

1. List the elements of  $\{a, ab\}^*$ . Find a way to describe strings in this language, i.e., find a predicate  $P(s)$  such that  $P(s)$  is true iff  $s$  is in  $\{a, ab\}^*$ , for all strings  $s$  over alphabet  $\{a, b\}$ .
2. Find three different examples of a language  $L$  over alphabet  $\{a, b, c\}$  such that  $L = L^*$ .
3. Give a DFA for each language below.
  - a)  $L_1 = \{s \in \{0, 1\}^* : s \text{ contains at least 2 characters and } s\text{'s second character is a } 1 \}$
  - b)  $L_2 = \{s \in \{0, 1\}^* : s \text{ contains fewer than 2 characters}\}$
  - c)  $L_3 = \{s \in \{a, b\}^* : \text{every } a \text{ in } s \text{ is eventually followed by } b\}$ . For example,  $aaab \in L_3$  because there is a  $b$  that follows every  $a$ — even though it is not immediately after the first two  $as$ .
  - d)  $L_4 = \{s \in \{a, b\}^* : \text{the third-last character of } s \text{ is a } b \}$