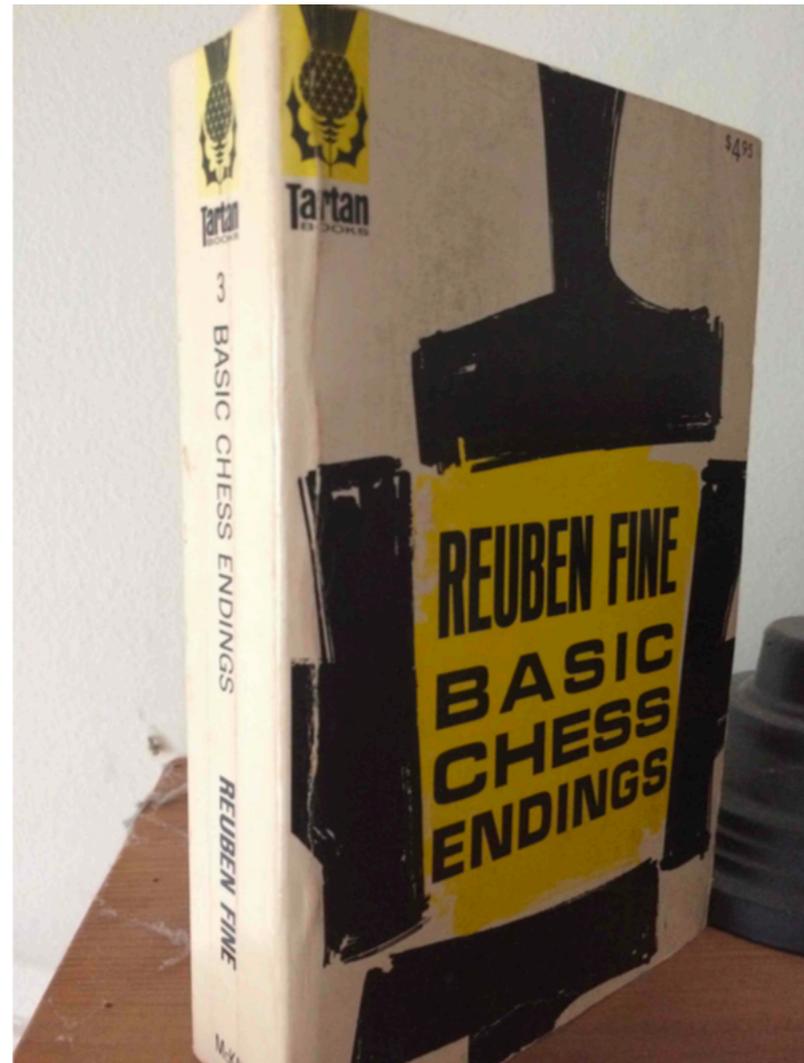
Blunder rate .165



Blunder rate .755



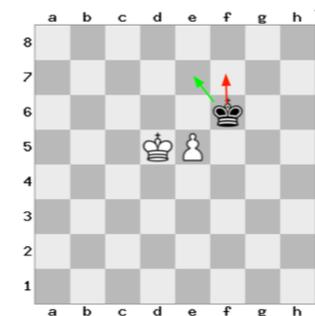
# Reflections on Teaching



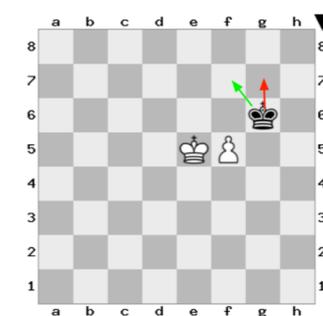
Contrast:

Traditional organization in textbooks

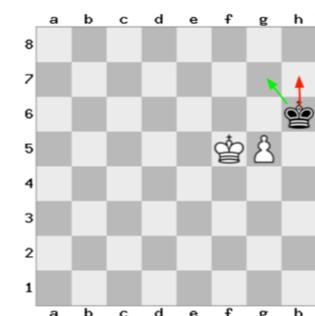
Adding information about frequency and rate



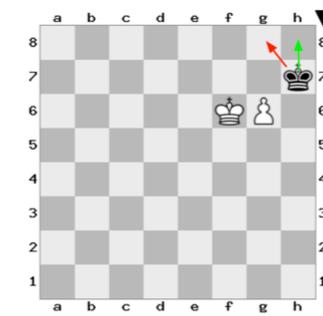
Blunder rate .046



Blunder rate .079



Blunder rate .165



Blunder rate .755

# Reflections on Teaching

High-level goal: create a human-like AI

Understand and model human decision-making qualities at various levels

Can we build an algorithmic teacher from large-scale data on human decisions?

# Reflections

Framework for analyzing human error given large numbers of similarly structured instances.

Compare human performance to computational benchmark (in this case a perfect one)

In chess, difficulty is the dominant predictor of human error

Similar for other domains?

Opportunities for rich understanding of human decision-making using algorithms