

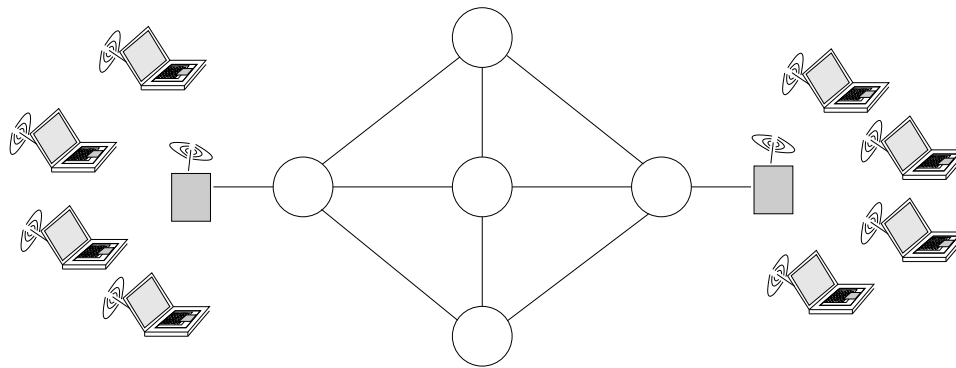
# Rate Control for Random Access Networks: The Finite Node Case

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# Price-Based Rate Control

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- Point-to-Point Wide Area Networks
  - Price-Based Rate Control  
(F. Kelly, S. Low, etc.)
- Local Area Networks
  - Random Access

# Point-to-Point Networks: Price-Based Rate Control

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## Problem Formulation

$$\max_{x_r \geq 0} \sum_r U_r(x_r)$$

subject to

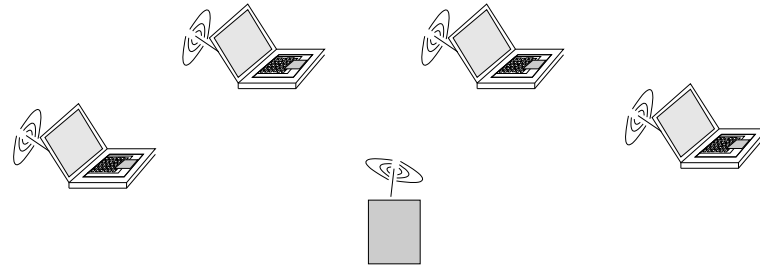
$$Ax \leq C$$

## Rate Control

- Lagrange Multipliers
- “Link Price”
  - Input Rate
  - Backlog
- Rate:  $x_r = D_r(u_r)$ ,  $u_r = \sum_{l \in r} \mu_l$

# Random Access Networks

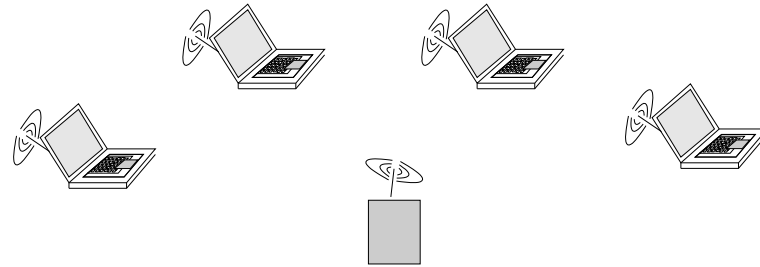
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- Collisions - Backlog - Stability
- Retransmission Strategies for Backlogged Packets
- Rate Control
  - Input Rate?
  - Backlog?
- Channel Feedback
  - Idle/Transmission/Collision

# Random Access Networks

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- Rate Control
  - Collision: Reduce Rate
  - Idle: Increase Rate
- Questions
  - Stable?
  - Operating Point?
  - Packet Scheduling?

## Approach

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- Channel Model: Slotted Aloha
  - CSMA, CSMA/CD
- Use Channel Feedback to Modulate Rate
  - Idle, Successful, Collision Slot
- Markov Chain Formulation
  - Stability
- Infinite Node Model: Operating Point
- Finite Node Model: Packet Scheduling

## Rate Control and Slotted Aloha

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- Poisson Arrival Rate
- Fixed Retransmission Probability  $q, 0 < q < 1$
- Price (Control) Signal  $u$
- Aggregated Transmission Rate  $\lambda(u)$ 
  - Continuous, Strictly Decreasing
  - $\lim_{u \rightarrow \infty} \lambda(u) = 0$
- Collision: Increase Price
- Idle Slot: Decrease Price
- Price Adaptation:  $\alpha < 0, \gamma > 0$

$$u_{t+1} = \left[ u_t + \alpha I[Z_t = 0] + \beta I[Z_t = 1] + \gamma I[Z_t \geq 2] \right]^+$$

## Infinite Node Model: Results

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- Markov Chain  $(n_t, u_t)$
- System is stable.
- (Under suitable conditions) There exists a unique operating point  $(n^*, u^*)$
- We can set  $S^* = \lambda(u^*)$  and  $D^* = n^*/S^*$  by choosing  $\alpha, \beta, \gamma$ .



## Finite Number of Nodes

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- Finite Number of Nodes

$$\lambda(u) = \sum_{m=1}^M \lambda_m(u).$$

- Nodes can have several backlogged packets
- Backlog-Dependant Retransmission Probabilities

$$q_m(n_m) = \begin{cases} n_m q_m, & n_m q_m \leq 1 - \epsilon, \\ 1 - \epsilon, & \text{otherwise,} \end{cases}$$

- Backlog-Independent Retransmission Probabilities,  $q_m$ .

## Finite Number of Nodes: Results

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- “Scheduling” is important
- Service differentiation
  - Rate

$$\lambda(u) = \sum_{m=1}^M \lambda_m(u).$$

- Delay

$$q_m(n_m) = \begin{cases} n_m q_m, & n_m q_m \leq 1 - \epsilon, \\ 1 - \epsilon, & \text{otherwise,} \end{cases}$$

## Backlog-Dependant Retransmission Probabilities

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**Assumption:** “Price tends to increase when all nodes are saturated and retransmit with probability  $1 - \epsilon$ .”

### Case Study

Node	Bandwidth	Delay
1	low	high
2	low	low
3	high	high
4	high	low

## Results

Node $m$	$S_m$	$D_m$
1	0.021	186.7
2	0.021	19.9
3	0.206	116.5
4	0.210	11.8

## Overview

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- Point-to-Point vs. Random Access Networks
- Markov Chain Model
- Operating Point
- Delay and Throughput Differentiation
- End-to-End Rate Control

## Related Work

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- Price-Based Rate Control
  - Frank Kelly, Steven Low,.....
- Rate Control and Slotted Aloha
  - Kleinrock and Lam
  - Mittal and Venetsanopoulos
- TCP over 802.11
  - Cali *et al.*
- Price-Based Rate Control for Random Access Networks
  - Jin and Kesidis
  - Battiti *et al.*