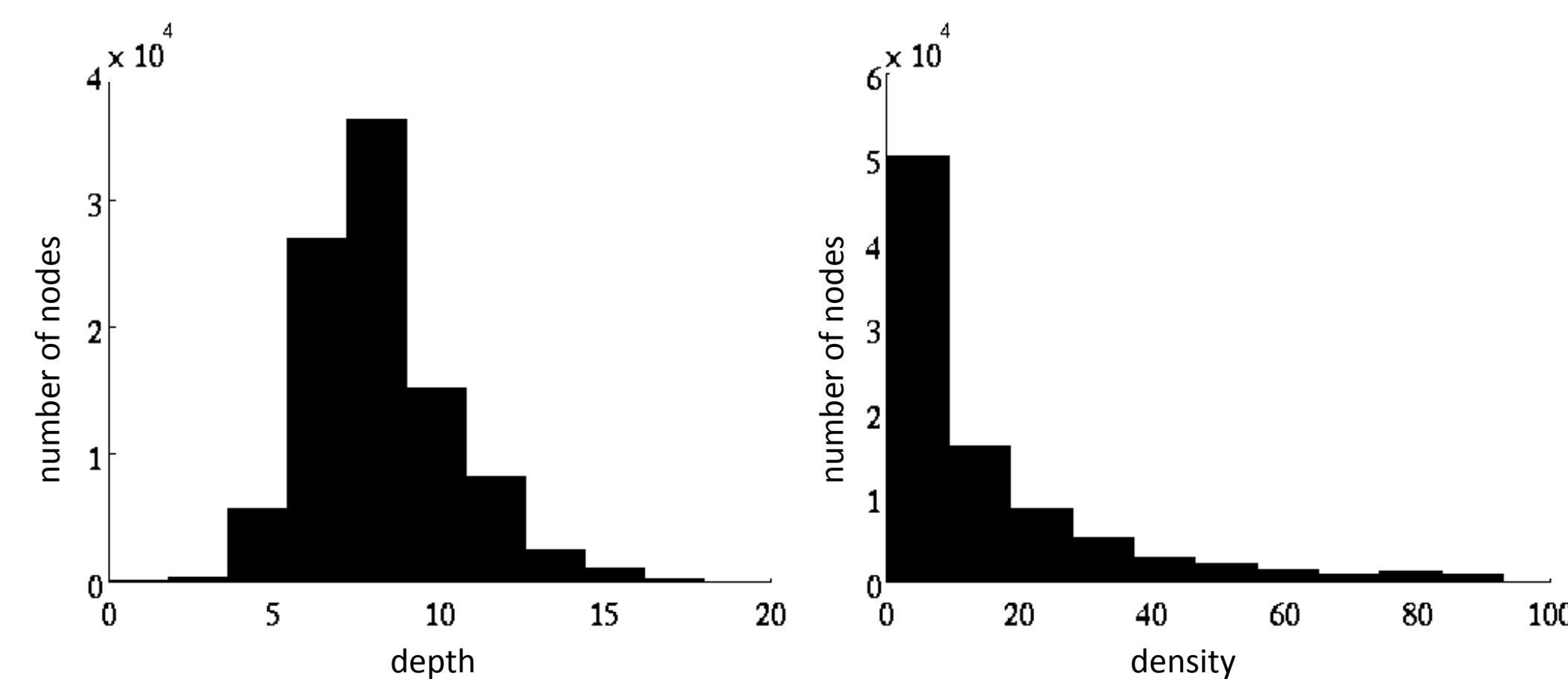


# Refining the Notions of Depth and Density in WordNet-based Semantic Similarity Measures

Tong Wang and Graeme Hirst  
University of Toronto  
{tong, gh}@cs.toronto.edu

## 1. Motivation

- Depth and density
  - Quantitative features of taxonomic structures
  - Used in *WordNet*-based semantic similarity measures (Sussna 1993; Wu and Palmer 1994; Jiang and Conrath 1997)
- Taxonomic depth and density as integers
  - Relative concepts used in absolute terms
  - Superimposing linearity on non-linear quantities



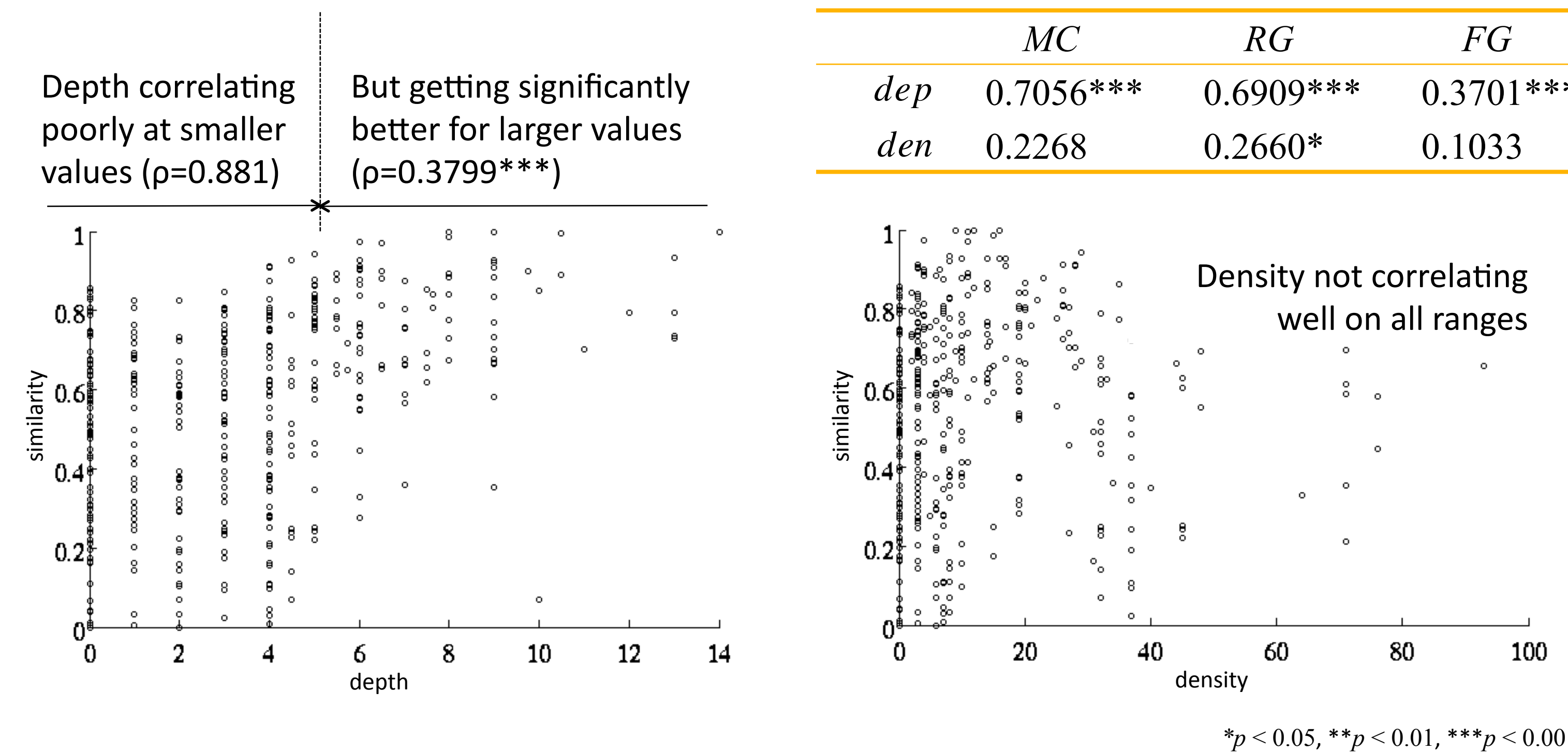
Distribution of depth and density of nodes in WordNet

## 2. Limitations of current definitions

Are depth and density actually related to semantic similarity?

- Gold standard of semantic similarity: human judgment of lexical semantic similarity from psycholinguistic experiments (the *MC*, *RG*, and *FG* datasets)
- Correlation between depth/density and human judgment of similarity: measured by Spearman's Rho

Depth correlating poorly at smaller values ( $\rho=0.881$ )  
But getting significantly better for larger values ( $\rho=0.3799***$ )



\* $p < 0.05$ , \*\* $p < 0.01$ , \*\*\* $p < 0.001$

## 3. Redefining depth and density

Depth

- “Re-curving” a depth value from integer to its cumulative distribution curve:

$$dep_u(c) = \frac{|\{c' \in \text{WN} \mid \{c' : dep(c') \leq dep(c)\}|}{|\text{WN}|}$$

	<i>MC</i>	<i>RG</i>	<i>FG</i>
<i>original</i>	0.7056***	0.6909***	0.3701***
<i>re-curving</i>	0.7201***	0.6798***	0.3751***

Density

- Re-curving does not work well due to Zipfian distribution
- Incorporating *inheritance* in the definition of density:

$$den_i(r) = 0$$

$$den_i(c) = \frac{\sum_{h \in \text{hyper}(c)} den_i(h)}{|\text{hyper}(c)|} + den(c)$$

	<i>MC</i>	<i>RG</i>	<i>FG</i>
<i>before</i>	0.2268	0.2660*	0.1033
<i>re-curving</i>	0.2268	0.2660*	0.1019
<i>inheritance</i>	0.7338***	0.6751***	0.3445***

## 4. Experiments

Do the new definitions contribute to better similarity measures?

- Same similarity gold standard as in section 2
- Re-implement some similarity measures that use depth and density
- Replace depth and density definition to see if there is performance improvement (in terms of correlation with gold standard)
  - Wu and Palmer (1994) – depth only

$$sim(c_1, c_2) = \frac{2 \cdot dep^\alpha(c)}{len(c_1, c) + len(c_2, c) + 2 \cdot dep^\alpha(c)}$$

- Jiang and Conrath (1997) – depth and density

$$w(c, p) = \left( \frac{dep(p) + 1}{dep(p)} \right)^\alpha \times \left[ \beta + (1 - \beta) \frac{\bar{E}}{den(p)} \right] \times [IC(c) - IC(p)]T(c, p)$$

- Parameterization of depth/density components enables investigation of numerical stability

## 5. Results and conclusions

- Refining depth in Wu and Palmer (1994)

	Best <sup>1</sup>			Average <sup>2</sup>		
	<i>MC</i>	<i>RG</i>	<i>FG</i>	<i>MC</i>	<i>RG</i>	<i>FG</i>
<i>dep</i>	0.7671	0.7824	0.3773	0.7612	0.7686	0.3660
<i>dep_u</i>	0.7824	0.7912	0.3946	0.7798	0.7810	0.3787

1. Highest correlation with human judgment among all parameters
2. Average correlation across parameters (indicating numerical stability of parameterization)

- Refining depth and density in Jiang and Conrath (1997)

	Best			Average		
	<i>MC</i>	<i>RG</i>	<i>FG</i>	<i>MC</i>	<i>RG</i>	<i>FG</i>
<i>dep, den</i>	0.7875	0.8111	0.3720	0.7689	0.7990	0.3583
<i>dep_u, den</i>	0.8009	0.8181	0.3804	0.7885	0.8032	0.3669
<i>dep, den_i</i>	0.7882	0.8199	0.3803	0.7863	0.8102	0.3689
<i>dep_u, den_i</i>	0.8065	0.8202	0.3818	0.8189	0.8194	0.3715

- **Both new definitions improve similarity measure performance and numerical stability**
- **Best result achieved using both new definitions together**

## References and acknowledgement

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Lev Finkelstein, Evgeniy Gabrilovich, Yossi Matias, Ehud Rivlin, Zach Solan, Gadi Wolfman, and Eytan Ruppin. Placing search in context: The concept revisited. In *Proceedings of the 10th International Conference on World Wide Web*, pages 406–414. ACM, 2001.

Jay Jiang and David Conrath. Semantic similarity based on corpus statistics and lexical taxonomy. In *Proceedings of International Conference on Research in Computational Linguistics*, 19–33, 1997.

George Miller and Walter Charles. Contextual correlates of semantic similarity. *Language and Cognitive Processes*, 6(1):1–28, 1991.

Herbert Rubenstein and John Goodenough. Contextual correlates of synonymy. *Communications of the ACM*, 8(10):627–633, 1965.

Michael Sussna. Word sense disambiguation for free-text indexing using a massive semantic network. In *Proceedings of the Second International Conference on Information and Knowledge Management*, pages 67–74. ACM, 1993.

Zhibiao Wu and Martha Palmer. Verb semantics and lexical selection. In *Proceedings of the 32nd Annual Meeting of the Association for Computational Linguistics*, pages 133–138. Association for Computational Linguistics, 1994.