

Consider the following algorithm.

```
1: function MYSTERY(A,s,f)
2:   # A is a list and s,f are indices such that  $0 \leq s \leq f + 1 \leq \text{length}(A)$ 
3:   if  $s > f$  then
4:     return 0
5:   end if
6:    $m = \lfloor \frac{f-s+1}{4} \rfloor$ 
7:    $res = \text{Mystery}(A, s, s + m - 1)$ 
8:   # loop precondition goes here...
9:   for  $i = s + m, \dots, f - m$  do
10:     $res = res + A[i]$ 
11:  end for
12:  # loop postcondition goes here...
13:   $res = res + \text{Mystery}(A, f - m + 1, f)$ 
14:  return  $res$ 
15: end function
```

1. State clear and precise preconditions for this algorithm.
2. State clear and precise postconditions for this algorithm.
3. Prove the correctness of this algorithm.

Note: You may assume that the loop is correct without proof, as long as you state clear preconditions and postconditions specifically for the loop where indicated by comments.