# The solution to Q3 (midterm) 

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Q3.
Let $G$ denote the graph in the question and $f$ is a max flow for $G$.
For any edge $e$ of $G$, we just need to increase the capacity if $f(e)>c(e)-1$.
Identify a max flow $f$. Create another graph $G^{\prime}$ similar to $G$ (the same nodes and edges) with new edges' weights. For any edge $e$ in $G$ : if $f(e)>c(e)-1$, set the weight of the corresponding edge in $G^{\prime}$ to $p(e)$; otherwise, set the weight to 0 . We want to find a path from $s$ to $t$ with the smallest weight in this graph (the shortest path from $s$ to $t$ ) that can be done by Dijkstra algorithm. The run time of the algorithm is $\mathcal{O}(m \log n)$.

