Give a RE (regexp) and an NFA for each language below.

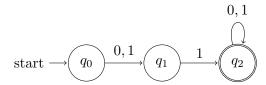
1.  $L_1 = \{s \in \{0,1\}^* : s \text{ contains at least 2 characters and } s$ 's second character is a  $1\}$ 

Ans:

RE:

$$(0+1)1(0+1)^*$$

NFA:



2.  $L_2 = \{s \in \{0,1\}^* : s \text{ contains fewer than 2 characters}\}$ 

Ans:

RE:

$$\epsilon + 0 + 1$$

NFA:

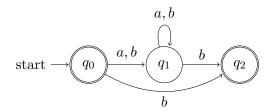
start 
$$\longrightarrow q_0 \xrightarrow{0,1} q_1$$

3.  $L_3 = \{s \in \{a,b\}^* : \text{every } a \text{ in s is eventually followed by } b\}$ 

Ans:

$$(a+b)^*b + \epsilon$$

NFA:



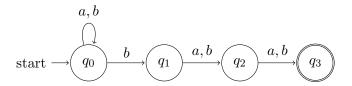
4.  $L_4 = \{s \in \{a,b\}^* : \text{the third-last character of } s \text{ is a } b\}$ 

Ans:

RE:

$$(a+b)^*b(a+b)(a+b)$$

NFA:



5.  $L_5 = \{s \in \{a, b\}^* : s \text{ contains some substring of length 4 whose first and last characters are the same}\}$ 

Ans:

RE:

$$(a+b)^*(a(a+b)(a+b)a+b(a+b)(a+b)b)(a+b)^*$$

NFA:

